

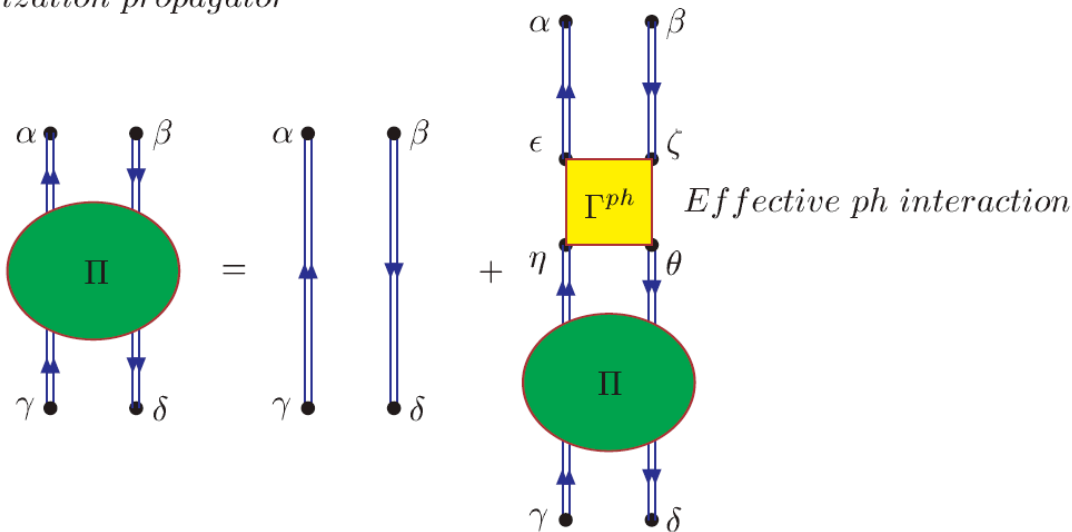
FSI and (e,e'p) \Leftrightarrow analysis

$$\hat{O} = \sum_{\alpha\beta} \langle \alpha | O | \beta \rangle a_{\alpha}^+ a_{\beta} \quad \text{Electron Scattering} \Rightarrow \text{one-body operator}$$

$$\left| \langle \Psi_n^A | \hat{O} | \Psi_0^A \rangle \right|^2 = \sum \langle \alpha | O | \beta \rangle^* \langle \gamma | O | \delta \rangle \langle \Psi_0^A | a_{\beta}^+ a_{\alpha} | \Psi_n^A \rangle \langle \Psi_n^A | a_{\gamma}^+ a_{\delta} | \Psi_0^A \rangle$$

Requires (imaginary part of) **exact** polarization propagator

Polarization propagator



Choose kinematics:
 \Rightarrow only first term

$$\langle \Psi_m^{A+1} | a_{\alpha}^+ | \Psi_0^A \rangle$$

\Rightarrow Elastic scattering
 (phenomenology)

$$\langle \Psi_n^{A-1} | a_{\beta} | \Psi_0^A \rangle$$

“Absolute” spectroscopic factors $\checkmark \Rightarrow$ Quasihole wave function

NSCL 7/27/05

Spectroscopic factors and the physics of the single-particle strength distribution in nuclei

- Lecture 1: 7/18/05 Propagator description of single-particle motion and the link with experimental data
- Lecture 2: 7/19/05 From diagrams to Hartree-Fock and spectroscopic factors < 1
- Lecture 3: 7/20/05 Influence of long-range correlations and the relation to excited states
- Lecture 4: 7/27/05 Role of short-range and tensor correlations associated with realistic interactions. Prospects for nuclei with N very different from Z .
- Lecture 5: 7/28/05 Saturation problem of nuclear matter

Wim Dickhoff
Washington University in St. Louis

Outline

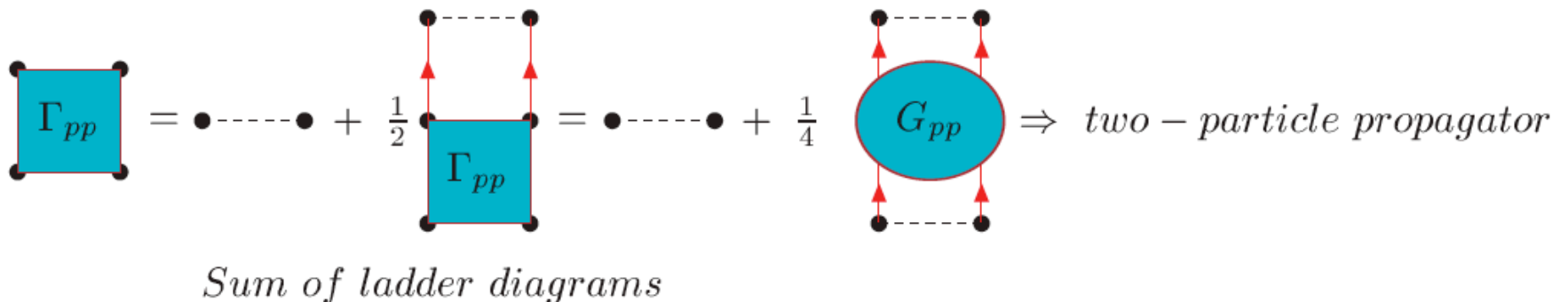
- SRC for free particles
- Ladders in the medium
- Self-energy and Dyson equation
- Nuclear matter simplifications
- Self-consistent Green's functions in nuclear matter & results
- SRC in finite nuclei: where are the high-momentum nucleons
- Summary of sp strength in closed-shell nuclei
- Other nuclei
- N very different from Z
- Nuclear matter with isospin polarization

Short-range correlations for two free particles

Solve the Schrödinger equation or the equivalent “ T ”-matrix

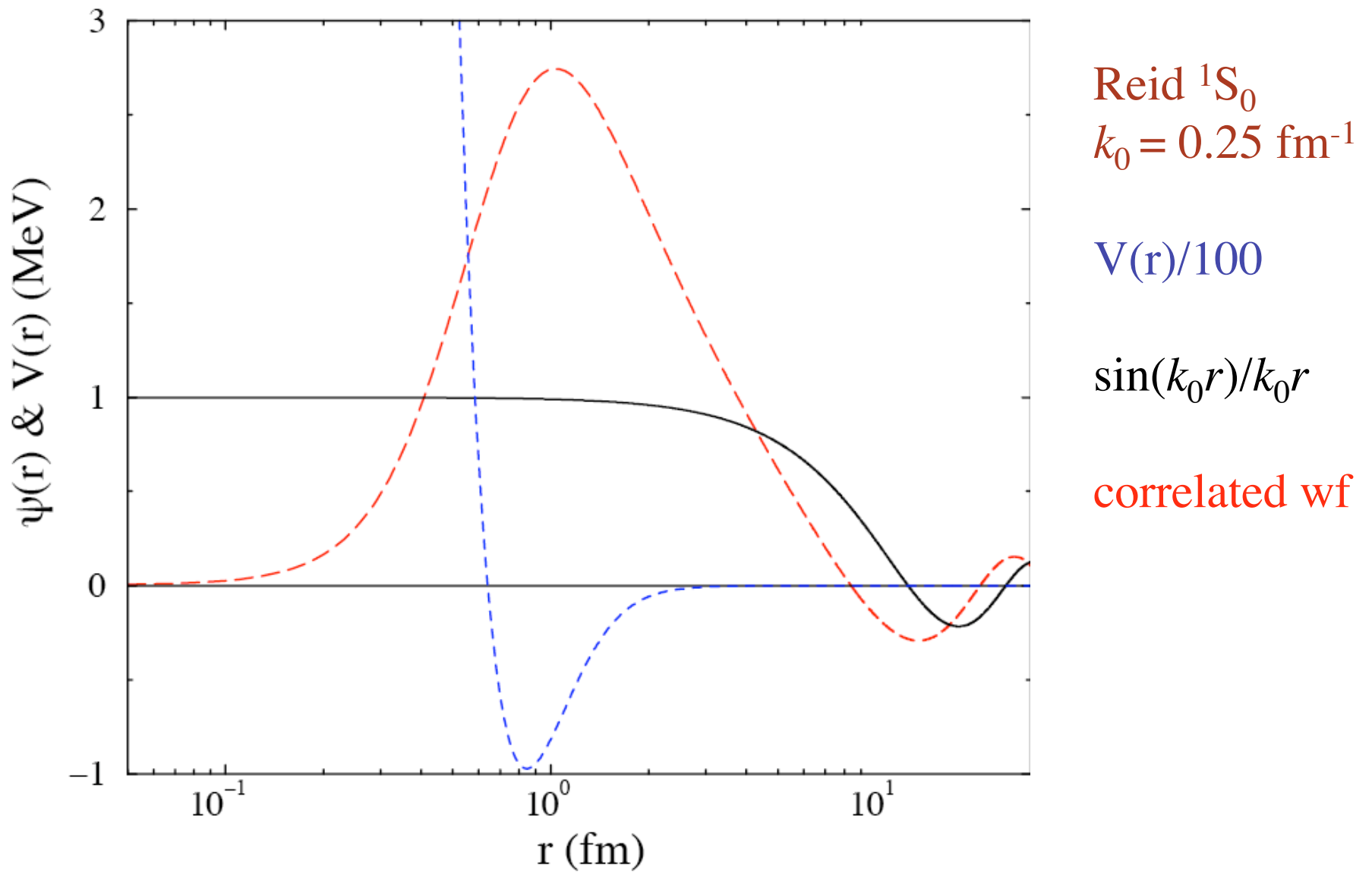
$$\langle k\ell | \Gamma_{pp}^{JST}(k_0) | k'\ell' \rangle = \langle k\ell | V^{JST} | k'\ell' \rangle + \frac{m}{2\hbar^2} \sum_{\ell''} \int_0^\infty \frac{dq}{(2\pi)^3} q^2 \langle k\ell | V^{JST} | q\ell'' \rangle \frac{1}{k_0^2 - q^2 + i\eta} \langle q\ell'' | \Gamma_{pp}^{JST}(k_0) | k'\ell' \rangle$$

