

# Lepton flavor violation induced by neutral and doubly-charged scalars at future lepton colliders

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#### based on

P. S. B. Dev, R. N. Mohapatra & YCZ, PRL120(2018)221804 [1711.08430]

P. S. B. Dev, R. N. Mohapatra & YCZ, 1803.11167, accepted by PRD

contributing to CEPC CDR & CLIC CERN Yellow Book

#### Outline

- Motivations of the LFV processes
- Beyond SM neutral scalar H at future lepton colliders
  - On-shell production
  - Off-shell production
  - Prospects at ILC and CEPC (CLIC in backup slides)
- Doubly-charged scalar  $H^{\pm\pm}$  at future lepton colliders
  - On-shell production through the (LFV) Yukawa couplings
  - Off-shell production
  - Prospects at ILC and CEPC (CLIC in backup slides)
- Conclusion

#### Why lepton-flavor violation (LFV) at future lepton colliders?

- "Smoking-gun" signal beyond the SM;
- Clean SM background at lepton colliders
- ...Connection to neutrino mass generation (and other pheno)
  - Beyond SM neutral scalar H from e.g. left-right model, sneutrino in RPV SUSY models;
  - ▶ Doubly-charged scalar H<sup>±±</sup> in type-II seesaw and its extensions like left-right model;
  - ▶ Might also be connected to the heavy neutrino searches, effective 4-fermion interactions, or even DM pheno at future lepton colliders.

# Beyond SM neutral scalar *H*@ future lepton colliders

# Well-motivated underlying models

• RPV SUSY: sneutrinos ( $\tilde{\nu}$ ) [Aulakh, Mohapatra '82; Hall,Suzuki '84; Ross, Valle '85, Barbier+ '04; Duggan, Evans, Hirschauer '13]

$$\mathcal{L}_{\mathrm{RPV}} = \frac{1}{2} \lambda_{\alpha\beta\gamma} \widehat{\mathcal{L}}_{\alpha} \widehat{\mathcal{L}}_{\beta} \widehat{\mathcal{E}}_{\gamma}^{c}$$

• Left-right symmetric models: the  $SU(2)_R$ -breaking scalar  $H_3$  [Dev, Mohapatra, YCZ '16; '16; '17; Maiezza, Senjanović, Vasquez '16]

LFV couplings are generated at tree and loop level

• 2HDM: CP-even or odd (heavy) scalars from the 2nd doublet [Branco+ '11; Crivellin, Heeck, Stoffer '15]

LFV couplings are induced from small deviation from the lepton-specific structure.

• Mirror models: singlet scalar connecting the SM leptons to heavy mirror leptons [Hung '06, '07; Bu, Liao, Liu '08; Chang, Chang, Nugroho+ '16; Hung, Le, Tran+ '17]

LFV couplings arise from the SM-heavy lepton mixing

# Beyond SM neutral Higgs & effective LFV couplings

Model-independent effective LFV couplings of H

$$\mathcal{L}_{Y} = h_{\alpha\beta}\bar{\ell}_{\alpha,L}H\ell_{\beta,R} + \text{H.c.}.$$

For simplicity, we assume  $h_{\alpha\beta}$  are real, symmetric, H is CP-even, hadrophobic and the mixing with the SM Higgs h is small.

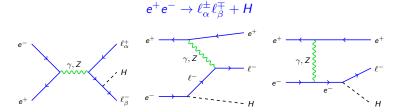
H might originate from a isospin singlet, doublet or triplet, depending on specific underlying models.

• Effective Dim-4 couplings  $\neq$  Effective 4-fermion couplings like  $\frac{1}{\Lambda^2}(\bar{e}e)(\bar{e}\mu)$  [Kabachenko, Pirogov '97; Ferreira, Guedes, Santos '06; Aranda, Flores-Tlalpa, Ramirez-Zavaleta+ '09; Murakami, Tait '14; Cho, Shimo '14]

$$m_H < \sqrt{s} \Rightarrow$$
 on-shell production

# On-shell production of H at lepton colliders

• the  $e^+e^-$  process



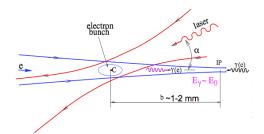
involving the charged-currents [H decaying into visible particles]

$$e^+e^- \rightarrow \nu_{\alpha}\bar{\nu}_e + H$$
 $e^+ \qquad \qquad \bar{\nu}_e$ 
 $\ell^- \qquad \qquad \ell^-$ 

