

# Probing heavy neutrino oscillation and associated CP violation at future hadron colliders

Yongchao Zhang (張永超) Washington University in St. Louis

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> > based on

P. S. B. Dev, R. N. Mohapatra & YCZ, 1904.04787

# Seesaw mechanism

Minkowski, '77; Mohapatra & Senjanovic, '80; Yanagida, '79; Gell-Mann, Ramond & Slansky, '79; Glashow, '80



#### $m_{ u}\simeq -m_D M_N^{-1} m_D^{\mathsf{T}}$

At least two heavy right-handed neutrinos (RHNs) to generate the tiny neutrino masses. ("fair-play rule")

#### Seesaw scenarios

- In pure type-I seesaw and  $U(1)_{B-L}$  gauge extension of SM, RHN mixing and associated CP violation signatures depend on heavy-light neutrino mixing. Thanks to the discussions with Shun Zhou [Chao, Si, Zheng, Zhou '09]
- In the left-right model based on the gauge group  $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$ :

[Pati & Salam, '74; Mohapatra & Pati, '75; Senjonavić & Mohapatra, '75]

$$Q_{L} = \begin{pmatrix} u_{L} \\ d_{L} \end{pmatrix} \in \left(\mathbf{2}, \mathbf{1}, \frac{1}{3}\right) \stackrel{\mathcal{P}}{\leftrightarrow} Q_{R} = \begin{pmatrix} u_{R} \\ d_{R} \end{pmatrix} \in \left(\mathbf{1}, \mathbf{2}, \frac{1}{3}\right)$$
$$\Psi_{L} = \begin{pmatrix} \nu_{L} \\ e_{L} \end{pmatrix} \in \left(\mathbf{2}, \mathbf{1}, -1\right) \stackrel{\mathcal{P}}{\leftrightarrow} \Psi_{R} = \begin{pmatrix} N_{R} \\ e_{R} \end{pmatrix} \in \left(\mathbf{1}, \mathbf{2}, -1\right)$$

The RHN mixing and CP violation can be measured at colliders.

• This can be used to directly test TeV-scale leptogenesis at future hadron colliders!

# Flavor dependence of same-sign dilepton signals



- The "smoking-gun" signal of W<sub>R</sub> and N! [Keung & Senjanović, '83]
- With only one RHN, or the production and decays of RHNs not interfering coherently:

$$\Gamma(N \to \ell^+ jj) = \Gamma(N \to \ell^- jj) \implies \mathcal{N}(\ell^\pm \ell^\pm) = \mathcal{N}(\ell^+ \ell^-)$$

 If we have more than one RHNs, and there are mixing and CPV in the RHN sector [Dev & Mohapatra, '15; Gluza, Jelinski & Szafron, '16; Anamiati, Hirsch & Nardi, '16; Antusch, Cazzato & Fischer, '17; Das, Dev & Mohapatra, '17]

$$\begin{split} &\Gamma(N_{\alpha} \to \ell_{\beta}^{+}jj) = \Gamma(N_{\alpha} \to \ell_{\beta}^{-}jj), \quad \text{but} \quad \mathcal{N}(\ell_{\alpha}^{\pm}\ell_{\beta}^{\pm}) \neq \mathcal{N}(\ell_{\alpha}^{+}\ell_{\beta}^{-}), \\ &\mathcal{N}(\ell_{\alpha}^{+}\ell_{\beta}^{+}) \neq \mathcal{N}(\ell_{\alpha}^{-}\ell_{\beta}^{-}) \text{ (CP-induced effects)} \end{split}$$

# RHN mixing and CP violation

Some assumptions

• Only two RHNs  $N_{e,\mu}$  mixing with each other; the third one  $N_{\tau}$  does not mix with  $N_{e,\mu}$ :

$$\begin{pmatrix} \mathsf{N}_{e} \\ \mathsf{N}_{\mu} \end{pmatrix} = \begin{pmatrix} \cos \theta_{R} & \sin \theta_{R} e^{-i\delta_{R}} \\ -\sin \theta_{R} e^{i\delta_{R}} & \cos \theta_{R} \end{pmatrix} \begin{pmatrix} \mathsf{N}_{1} \\ \mathsf{N}_{2} \end{pmatrix},$$

• The mass relation  $M_{1,2} < M_{W_R}$  (and  $M_3 > M_{W_R}$ ):

on-shell production of RHNs from  $W_R$  decay:  $W_R^{\pm} \rightarrow \ell_{\alpha}^{\pm} N_{\alpha}$ 

