

# A Combined Astrophysical and Dark Matter Interpretation of the IceCube HESE and Throughgoing Muon Events

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Washington University in St. Louis

Y. S, B. Dev, arXiv:1804.04919 [hep-ph]

Pheno2018  
University of Pittsburgh  
May 8, 2018



# Outline

- Introduction and Motivation
- 2 Comp Astro Flux
- DM + 1 Comp Astro Flux
- Gamma-Ray Constraint
- Conclusion



# Introduction of Neutrino Flux



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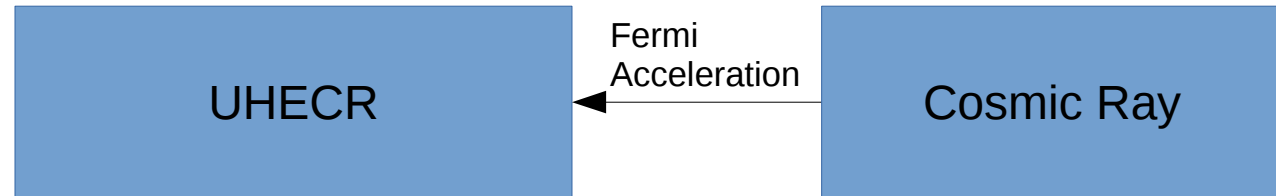


Cosmic Ray

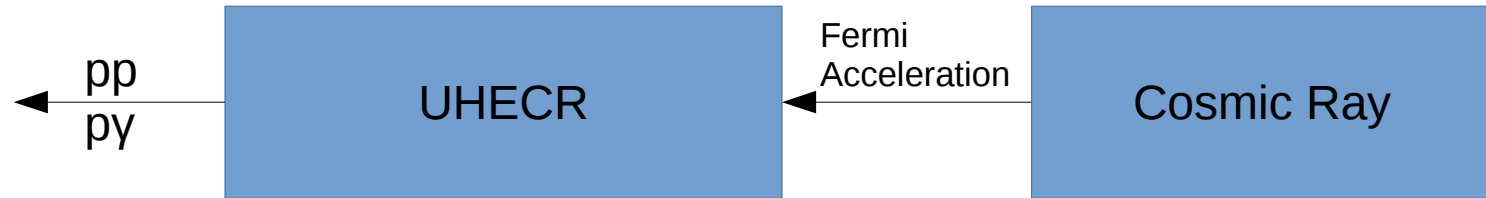
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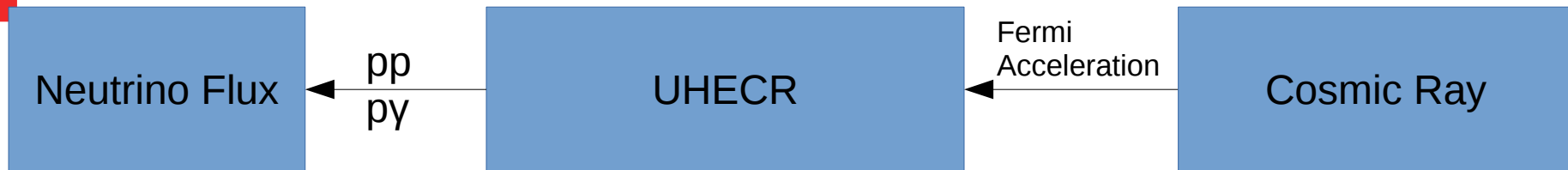
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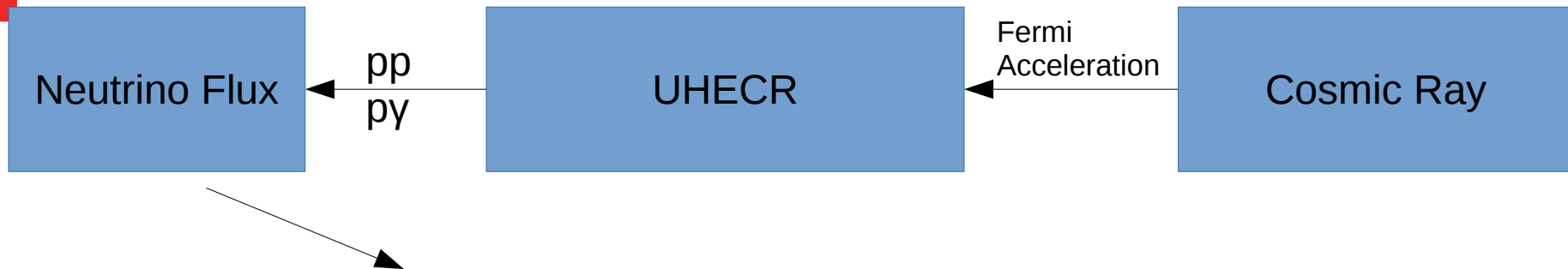


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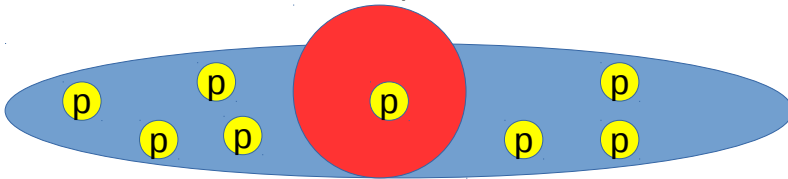


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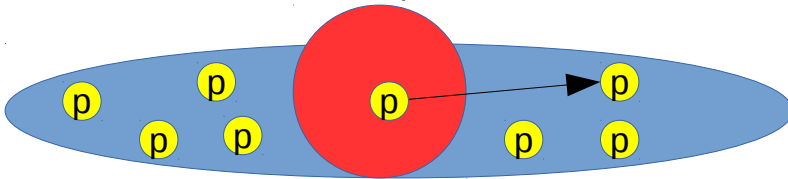