# Laser photon in future lepton colliders

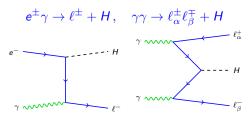
- In future lepton colliders, high luminosity photon beams can be obtained by Compton backscattering of low energy, high intensity laser beam off the high energy electron beam [Ginzburg+ '83, '84].
- The effective photon luminosity distribution  $(x = \omega/E_e \lesssim 0.83 \text{ the fraction of electron energy carried away by the scattered photon,}$   $\xi = 4\omega_0 E_e/m_e^2)$

$$f_{\gamma/e}(x) = \frac{1}{D(\xi)} \left[ (1-x) + \frac{1}{(1-x)} - \frac{4x}{\xi(1-x)} + \frac{4x^2}{\xi^2(1-x)^2} \right],$$
with  $D(\xi) = \left( 1 - \frac{4}{\xi} - \frac{8}{\xi^2} \right) \log(1+\xi) + \frac{1}{2} + \frac{8}{\xi} - \frac{1}{2(1+\xi)^2},$ 



# On-shell production of H at lepton colliders

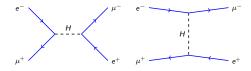
• involving the laser photon(s)



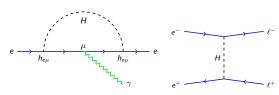
# Constraints on the LFV couplings: on-shell

On-shell production amplitudes depend *linearly* on the LFV couplings

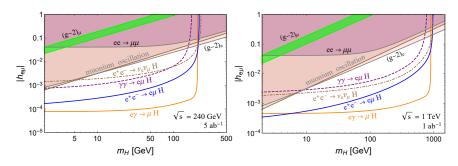
• muonium anti-muonium oscillation:  $(\bar{\mu}e) \leftrightarrow (\mu\bar{e})$   $(h_{e\mu})$  [Clark, Love '03]



- Electron and muon g-2 ( $h_{e\ell}$ ,  $h_{\mu\ell}$ ) [Lindner, Platscher, Queiroz '16]
- Bhabha scattering, LEP  $ee \rightarrow \ell\ell$  data ( $h_{e\ell}$ ) [OPAL '03; L3 '03; DELPHI '05]



### Prospects of *H*: on-shell production

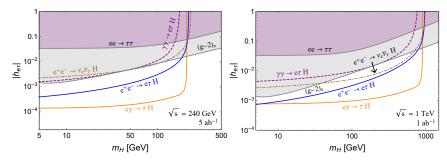


 $\gamma\gamma$  (e\gamma) channel: laser photon collision.

Green bands: muon g-2 anomaly (excluded).

Assuming the dominant decay mode  $H o e^{\pm} \mu^{\mp}$ .

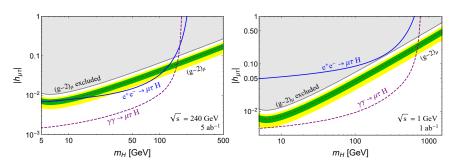
## Prospects of *H*: on-shell production



 $\gamma\gamma$  ( $e\gamma$ ) channel: laser photon collision.

Assuming the dominant decay mode  $H o e^\pm au^\mp$ .

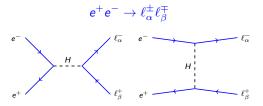
## Prospects of *H*: on-shell production



- $\gamma\gamma$  ( $e\gamma$ ) channel: laser photon collision.
- Assuming the dominant decay mode  $H \to \mu^{\pm} \tau^{\mp}$ .
- ▶ The muon g-2 discrepancy can be directly tested at CEPC & ILC via the searches  $e^+e^-, \gamma\gamma \to \mu\tau + H$ .