Effective interaction



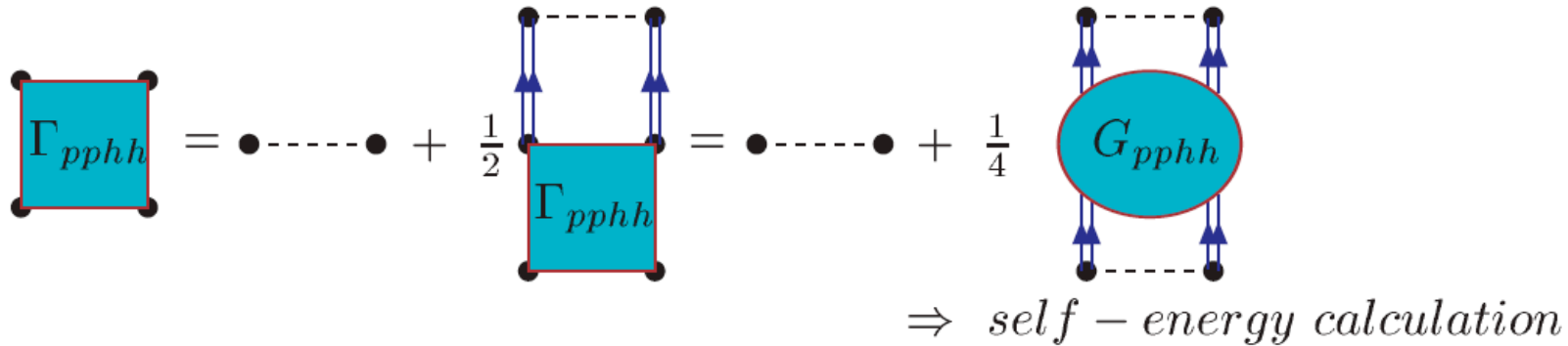
Sum of ladder diagram takes care of SRC
Also in the medium!

Relative wave function and potential



Ladder diagrams in the medium (options)

Ladders in the medium



$$\langle k\ell | \Gamma_{pphh}^{JST}(K, E) | k' \ell' \rangle = \langle k\ell | V^{JST} | k' \ell' \rangle + \frac{1}{2} \sum_{\ell''} \int_0^{\infty} \frac{dq}{(2\pi)^3} q^2 \langle k\ell | V^{JST} | q\ell'' \rangle G_{pphh}^f(q; K, E) \langle q\ell'' | \Gamma_{pphh}^{JST}(K, E) | k' \ell' \rangle$$

G_{pphh}^f has different form depending on the level of sophistication

Nuclear matter:

$$G_{BG}^f(k_1, k_2; E) = \frac{\theta(k_1 - k_F) \theta(k_2 - k_F)}{E - \varepsilon(k_1) - \varepsilon(k_2) + i\eta}$$

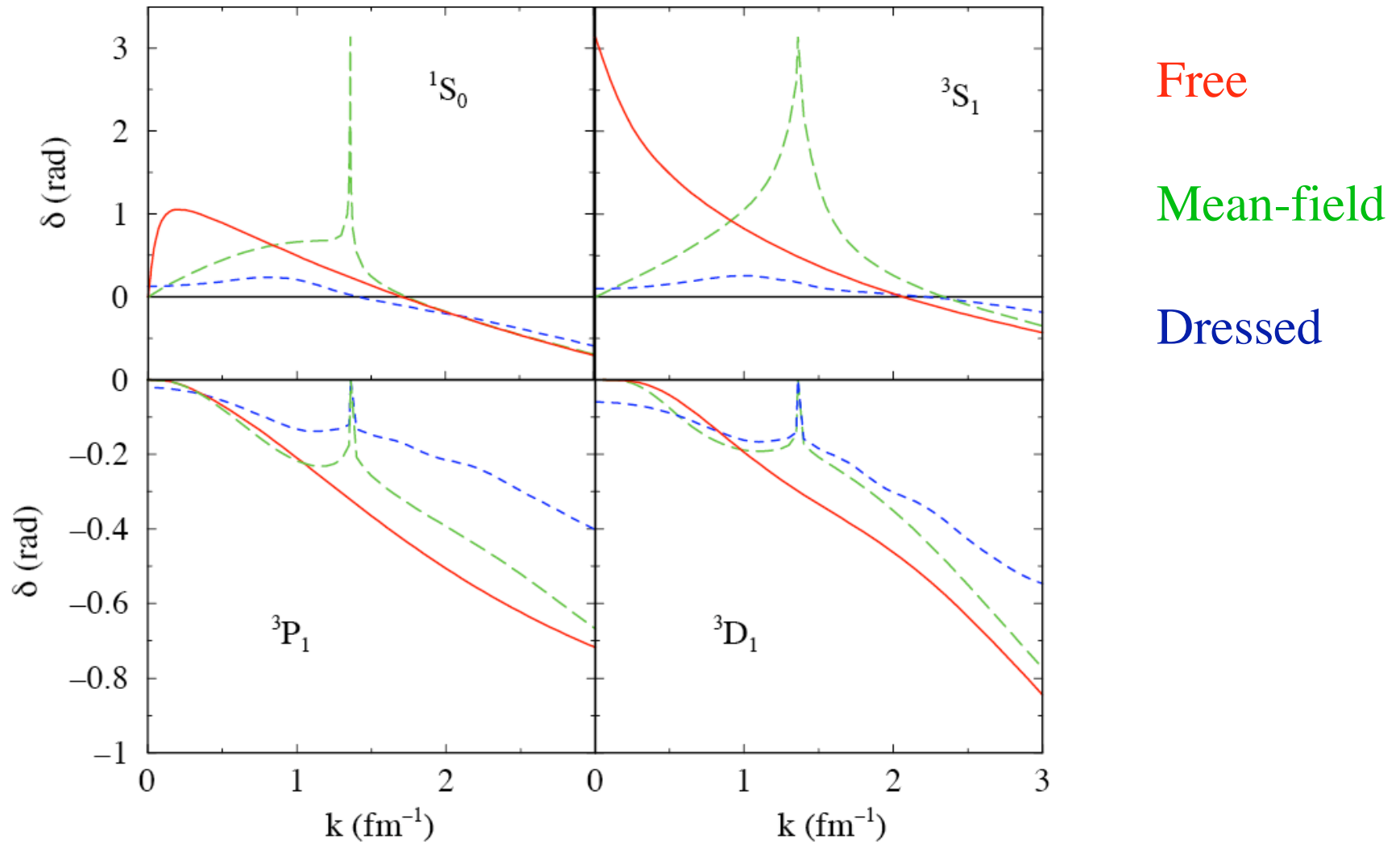
Bethe-Goldstone

$$G_{GF}^f(k_1, k_2; E) = \frac{\theta(k_1 - k_F) \theta(k_2 - k_F)}{E - \varepsilon(k_1) - \varepsilon(k_2) + i\eta} - \frac{\theta(k_F - k_1) \theta(k_F - k_2)}{E - \varepsilon(k_1) - \varepsilon(k_2) - i\eta}$$

Galitskii-Feynman

$$G_{pphh}^f(k_1, k_2; E) = \int_{\varepsilon_F}^{\infty} dE_1 \int_{\varepsilon_F}^{\infty} dE_2 \frac{S_p(k_1; E_1) S_p(k_2; E_2)}{E - E_1 - E_2 + i\eta} - \int_{-\infty}^{\varepsilon_F} dE_1 \int_{-\infty}^{\varepsilon_F} dE_2 \frac{S_h(k_1; E_1) S_h(k_2; E_2)}{E - E_1 - E_2 - i\eta} \quad \text{SC}$$