# Same-sign charge asymmetry (SSCA)

Define the same-sign charge asymmetry (SSCA)

$$\begin{aligned} \mathcal{A}_{\alpha\beta} &\equiv \frac{\mathcal{N}(\ell_{\alpha}^{+}\ell_{\beta}^{+}) - \mathcal{N}(\ell_{\alpha}^{-}\ell_{\beta}^{-})}{\mathcal{N}(\ell_{\alpha}^{+}\ell_{\beta}^{+}) + \mathcal{N}(\ell_{\alpha}^{-}\ell_{\beta}^{-})} \\ &= \frac{\sigma(pp \to W_{R}^{+})\mathcal{R}(\ell_{\alpha}^{+}\ell_{\beta}^{+}) - \sigma(pp \to W_{R}^{-})\mathcal{R}(\ell_{\alpha}^{-}\ell_{\beta}^{-})}{\sigma(pp \to W_{R}^{+})\mathcal{R}(\ell_{\alpha}^{+}\ell_{\beta}^{+}) + \sigma(pp \to W_{R}^{-})\mathcal{R}(\ell_{\alpha}^{-}\ell_{\beta}^{-})} \end{aligned}$$

Combing both the three-body decays of  $N_{\alpha}$  through the gauge couplings to  $W_R$  boson  $(1 - BR_y)$  and two-body decays of  $N_{\alpha}$  through the Yukawa couplings via heavy-light neutrino mixing  $(BR_y)$ 

$$\mathcal{R}(\ell_{\alpha}^{\pm}\ell_{\beta}^{\pm}) \simeq \underbrace{(1 - \mathrm{BR}_{y})\mathcal{R}(\ell_{\alpha}^{\pm}\ell_{\beta}^{\pm})}_{3\text{-body decay ctrb.}} + \underbrace{\frac{1}{4}}_{2\text{-body decay ctrb.}} \underbrace{\frac{1}{4}}_{2\text{-body decay ctrb.}} \underbrace{\frac{1}{4}}_{2\text{-body decay ctrb.}} \underbrace{\frac{1}{4}}_{3\text{-body de$$

# 3-body and 2-body decay contributions

• Three-body decays  $N_{\alpha} \rightarrow \ell_{\beta}^{\pm} j j$ , in the limit of  $\Gamma_1 = \Gamma_2$ , with  $x \equiv \Delta E_N / \Gamma_{\text{avg}}$ [normalization condition  $\sum_{\alpha,\beta=e,\mu} R(\ell_{\alpha}^{\pm}\ell_{\beta}^{\pm}) = 1$ ]

$$\begin{split} & R(e^{\pm}\mu^{\pm}) = R(\mu^{\pm}e^{\pm}) \simeq \frac{1}{4}\sin^2 2\theta_R \left(1 - \frac{\cos 2\delta_R \pm x\sin 2\delta_R}{1 + x^2}\right), \\ & R(e^{\pm}e^{\pm}) \simeq R(\mu^{\pm}\mu^{\pm}) \simeq \frac{1}{2} - R(e^{\pm}\mu^{\pm}), \end{split}$$

• Two-body decays  $N_{lpha} 
ightarrow \ell_{eta}^{\pm} W^{\mp}$  ( $lpha = e, \mu, \ eta = e, \mu, au$ )

$$\mathcal{N}(\ell_{\alpha}^{\pm}\ell_{\beta}^{\pm}) \propto \left[R(e^{\pm}e^{\pm}) + R(e^{\pm}\mu^{\pm})\right]B_{e\beta} = \frac{1}{2}B_{e\beta}$$
$$B_{\alpha\beta} = \Gamma(N_{\alpha} \to \ell_{\beta}^{\pm}W^{\mp})/\Gamma(N_{\alpha} \to \sum_{\beta}\ell_{\beta}^{\pm}W^{\mp})$$

In most of the parameter space of interest, the dependence of SSCAs on  $\theta_R$  and  $\delta_R$  is negligible.