## Off-shell production of H at lepton colliders

• Off-shell production (at resonance when  $m_H \simeq \sqrt{s}$ ) might also be mediated by a (light) gauge boson Z' with LFV couplings [Heeck '16]



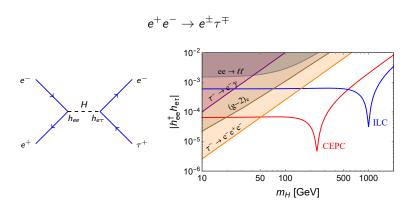
# Constraints on the LFV couplings: off-shell

Off-shell production amplitudes depend *quadratically* on the LFV couplings

process	current data	constraints $[GeV^{-2}]$
$\mu^-  ightarrow e^- e^+ e^-$	$< 10^{-12}$	$ h_{ m ee}^{\dagger}h_{ m e\mu} /m_H^2 < 6.6  imes 10^{-11}$
$ au^-  ightarrow e^- e^+ e^-$	$< 2.7 \times 10^{-8}$	$ h_{ee}^{\dagger}h_{e\tau} /m_H^2 < 2.6 \times 10^{-8}$
$ au^-  ightarrow \mu^- e^+ e^-$	$< 1.8  imes 10^{-8}$	$  h_{ee}^{\dagger}h_{\mu au} /m_H^2 < 1.5  imes 10^{-8}$
$ au^-  ightarrow \mu^+ e^- e^-$	$<1.5 imes10^{-8}$	$  h_{e\mu}^{\dagger}h_{e\tau} /m_H^2 < 1.9  imes 10^{-8}$
$ au^-  ightarrow { m e}^- \gamma$	$< 3.3 \times 10^{-8}$	$  h_{ee}^{\dagger}h_{e\tau} /m_H^2 < 1.0 \times 10^{-6}$
$\tau^- \to \mu^- \gamma$	$< 4.4 \times 10^{-8}$	$  h_{e\mu}^{\dagger}h_{e\tau} /m_H^2 < 1.2  imes 10^{-6}$
$(g-2)_{e}$	$< 5.0 \times 10^{-13}$	$ h_{ee}^{\dagger}h_{e au} /m_H^2 < 1.1  imes 10^{-7}$
		$  \   h_{e\mu}^\dagger h_{e au}   / m_H^2 < 1.0  imes 10^{-8}$
ee  ightarrow ee,  au au	$\Lambda > 5.7 \& 6.3 \text{ TeV}$	$h_{ee}^{\dagger} h_{e au}  /m_H^2 < 1.4  imes 10^{-7}$
ee $\rightarrow \mu\mu,   au au$	$\Lambda > 5.7 \& 7.9 \text{ TeV}$	$  h_{e\mu}^{\dagger}h_{e\tau} /m_H^2 < 1.3 \times 10^{-7}$
		<u> </u>

The  $\mu \to 3e$  limit is so strong that the it leaves no hope to see any signal in the  $ee \to e\mu$  channel at future lepton colliders.

# Prospects of *H*: off-shell production



- ▶ Resonance effect at  $m_H \simeq \sqrt{s}$  with width  $\Gamma_H = 10$  (30) GeV at CEPC (ILC).
- ▶ The off-shell scalar could be probed well beyond 10 TeV scale for couplings  $h_{\alpha\beta}$  of order one.

# Prospects of *H*: off-shell production

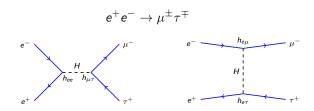
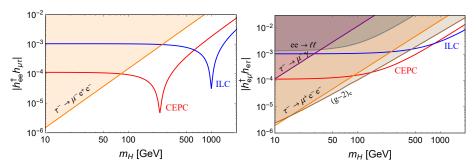


Figure: The s and t channels depend on different  $h^{\dagger}h$  couplings.



# Doubly-charged scalar $H^{\pm\pm}$ @ future lepton colliders

# $H^{\pm\pm}$ at lepton (and hadron) colliders

- The (left- and right-handed)  $H^{\pm\pm}$  can be pair produced from the gauge interactions to the  $\gamma/Z$  bosons.
- The Drell-Yan production channels can not be used to measure *directly* the (LFV) Yukawa couplings  $f_{\alpha\beta}$  of  $H^{\pm\pm}$  to charged leptons, unless  $H^{\pm\pm}$  is long-lived.
- The current LHC same-sign dilepton limits depend largely on the branching fractions  $\mathrm{BR}(H^{\pm\pm}\to\ell_\alpha^\pm\ell_\beta^\pm)$ .