Phase shifts for dressed nucleons



PRC60, 064319 (1999) also PRC58, 2807 (1998)

Dyson equation and spectral functions in nuclear matter (some simplifications)

$$G(k; E) = G^{(0)}(k; E) + G^{(0)}(k; E)\Sigma(k; E)G(k; E) \quad \text{Dyson equation}$$

$$= \frac{1}{E - \varepsilon(k) - \Sigma(k; E)}$$

$$G^{(0)}(k; E) = \frac{\theta(k - k_F)}{E - \varepsilon(k) + i\eta} + \frac{\theta(k_F - k)}{E - \varepsilon(k) - i\eta} \quad \text{Noninteracting sp propagator}$$

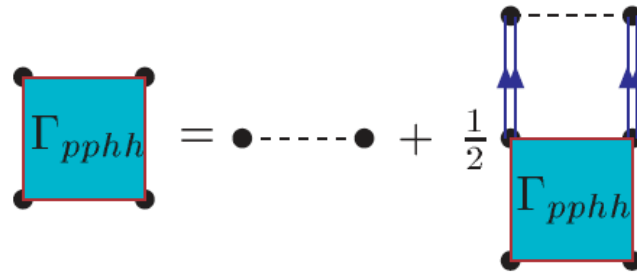
$$S_p(k; E) = \frac{1}{\pi} \frac{\text{Im}\Sigma(k; E)}{\left(E - \varepsilon(k) - \text{Re}\Sigma(k; E)\right)^2 + \left(\text{Im}\Sigma(k; E)\right)^2} \quad \text{particle spectral function}$$

$$S_h(k; E) = \frac{1}{\pi} \frac{\text{Im}\Sigma(k; E)}{\left(E - \varepsilon(k) - \text{Re}\Sigma(k; E)\right)^2 + \left(\text{Im}\Sigma(k; E)\right)^2} \quad \text{hole spectral function}$$

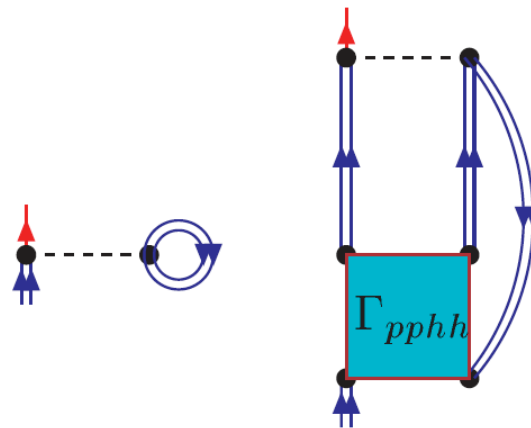
$$G(k; E) = \int_{\varepsilon_F}^{\infty} dE' \frac{S_p(k; E')}{E - E' + i\eta} + \int_{-\infty}^{\varepsilon_F} dE' \frac{S_h(k; E')}{E - E' - i\eta}$$

Again:
numerator sp strength
denominator where

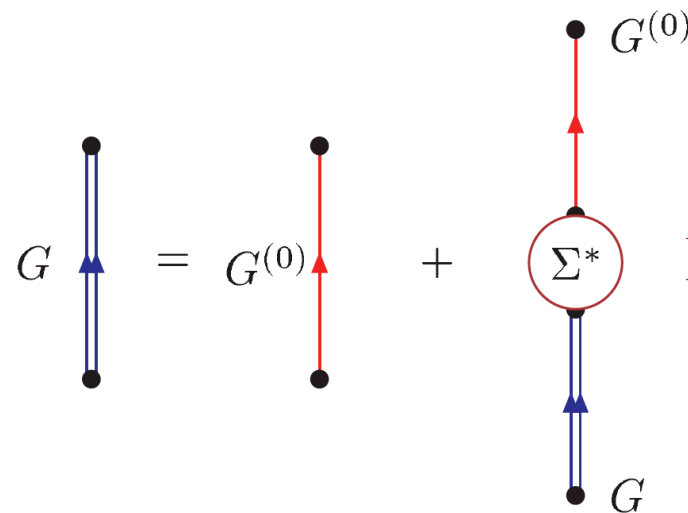
Self-consistency



Interaction



Self-energy

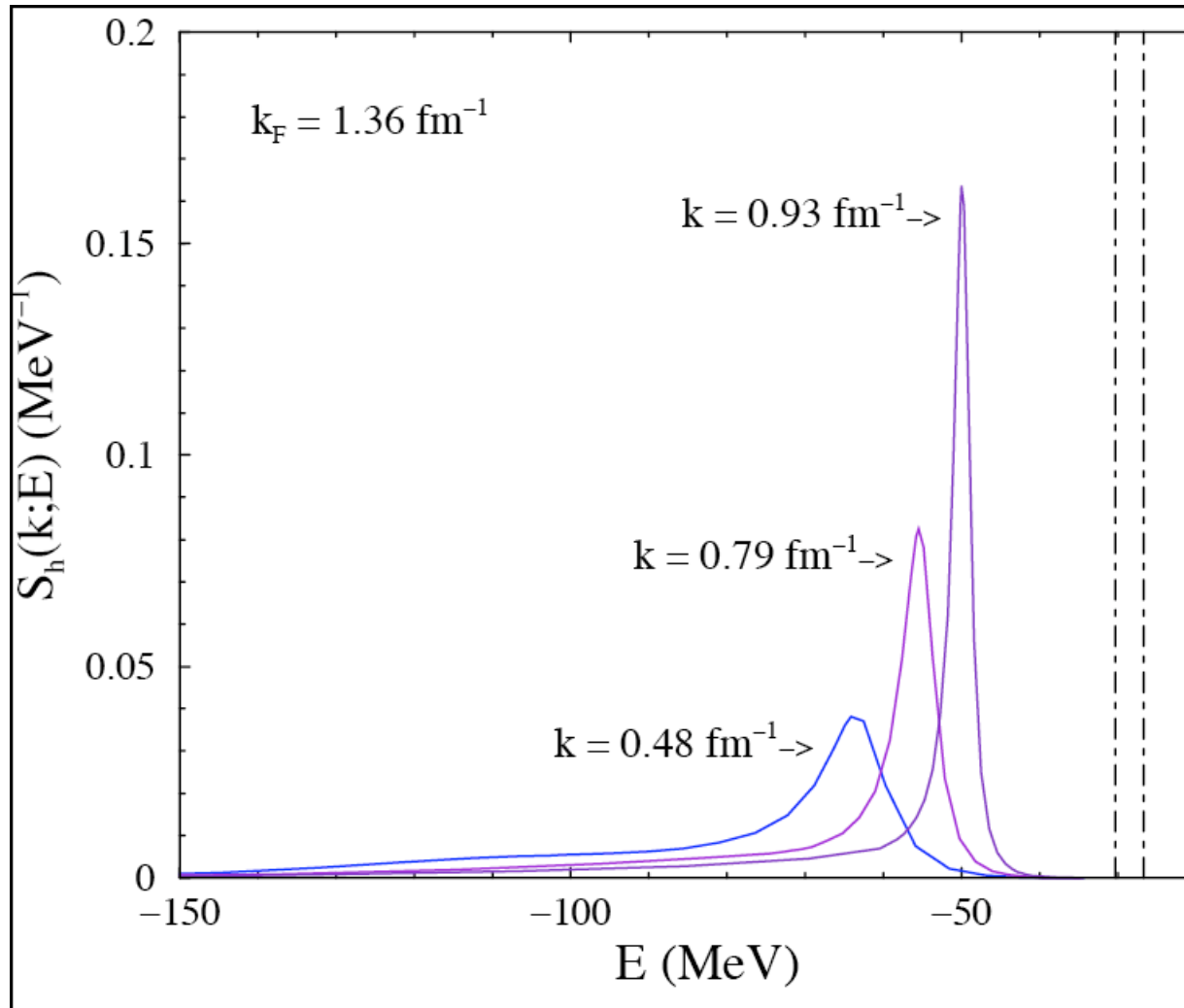


Dyson equation

Recent developments

- St. Louis ⇒ Complete self-consistency for spectral functions
<http://wuphys.wustl.edu/~wimd/thesis1016.pdf>
- Ghent ⇒ Discrete method
- Cracow ⇒ Separable & soft interactions
- Tübingen ⇒ Finite temperature & soft interactions
- Giessen ⇒ Interaction related to cross section