# Some comments

- $\mathcal{A}_{ee, \mu\mu}$  depend both on  $\theta_R$  and  $\delta_R$ , while  $\mathcal{A}_{e\mu}$  depends only on  $\delta_R$ .
- We expect the relation, in the limit of  $(1 BR_y) \gg BR_y$ ,

$$\mathcal{A}_{e\mu}(\delta_R) \;=\; \mathcal{A}_{ee,\,\mu\mu}\left( heta_R=rac{\pi}{4},\delta_R+rac{\pi}{2}
ight)\,.$$

- $A_{ee, \mu\mu, e\mu}$  can be used to determine the RHN mixing angle  $\theta_R$  and CP phase  $\delta_R$  at future colliders.
- If the two-body decay dominates, the CP-induced SSCAs will be suppressed.
- If the three-body decay dominates, the TeV-scale leptogenesis efficiency will be suppressed.

# Dominant (reducible) backgrounds



Figure: From ATLAS, 1809.11105, with  $\mathcal{L} = 36.1 \, \mathrm{fb^{-1}}$ . [See also CMS, 1803.11116; Mitra, Ruiz, Scott & Spannowsky, '16; Nemevsek, Nesti & Popara, '18]

#### Production cross sections



Figure: Using a conservative k-factor of 1.1. Mitra, Ruiz, Scott & Spannowsky, '16

Even if there is no CPV in the RHN sector, we can still expect non-zero SSCAs:

$$\sigma(pp \rightarrow W_R^+) > \sigma(pp \rightarrow W_R^-)$$

# The proton PDF uncertainties are more important...



Figure: Using NNPDF3.1 and  $\theta_R = \delta_R = \pi/4$ . Left: BR<sub>y</sub> = 0 and Right: BR<sub>y</sub> = 1/2.

#### • The proton parton energy fraction

$$x_1 x_2 = rac{\hat{s}}{s} \simeq rac{M_{W_R}^2}{s} \gtrsim 0.1 \quad ext{for} \ M_{W_R} \gtrsim 5 \ ext{TeV}$$

We need a higher-energy collider!

# Prospects @ HE-LHC $\sqrt{s} = 27$ TeV



Figure: Left:  $BR_y = 0$  and Right:  $BR_y = 1/2$ .

- One could measure the RHN mixing and CPV at future high energy colliders by using the SSCA signals.
- The maximal CPV case ( $\theta_R = \delta_R = \pi/4$ ) can be measured at  $\sqrt{s} = 27$  TeV, for a  $W_R$  mass up to 7.2 TeV.
- We need only O(100 fb<sup>-1</sup>) of data to have at least 100 events of both ℓ<sup>+</sup>ℓ<sup>+</sup> and ℓ<sup>-</sup>ℓ<sup>-</sup> at HE-LHC for a W<sub>R</sub> mass of 5 TeV.

# Prospects @ FCC-hh/SPPC $\sqrt{s} = 100$ TeV



Figure: Left:  $BR_y = 0$  and Right:  $BR_y = 1/2$ .

- One could measure the RHN mixing and CPV at future high energy colliders by using the SSCA signals.
- The maximal CPV case ( $\theta_R = \delta_R = \pi/4$ ) can be measured at  $\sqrt{s} = 100$  TeV, for a  $W_R$  mass up to 26 TeV.
- We need only O(100 fb<sup>-1</sup>) of data to have at least 100 events of both ℓ<sup>+</sup>ℓ<sup>+</sup> and ℓ<sup>-</sup>ℓ<sup>-</sup> at FCC-hh/SPPC for a W<sub>R</sub> mass of 10 TeV.

# Expected SSCAs: benchmark points



- The  $\mathcal{A}_{e\mu}$  does not depend on  $\theta_R$ , thus one can use  $\mathcal{A}_{e\mu}$  to first determine the phase  $\delta_R$ , up to a twofold ambiguity.
- Then one can use  $A_{ee, \mu\mu}$  to determine the mixing angle  $\theta_R$  (and potentially remove the ambiguity of  $\delta_R$ ).
- By comparing the  $A_{ee}$  and  $A_{\mu\mu}$  data, we can get information on the BRs of 3- and 2-body decays of RHNs.

# Expected SSCAs: benchmark points



• With only  $A_{ee}$  (or  $A_{\mu\mu}$ ), one can limit  $\theta_R$  and  $\delta_R$  to a circle (band).

• Then one can use  $\mathcal{A}_{e\mu}$  to determine  $\theta_R$  and  $\delta_R$  (to a limited range).