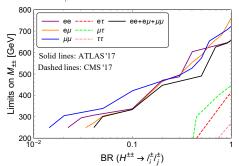


Figure: LHC dilepton limits on the right-handed  $H^{\pm\pm}$ .

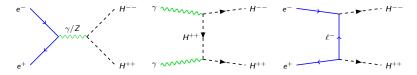
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# On-shell Production of $H^{\pm\pm}$ at lepton colliders through the (LFV) Yukawa couplings $f_{\alpha\beta}$

Model-independent effective couplings of (right-handed)  $H^{\pm\pm}$ 

$$\mathcal{L}_{Y} = f_{\alpha\beta}H^{++}\overline{\ell_{\alpha}^{C}}\ell_{\beta} + \text{H.c.}$$

 Pair production through the gauge and Yukawa couplings [Chakrabarti+, hep-ph/9804297]

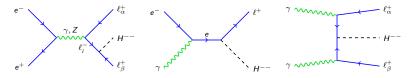


The Drell-Yan processes dominate the pair production if the Yukawa couplings  $f_{e\ell}$  are very small.

# On/off-shell production of $H^{\pm\pm}$ at lepton colliders

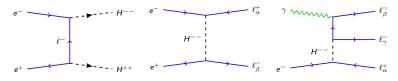
#### • Single production through the Yukawa couplings

[Kuze & Sirois, hep-ex/0211048; Barenboim, Huitu, Maalampi & Raidal, hep-ph/9611362; Lusignoli & Petrarca, PLB**226**, 397; Yue & Zhao, hep-ph/0701017; Godfrey, Kalyniak, Romanenko, hep-ph/0108258; hep-ph/0207240; Rizzo, PRD**25**, 1355; Yue, Zhao & Ma, 0706.0232]

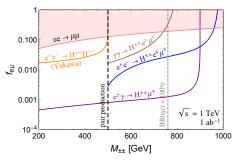


#### Off-shell production

[Godfrey, Kalyniak, Romanenko, hep-ph/0108258; hep-ph/0207240; Rizzo, PRD25, 1355



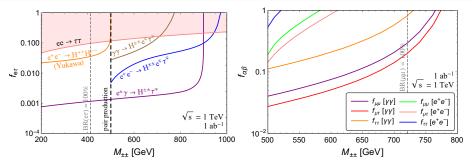
# Prospects of $H^{\pm\pm}$ @ ILC 1TeV: single production



- Assuming the dominant decay mode  $H^{\pm\pm} \rightarrow e^{\pm}\mu^{\pm}$ .
- ▶ Below  $\sqrt{s}/2 \simeq 500$  GeV, the process  $e^+e^- \to H^{\pm\pm}\ell_\alpha^\mp\ell_\beta^\mp$  is dominated by the Drell-Yan pair production  $e^+e^- \to H^{++}H^{--}$  with the subsequent decay  $H^{\mp\mp} \to \ell_\alpha^\mp\ell_\beta^\mp$ .
- ▶ The electron and muon g-2 limits are highly suppressed by the charge lepton masses and are not shown in the plot.

CLIC could probe higher mass ranges.

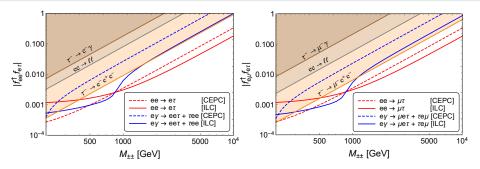
# Prospects of $H^{\pm\pm}$ @ ILC 1TeV: single production



- Assuming the dominant decay mode  $H^{\pm\pm} o e^\pm au^\pm$  (left),  $\ell^\pm_lpha\ell^\pm_eta$  (right).
- ▶ Below  $\sqrt{s}/2 \simeq 500$  GeV, the process  $e^+e^- \to H^{\pm\pm}\ell_\alpha^\mp\ell_\beta^\mp$  is dominated by the Drell-Yan pair production  $e^+e^- \to H^{++}H^{--}$  with the subsequent decay  $H^{\mp\mp} \to \ell_\alpha^\mp\ell_\beta^\mp$ .
- ▶ The electron and muon g-2 limits are highly suppressed by the charge lepton masses and are not shown in the plots.

CLIC could probe higher mass ranges.