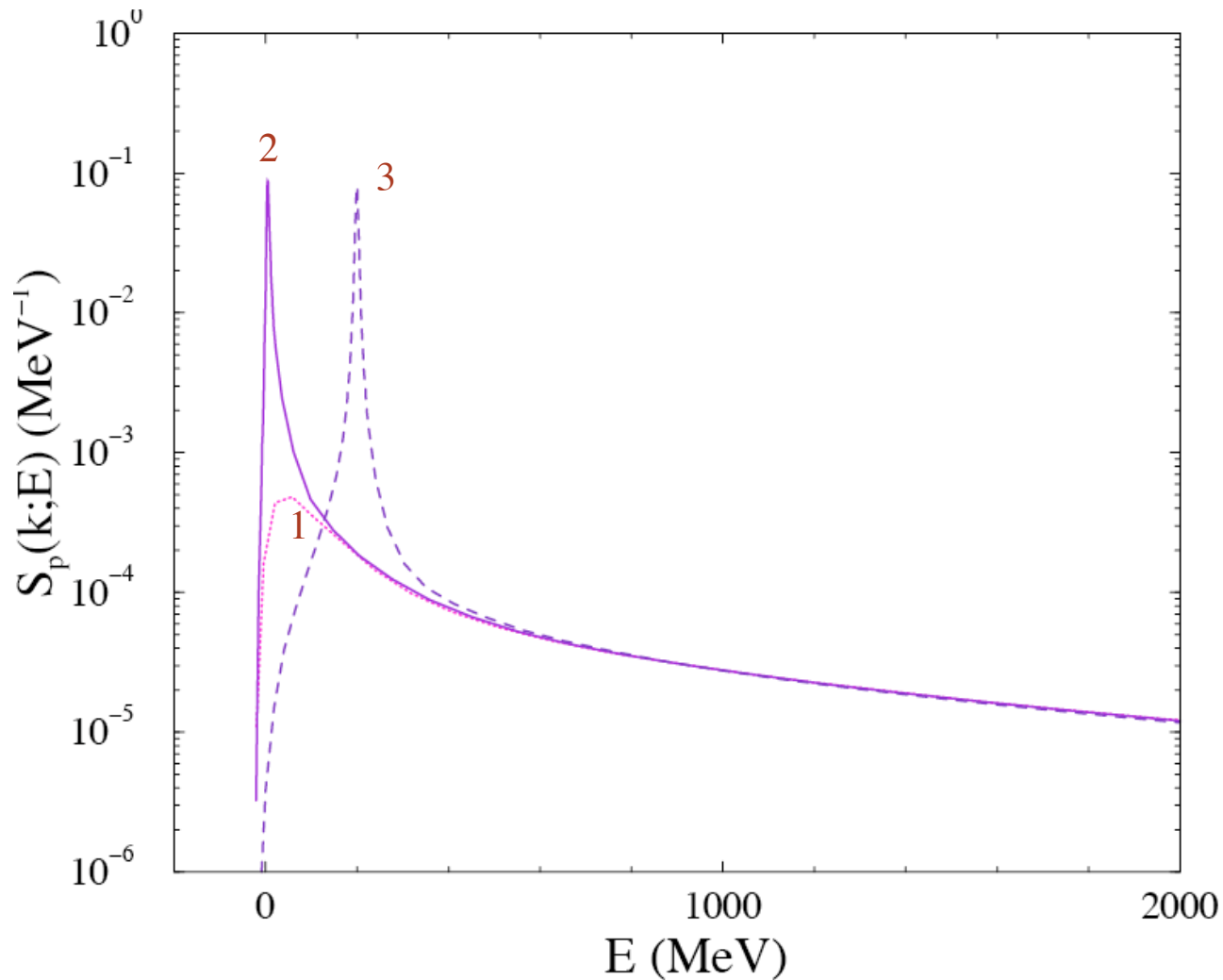
Illustrative results for mean-field input



Strength distribution as in nuclei ...

peak strength +10% at lower energy + global depletion!!

Where does the strength go?



All tails the same!
 \Rightarrow SRC

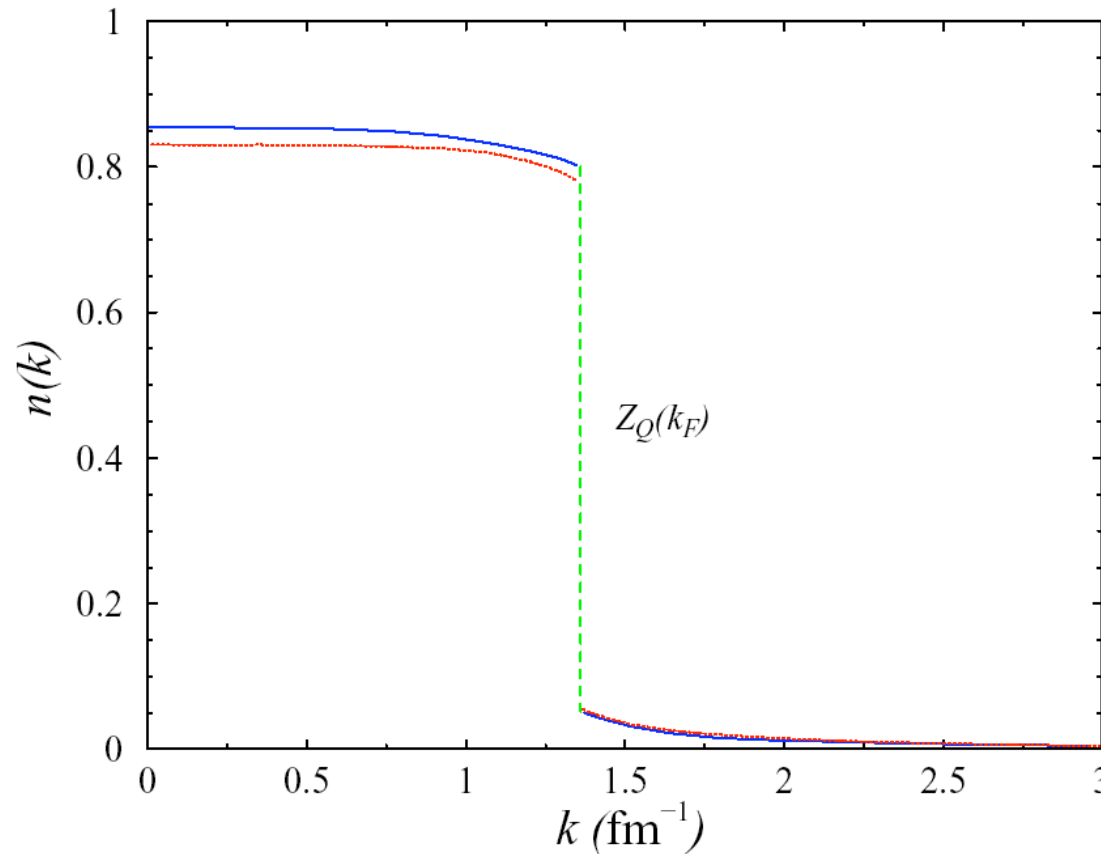
$$k_1 = 0.79 \text{ fm}^{-1}$$
$$k_2 = 1.74 \text{ fm}^{-1}$$
$$k_3 = 3.51 \text{ fm}^{-1}$$

$k < k_F$: 17% $> \varepsilon_F$ with 13% above 100 MeV (7% above 500 MeV)