# Casas-Ibarra parameterization

Casas & Ibarra, '01; Nemevšek, Senjanović, Tello, '12 PRL

- For simplicity, we "decouple"  $N_{\tau}$ , with one of the active neutrinos being massless.
- Casas-Ibarra parameterization of the *M<sub>D</sub>* matrix (equiv. to Nemevšek-Senjanović-Tello form in the LRSM)

$$M_D = i V_{
m PMNS} \, \widehat{m}_
u^{1/2} \mathcal{O} M_N^{1/2}$$

• The arbitrary matrix

$$\begin{split} \mathcal{O} &= \begin{pmatrix} 0 & 0\\ \cos \zeta & \sin \zeta\\ -\sin \zeta & \cos \zeta \end{pmatrix} , \quad \mathcal{O}\mathcal{O}^\mathsf{T} = \begin{pmatrix} 0 & 0\\ 0 & \mathbf{1}_{2\times 2} \end{pmatrix} \text{ for NH} , \\ \mathcal{O} &= \begin{pmatrix} \cos \zeta & \sin \zeta\\ -\sin \zeta & \cos \zeta\\ 0 & 0 \end{pmatrix} , \quad \mathcal{O}\mathcal{O}^\mathsf{T} = \begin{pmatrix} \mathbf{1}_{2\times 2} & 0\\ 0 & 0 \end{pmatrix} \text{ for IH} . \end{split}$$

•  $\zeta$  could be complex, enhancing largely the couplings  $y = M_D / v_{\rm EW}$ .

Yongchao Zhang (Wustl)

#### Leptogenesis

• The lepton asymmetry generated from RHN decay, with  $K_{\alpha}^{\rm eff}$  the washout factor [Dev, Lee & Mohapatra, '14]

$$\eta_i^{\Delta L} \simeq \frac{3}{2 z_c \mathcal{K}_{\alpha}^{\mathrm{eff}}} \sum_{\alpha} \varepsilon_{i \alpha} d_i,$$

• The dilution factor due to the right-handed gauge interactions of RHNs,

$$d_{i} = \gamma_{L\phi}^{N_{i}} / \left( \gamma_{L\phi}^{N_{i}} + \gamma_{Lqq}^{N_{i}} + \gamma_{W_{R}}^{N_{i}} \right)$$

• The flavor-dependent CP asymmetry contains the information of RHN mixing and CPV, with  $i \neq j$ ,

$$\varepsilon_{i\alpha} \simeq \frac{(M_i^2 - M_j^2) \mathrm{Im}[y_{\alpha i}^* y_{\alpha j}] \mathrm{Re}[(y^{\dagger} y)_{ij}]}{4\pi [4(M_i - M_j)^2 + \Gamma_j^2](y^{\dagger} y)_{ii}} \times \mathrm{BR}_y(N_i)$$

# Complex $\zeta$

Frerè, Hambye & Vertongen, '08; Dev, Lee & Mohapatra, '14; Dhuria, Hati, Rangarajan & Sarkar, '15

• Without any significant cancellation or fine-tuning in the  $M_D$  matrix,

$$|y|\sim \sqrt{|m_
u M_N|}\sim 10^{-6}\ll g_R$$

This sets a lower bound on the  $W_R$  boson mass

 $M_{W_R} \gtrsim 50 \, {
m TeV} \implies$  no CPV prospect @ 100 TeV collider

• The  $W_R$  mass could be significantly smaller, if

$$|\sin \zeta|, |\cos \zeta| \gg 1 \Rightarrow y \gg 10^{-6}$$

- However,  ${\rm Im}\zeta$  can not be too large
  - ▶ The  $\Delta L = 0$  processes  $L\phi \leftrightarrow L\phi$ ,  $\Delta L = 2$  process  $L\phi \leftrightarrow \bar{L}\phi^{\dagger}$  and/or the inverse decay  $L\phi \rightarrow N_i$  induce significant dilution/washout effects.
  - It is potentially constrained by high-precision low-energy constraints, such as  $\mu \rightarrow e\gamma$ ,  $0\nu\beta\beta$  and electron EDM (almost no limit in our case).