# Prospects of $H^{\pm\pm}$ @ CEPC & ILC: off-shell production



- Suppressed by the three-body phase space, the sensitivities in the  $e\gamma$  processes are comparatively much weaker.
- As in the neutral scalar case, the limit from  $\mu \to eee$  are so stringent that it has precluded the  $H^{\pm\pm}$ -mediated signal  $ee \to e\mu$  at CEPC & ILC.
- ► The effective cutoff scale  $\Lambda \simeq M_{\pm\pm}/|f|$  can be probed at CEPC & ILC 1TeV up to few 10 TeV (even higher at CLIC).
- ▶ The sensitivities for more flavor combinations  $\alpha$ ,  $\beta$ ,  $\gamma$  in  $e^{\pm}\gamma \to \ell_{\alpha}^{\mp}\ell_{\beta}^{\pm}\ell_{\gamma}^{\pm}$  can be found in our paper 1803.11167.

#### Conclusion

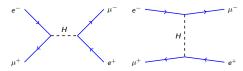
- A large variety of well-motivated models accommodate a beyond SM neutral scalar H and/or doubly-charged scalar  $H^{\pm\pm}$ , with LFV couplings to the SM charged leptons.
- These LFV couplings can be studied in a *model-independent* way at future lepton colliders, which strengthens the physics case for future lepton colliders.
- The neutral scalar H can be produced on-shell via  $e^{\pm}\gamma \to \ell^{\pm} + H$  and  $e^{+}e^{-}, \gamma\gamma \to \ell^{\pm}_{\alpha}\ell^{\mp}_{\beta} + H$  or off-shell via  $e^{+}e^{-} \to \ell^{\pm}_{\alpha}\ell^{\mp}_{\beta}$ .
- The doubly-charged scalar  $H^{\pm\pm}$  can be (doubly & singly) on-shell and off-shell produced from the (LFV) Yukawa couplings to the charged leptons.
- It is promising that future lepton colliders could probe a broad region of mass and coupling parameters for both H and  $H^{\pm\pm}$ , which go well beyond the existing low-energy LFV constraints like au o eee.
- The neutral scalar explanation of the muon g-2 anomaly can be directly tested at future lepton colliders in the  $e^+e^-, \gamma\gamma \to \mu^\pm\tau^\mp + H$  processes.

## Thank you for your attention!



On-shell production amplitudes depend *linearly* on the LFV couplings

• muonium anti-muonium oscillation:  $(\bar{\mu}e) \leftrightarrow (\mu\bar{e}) \ (h_{e\mu})$ 



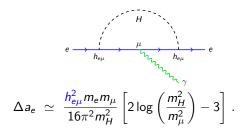
Oscillation probablity [Clark, Love '03]

$$\mathcal{P} = \frac{2(\Delta M)^2}{\Gamma_{\mu}^2 + 4(\Delta M)^2}$$

with the H-induced mass splitting

$$\Delta M = \frac{2\alpha_{\rm EM}^3 h_{\rm e\mu}^2 \mu^3}{\pi m_H^2}, \quad \mu = \frac{m_{\rm e} m_{\mu}}{m_{\rm e} + m_{\mu}}$$

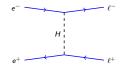
• Electron and muon g-2 ( $h_{e\ell}$ ,  $h_{\mu\ell}$ ) [Lindner, Platscher, Queiroz '16]



The value of  $h_{e\mu}$  to explain  $(g-2)_{\mu}$  discrepancy is excluded by the  $(g-2)_{e}$  constraint.

$$\Delta a_{\mu} \equiv \Delta a_{\mu}^{\mathrm{exp}} - \Delta a_{\mu}^{\mathrm{th}} = (2.87 \pm 0.80) imes 10^{-9}$$

• Bhabha scattering, LEP  $ee \rightarrow \ell\ell$  data  $(h_{e\ell})$  [OPAL '03; L3 '03; DELPHI '05]



Effective 4-fermion interaction

$$\frac{h_{e\ell}^2}{m_H^2}(\bar{e}\ell)(\bar{e}\ell) \xrightarrow{\text{Fierz transf.}} \frac{1}{\Lambda^2}(\bar{e}\gamma_\mu e)(\bar{\ell}\gamma^\mu \ell)$$