Without tensor force only 10.5% above ε_F

Short-range correlations in nuclear matter and $n(k)$

$n(k=0) = 0.83 / 0.85 \Rightarrow$ finite nuclei



$$n(k) = \int_{-\infty}^{\varepsilon_F} dE S_h(k; E)$$

Reid soft core
 $k_F = 1.36 \text{ fm}^{-1}$

Old prediction!
New result

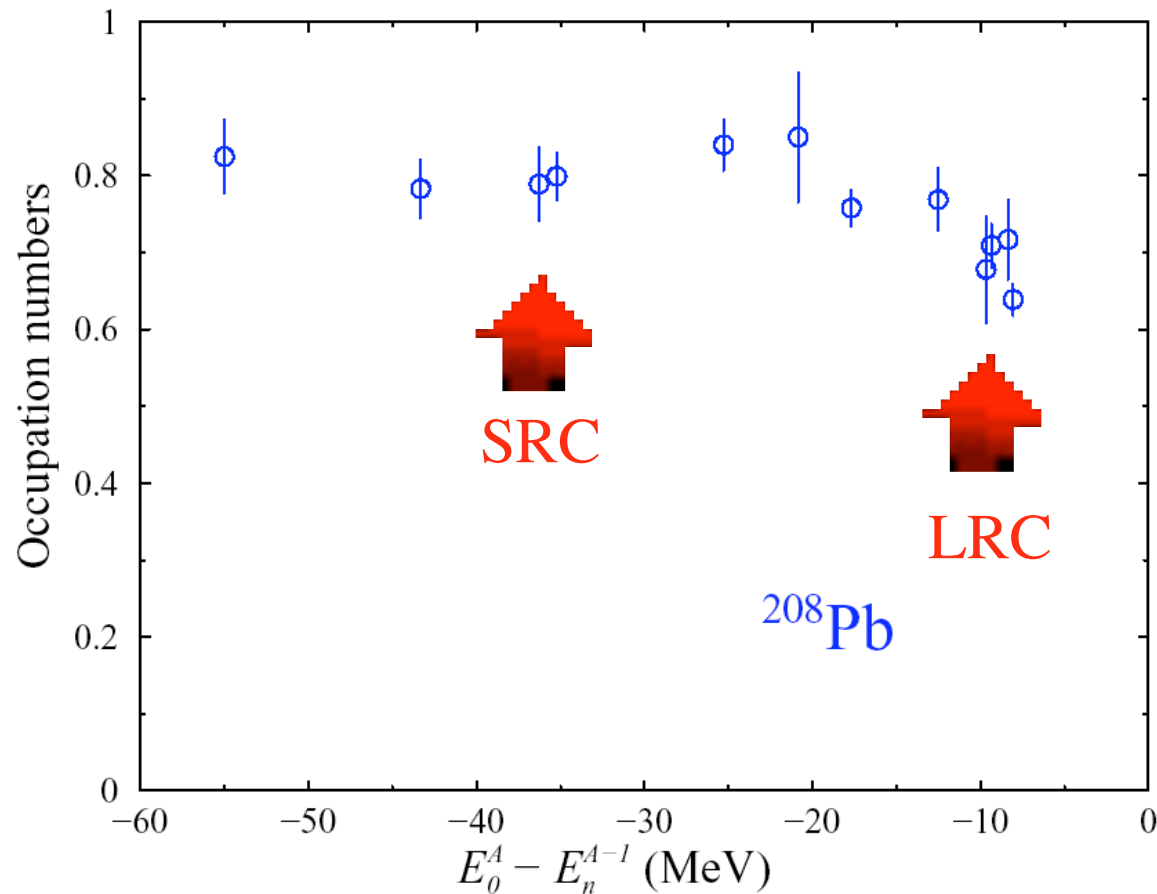
$$Z_Q(k_F) = 0.72$$

$$Z_Q(k_F) = 0.75$$

B.E. Vonderfecht et al. Nucl. Phys. A555, 1 (1993)
E.R. Stoddard, thesis (self-consistent ladders)

M. van Batenburg (thesis, 2001) & L. Lapikás from ^{208}Pb (e,e'p) ^{207}Tl

Occupation of deeply-bound proton levels from **EXPERIMENT**



Up to 100 MeV
missing energy
and
270 MeV/c
missing momentum

Covers the whole
mean-field domain
for the FIRST time!!

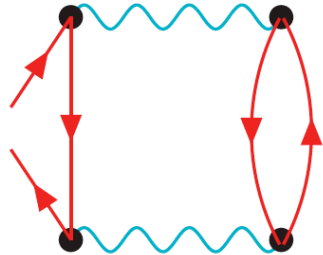
Confirmation of theory

Two effects associated with short-range correlations

- Depletion of the Fermi sea
- Admixture of high-momentum components to replace depleted strength

Location of high-momentum components

high momenta



require specific intermediate states

External line k (large).

Intermediate holes $< k_F$, say total momentum ~ 0 .

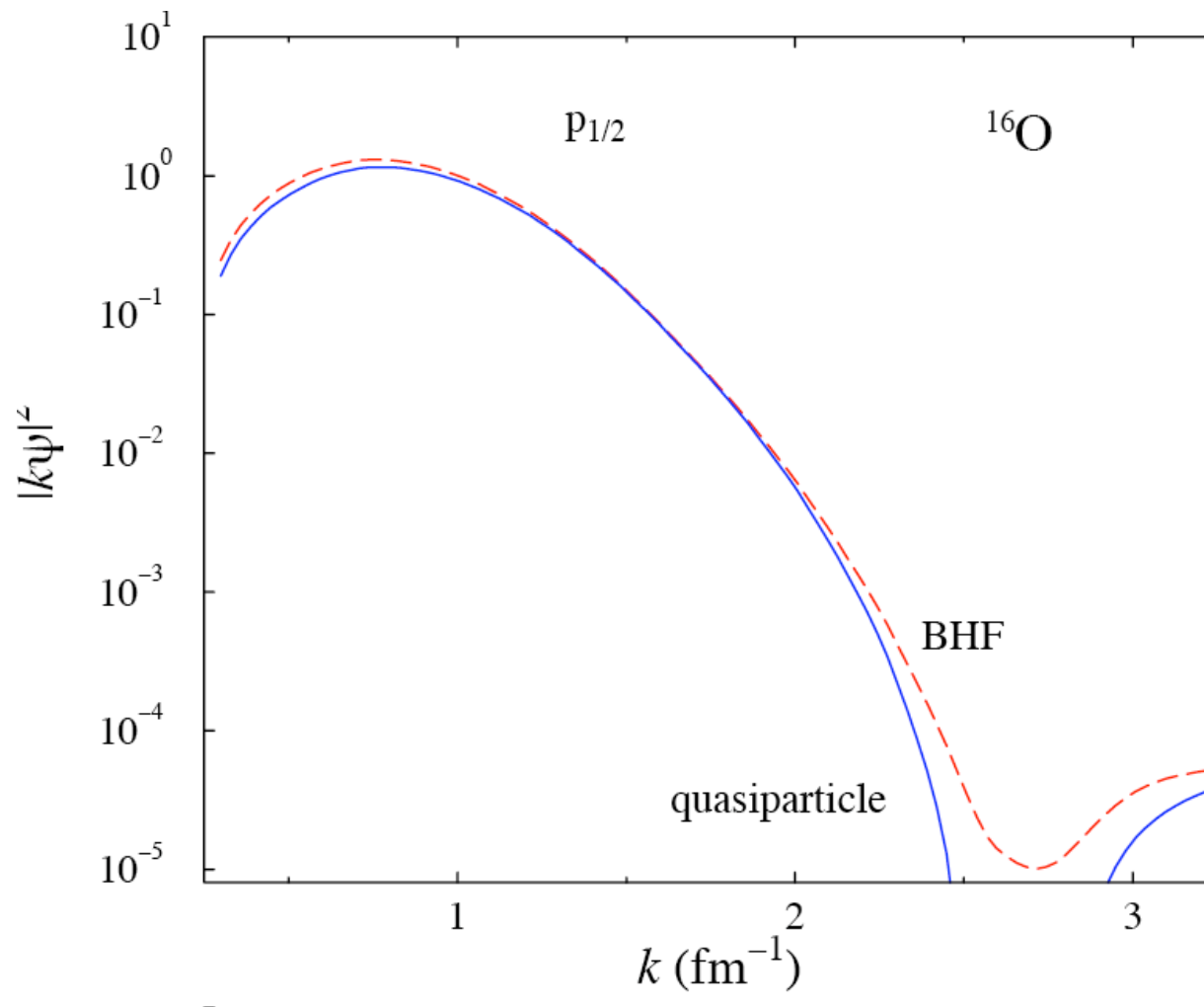
Momentum conservation: intermediate particle $-k$

\Rightarrow Energy intermediate state $\sim \langle \varepsilon_{2h} \rangle - \varepsilon(k)$