# ${ m Im}\zeta$ ranges



Ranges of parameters, with RHN mass splitting  $\varepsilon = \Gamma_{\rm avg}/2$  to have the maximal lepton asymmetry:

$$\begin{split} &\delta_{\nu} \in [0, \, 2\pi] \,, \quad \alpha \in [0, \, 2\pi] \,, \quad \zeta \in [0, \, 10] i \,, \\ &M_N \in [0.15, \, 10] \, \text{TeV} \,, \quad M_{W_R} \in [3, \, 50] \, \text{TeV} \,, \quad \theta_R \in [0, \, 2\pi] \,, \quad \delta_R \in [0, \, 2\pi] \,. \end{split}$$

The limits from LFV decay  $\mu \to e \gamma$  and electron EDM can not provide any limits in our case.

The ranges of  $\text{Im}\zeta$  we found:

$$\begin{cases} 1.3 \ \lesssim \ \mathrm{Im}\zeta \ \lesssim 7.8 \,, & \text{for NH} \,, \\ 0.8 \ \lesssim \ \mathrm{Im}\zeta \ \lesssim 7.7 \,, & \text{for NH} \,, \end{cases}$$

and the resultant magnitudes of Yukawa couplings  $y = M_D / v_{\rm EW}$ :

$$\begin{cases} 1.3 \times 10^{-6} ~\lesssim~ |y|_{\rm max} ~\lesssim~ 7.2 \times 10^{-4} \,, & \mbox{for NH} \,, \\ 1.0 \times 10^{-6} ~\lesssim~ |y|_{\rm max} ~\lesssim~ 8.6 \times 10^{-4} \,, & \mbox{for IH} \,. \end{cases}$$

#### Absolute $W_R$ mass limits



 $M_{W_R} > 9.38 (8.87) \,\mathrm{TeV}$  for NH (IH) at  $M_N \simeq 500 \,\mathrm{GeV}$ 

Leptogenesis lmits on  $W_R$  mass depend on RHN masses as well as active neutrino data and other parameters.

### Leptogenesis limits on $\theta_R \& \delta_R$



The neutrino data within their  $2\sigma$  ranges, and  $M_N = 1$  TeV  $\Delta M_N = \Gamma_{\text{avg}}/2$  to maximize the CP asymmetry.

# Testing leptogenesis @ colliders



Other methods to measure RHN CPV and test leptogenesis at colliders:

- Model-independent analysis of LNV signals  $pp \rightarrow \ell^{\pm} \ell^{\pm} j j$  [Deppisch, Harz, Hirsch, '13]
- LNV decays of right-handed doubly-charged scalar [Vasquez, '14]
- ▶ The decays  $N \rightarrow \ell^{\pm} H^{\mp}$  ( $H^{\pm}$  being charged mesons) [Caputo, Hernandez, Kekic, Lopez-Pavon & Salvado, '16]
- Heavy-light neutrino mixing at future lepton colliders [Antusch, Cazzato, Drewes, Fischer, Garbrecht, Gueter, Klaric, '17]

# Conclusion

- The mixing and CP violation in the RHN sector of TeV-scale left-right models can be directly probed at future high-energy hadron colliders, by measuring the same-sign charge asymmetries (SSCAs).
- In the case with only  $N_{e, \mu}$ , the  $e^{\pm}\mu^{\pm}$  channel can be used to measure the CP phase  $\delta_R$ , which is independent of the RHN mixing angle; using the channels  $e^{\pm}e^{\pm}$ ,  $\mu^{\pm}\mu^{\pm}$ , one can then determine the mixing angle  $\theta_R$ .
- The future 100 (27) TeV collider could probe the RHN mixing and CPV, for  $W_R$  mass up to 26 (7.2) TeV.
- TeV-scale resonant leptogenesis can be directly tested at future hadron colliders by measuring the SSCAs.
- There is an absolute lower bound around 9 TeV on the  $W_R$  boson mass to make leptogenesis work in the case with effectively only two RHNs.

# Thank you very much!

backup slides

• In the large  $M_N$  limit, the dependence is respectively (for the 2-body decays we have taken into account also the dependence  $M_D \propto M_N^{1/2}$ )

$$\Gamma(N o \ell q ar q') \propto M_N^5/M_{W_R}^4\,, \quad \Gamma(N o L \phi) \propto M_N^2\,.$$

When  $M_N$  gets larger, the 3-body width grows faster than the 2-body decays, therefore the  $W_R$  mass has to be larger to make leptogenesis work.

• When RHN masses get smaller  $\downarrow$  ( $\lesssim$  500 GeV),

$$K_{\text{eff}}\uparrow, d_i\downarrow, \varepsilon_{i\alpha}\uparrow \Rightarrow M_{W_R} \text{ limits }\uparrow$$