If  $m_H \lesssim \sqrt{s}$ , the LEP limits on the cut-off scale  $\Lambda$  do not apply, and we have to consider the kinetic dependence

$$rac{1}{m_H^2} o rac{1}{q^2 - m_H^2} \simeq rac{1}{-s\cos\theta/2 - m_H^2}$$

Off-shell production amplitudes depend quadratically on the LFV couplings

• 3-body LFV decays of muon and tauon, e.g. [Sher, Yuan '91]

$$\Gamma( au^- 
ightarrow e^+ e^- e^-) \simeq rac{1}{\delta} rac{|h_{
m ee}^\dagger h_{e au}|^2 m_ au^5}{3072 \pi^3 m_H^4} \,, \quad (\delta=2)$$

• 2-body LFV decays of muon and tauon, e.g. [Harnik, Kopp, Zupan '12]

$$\Gamma( au o e\gamma) = rac{lpha_{
m EM} m_ au^5}{64\pi^4} \left( |c_L|^2 + |c_R|^2 
ight) \,, \quad c_L = c_R \simeq rac{h_{
m ee}^\dagger h_{
m e au}}{24 m_H^2} \,.$$

•  $h_{ee,\,e\mu,\,e au}$  contribute to  $(g-2)_e$  & LEP  $ee \to \ell\ell$  data, [DELPHI '05; Hou, Wong '95]

$$\begin{array}{ll} |h_{ee}^{\dagger}h_{e\tau}| & \Rightarrow & ee \rightarrow e\tau \\ |h_{e\mu}^{\dagger}h_{e\tau}| & \Rightarrow & ee \rightarrow \mu\tau \text{ ($t$-channel)} \end{array}$$

# SM backgrounds for on-shell production of H

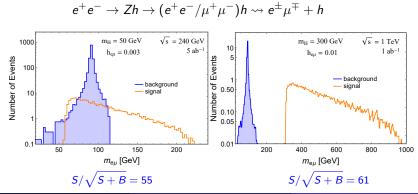
Main SM backgronds are particle misidentification for

$$e^+e^- \to \ell_{\alpha}^+\ell_{\beta}^- + X$$
,  $(\alpha \neq \beta)$ 

The mis-identification rate is expected to be small, of order  $10^{-3}$ 

[Milstene, Fisk, Para '06; Hammad, Khalil, Un '16; Yu, Ruan, Boudry+ '17]

#### Examle:



# SM backgrounds for off-shell production of H

Main SM backgrounds:

$$e^+e^- o W^+W^- o \ell_{\alpha}^+\ell_{\beta}^- 
u \bar{
u}$$

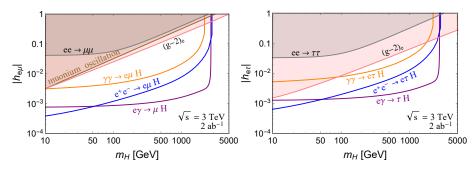
The backgrounds can be well controlled by

[Kabachenko, Pirogov '97; Cho, Shimo '16; Bian, Shu, YCZ '15]

requiring that the constructed energy  $E_\ell \simeq \sqrt{s}/2\,,$  kinetic distribution analysis of the backgrounds and signals

# CLIC prospects of H and $H^{\pm\pm}$

## CLIC prospects of *H*: on-shell production

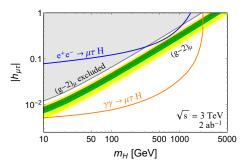


 $\gamma\gamma$  ( $e\gamma$ ) channel: laser photon collision.

Shaded regions are excluded.

Assuming the dominant decay mode  $H o e^\pm \mu^\mp$  (left),  $\mathrm{e}^\pm \tau^\mp$  (right).

### CLIC prospects of *H*: on-shell production



 $\gamma\gamma$  ( $e\gamma$ ) channel: laser photon collision.

Shaded regions are excluded.

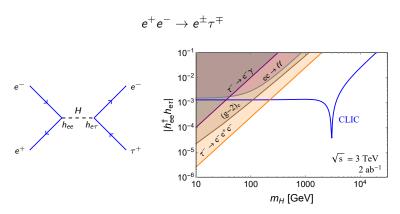
Assuming the dominant decay mode  $H \to \mu^{\pm} \tau^{\mp}$ .