\Rightarrow the higher k the more negative the location of its strength

\Rightarrow no high-momentum components near ε_F

SRC (only) calculated in ^{16}O



No enhancement
of high k near ϵ_F

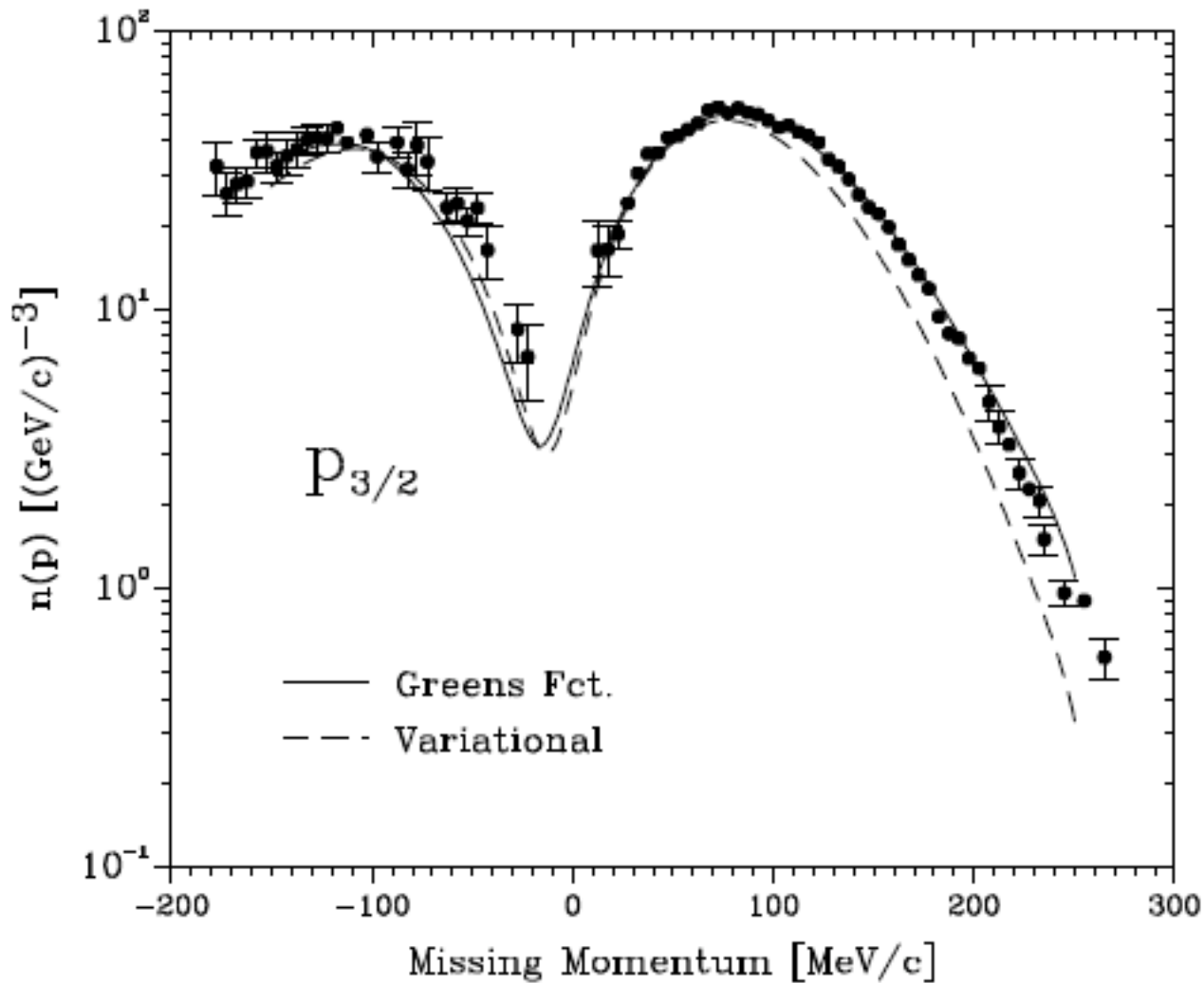
Not observed
experimentally
either!

PRL73,2684(1994)

PLB344,85(1995)

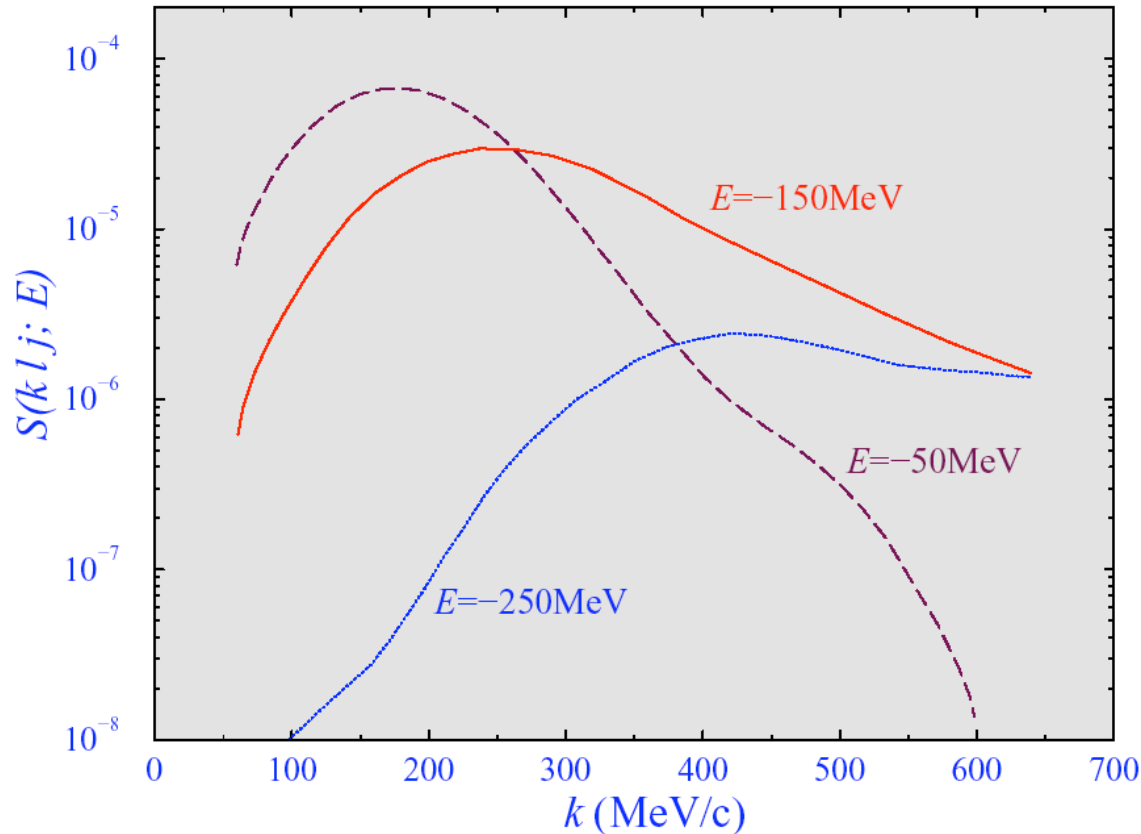
Strength depleted
by 10% due to SRC

Quality of quasihole wave function



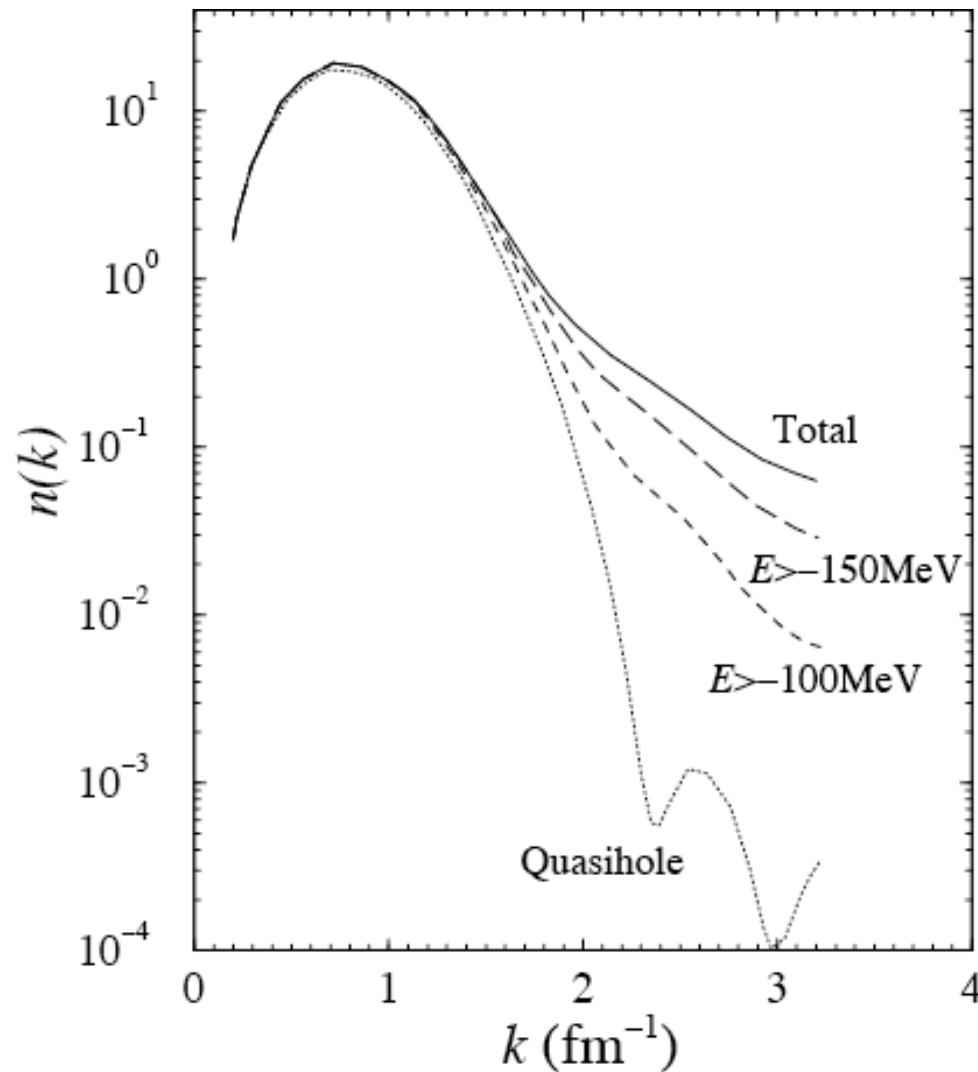
PRC55, 810 (1997)

Prediction of high-momentum components



$p_{1/2}$ spectral function at fixed energies in ^{16}O
Phys. Rev. C49, R17 (1994)

Momentum distribution ^{16}O



Confirms expectation:

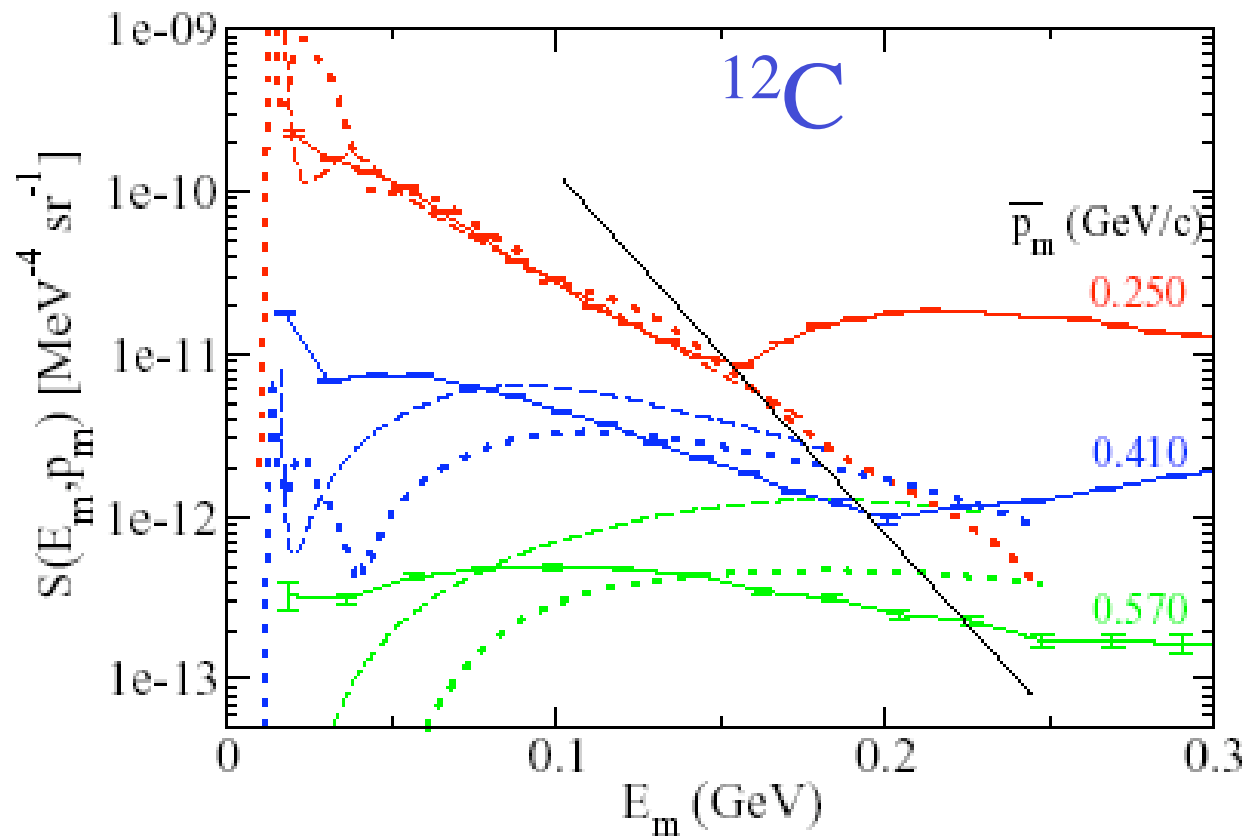
High momentum nucleons
can be found at large
negative energies

Where are the last protons? Answer is coming!

JLab data
PRL **93**,182501 (2004)
Rohe et al.

Location of high-
momentum components

Integrated strength ✓



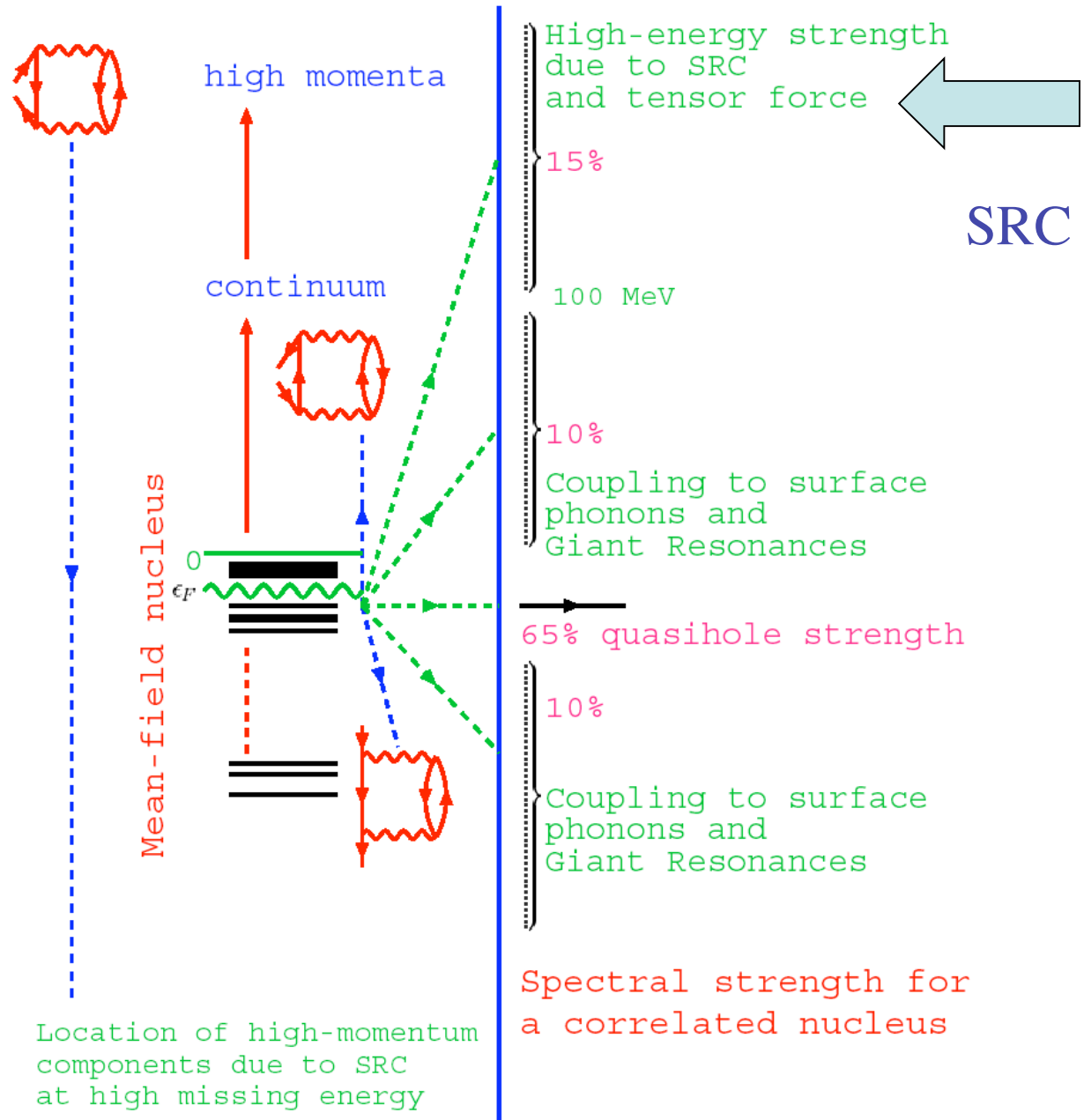
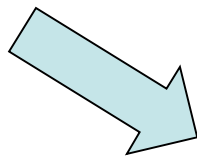
We now essentially know what all the protons are doing in a “closed-shell” nucleus !!!