Dotted brown line: central values of muon g-2 anomaly, green and yellow bands: the  $1\sigma$  and  $2\sigma$  regions.

The muon g-2 discrepancy can be directly tested at CLIC via the searches of  $\gamma\gamma \to \mu\tau + H$ .

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### CLIC prospects of *H*: off-shell production



Resonance effect at  $m_H \simeq \sqrt{s}$  with width  $\Gamma_H = 30$  GeV

The off-shell scalar could be probed well beyond 10 TeV scale (or even up to 100 TeV).

# CLIC prospects of *H*: off-shell production

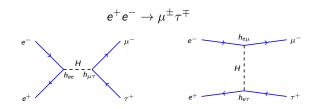
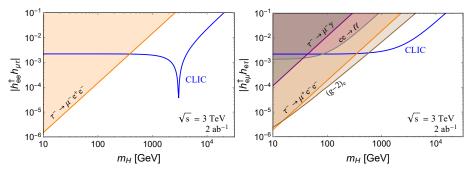
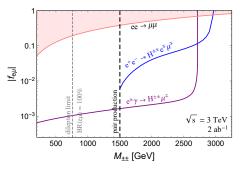


Figure: The s and t channels depend on different  $h^{\dagger}h$  couplings.



# CLIC prospects of $H^{\pm\pm}$ : single production



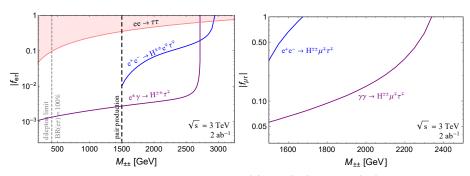
Assuming the dominant decay mode  $H^{\pm\pm} 
ightarrow e^\pm \mu^\pm.$ 

Below  $\sqrt{s}/2=1.5$  TeV, the process  $e^+e^- \to H^{\pm\pm}\ell_{\alpha}^{\mp}\ell_{\beta}^{\mp}$  is dominated by the Drell-Yan pair production  $e^+e^- \to H^{++}H^{--}$  with the subsequent decay  $H^{\mp\mp} \to \ell_{\alpha}^{\mp}\ell_{\beta}^{\mp}$ .

The  $\gamma\gamma \to H^{\pm\pm}\ell^\mp_\alpha\ell^\mp_\beta$  sensitivity is weaker than the  $e^+e^-$  process.

The electron and muon g-2 limits are highly suppressed by the charge lepton masses and are not shown in the plot.

# CLIC prospects of $H^{\pm\pm}$ : single production



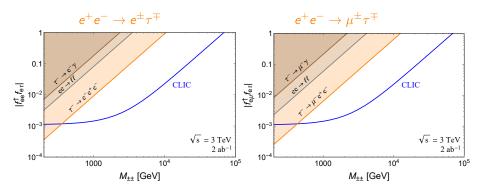
Assuming the dominant decay mode  $H^{\pm\pm} o e^\pm au^\pm$  (left),  $\mu^\pm au^\pm$  (right).

Below  $\sqrt{s}/2=1.5$  TeV, the process  $e^+e^- \to H^{\pm\pm}\ell_{\alpha}^{\mp}\ell_{\beta}^{\mp}$  is dominated by the Drell-Yan pair production  $e^+e^- \to H^{++}H^{--}$  with the subsequent decay  $H^{\mp\mp} \to \ell_{\alpha}^{\mp}\ell_{\beta}^{\mp}$ .

The  $\gamma\gamma \to H^{\pm\pm}\ell^\mp_\alpha\ell^\mp_\beta$  sensitivity is weaker than the  $e^+e^-$  process.

The electron and muon g-2 limits are highly suppressed by the charge lepton masses and are not shown in the plots.

# CLIC prospects of $H^{\pm\pm}$ : off-shell production



Suppressed by the three-body phase space, the sensitivities in the  $e\gamma$  processes are comparatively much weaker.

As in the neutral scalar case, the limit from  $\mu \to eee$  are so stringent that it has precluded the  $H^{\pm\pm}$ -mediated signal  $ee \to e\mu$  at CLIC.

The effective cutoff scale  $\Lambda \simeq M_{\pm\pm}/|f|$  can be probed at CLIC up to few 10 TeV.