- Unique for a **correlated** many-body system
- Information available for electrons in atoms (Hartree-Fock)
- **Not** for electrons in solids
- **Not** for atoms in quantum liquids
- **Not** for quarks in nucleons

⇒ **Study the nucleus for its intrinsic interest as a quantum many-body problem!**

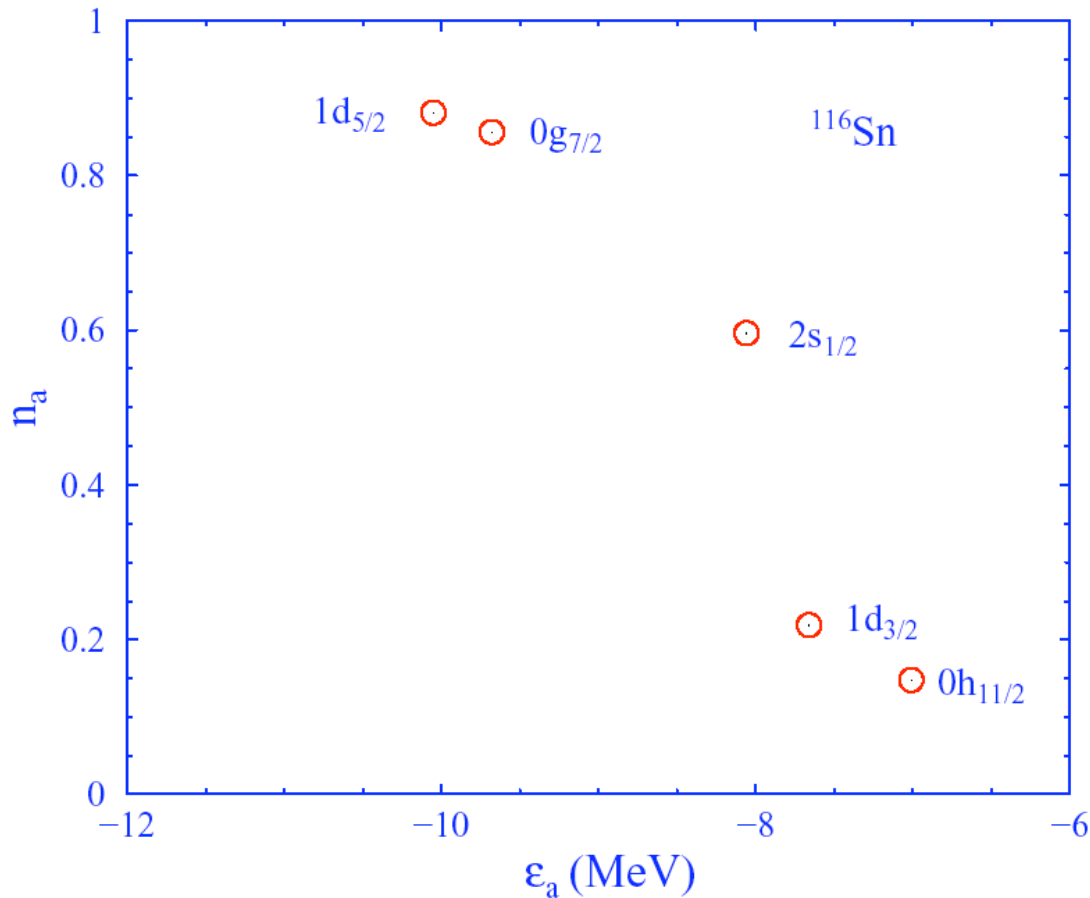
Location of single-particle strength in nuclei

SRC



What about open-shell systems?

Semi-magic nuclei
Green's function calculation



SRC the same
GRs similar

only difference
near ϵ_F

removal &
addition
probabilities
similar size
for $2s_{1/2}$!!

\Rightarrow pairing

Deformation?

$^{142}\text{Nd}(e,e'p)$ $Z=60$; $N=82$ compare with $^{146}\text{Nd}(e,e'p)$ $Z=60$; $N=86$
 Nucl. Phys. **A560**, 811 (1993)

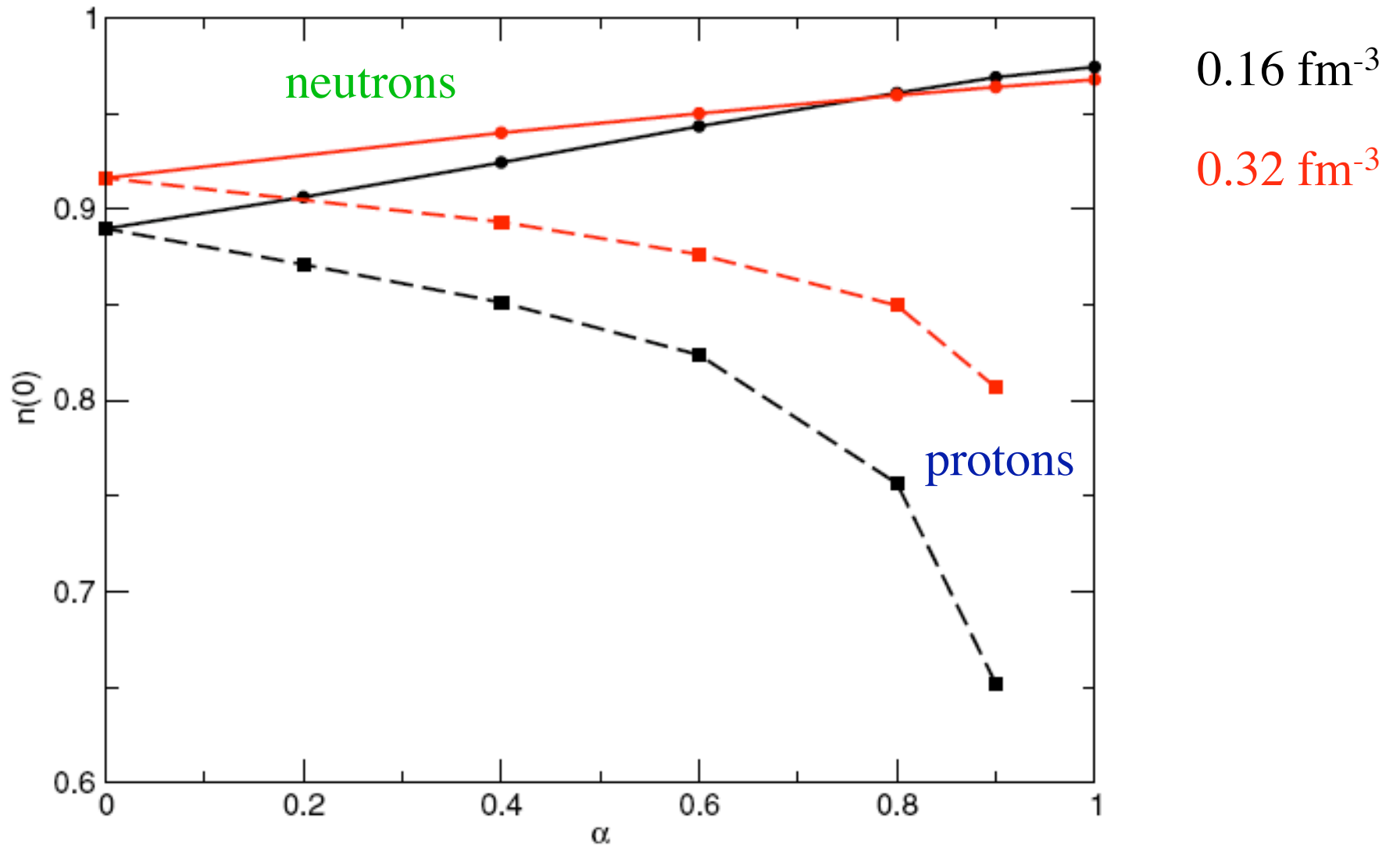
E_x ^{141}Pr	J^π	S_{exp}
0.000	$5/2^+$	0.23
0.145	$7/2^+$	0.39
1.118	$11/2^-$	0.05
1.298	$1/2^+$	0.03

	E_x ^{145}Pr	J^π	S_{exp}
	0.000	$7/2^+$	0.19
	0.063	$5/2^+$	0.17
	0.189	$5/2^+$	0.03
Wave functions in both	0.348	$3/2^+$	0.02
nuclei are the same!	0.555	$7/2^+$	0.03

Systems with N very different from Z ?

- SRC still the same (tensor force disappears for n and “increases” for p for $N > Z$)
(see PRC71,014313(2005))
- Collectivity of excited states is reduced
So less fragmentation
and removal of sp strength becomes
more like mean-field (+ SRC+ whatever is left of tensor force for n but perhaps strong effect for p)
- Continuum effects (soft dipoles ...)

SCGF for isospin-polarized nuclear matter



asymmetry

PRC71,014313(2005)