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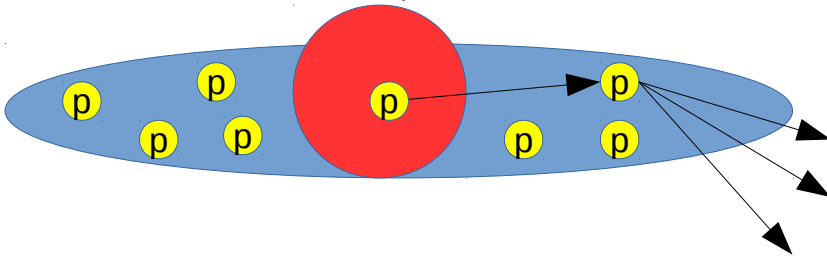


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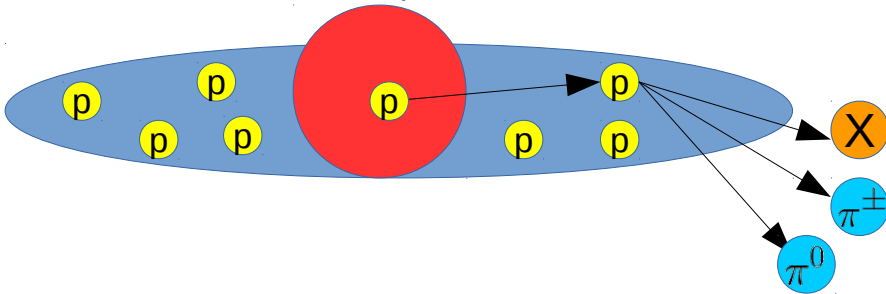


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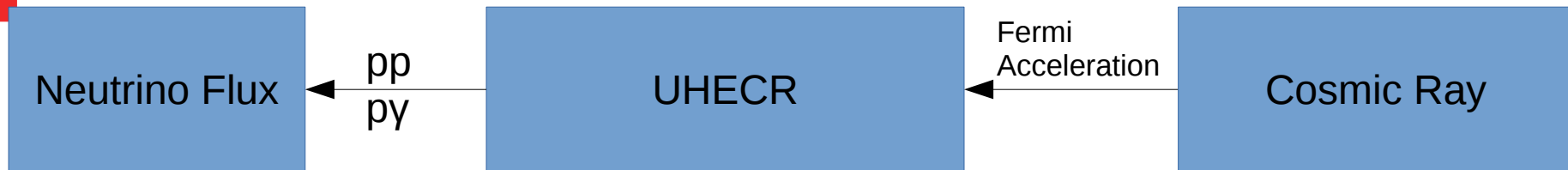
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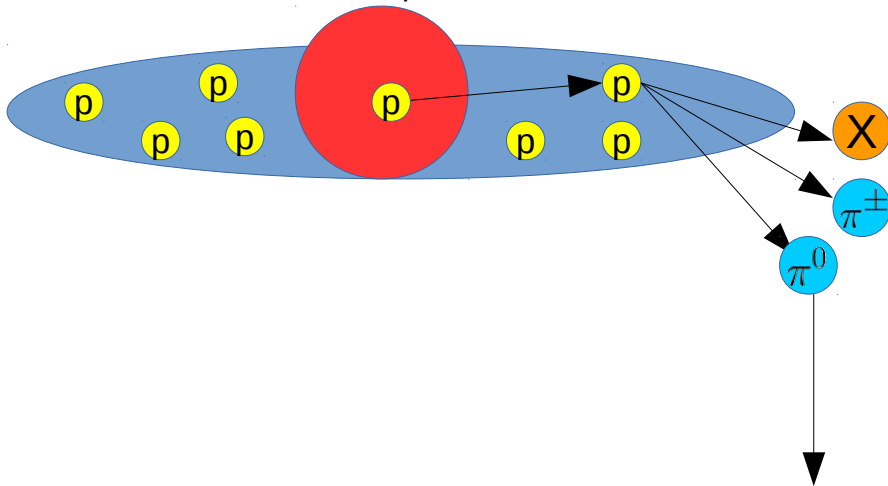


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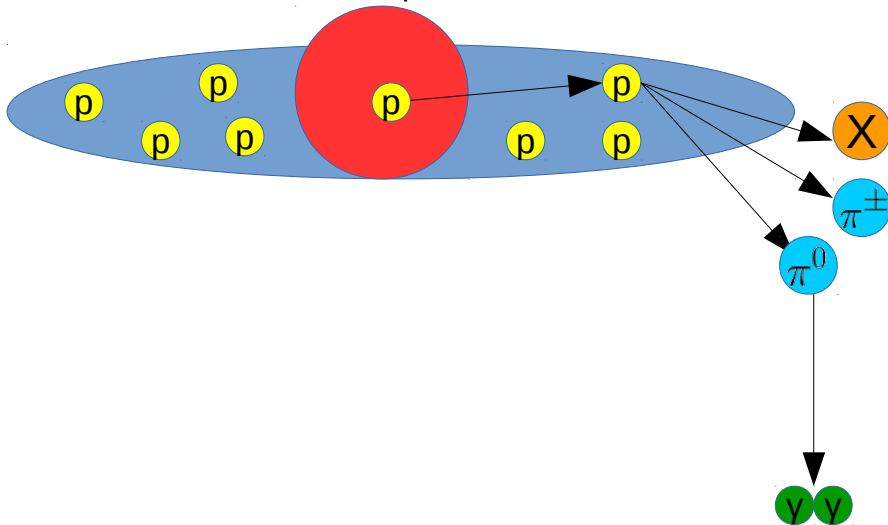


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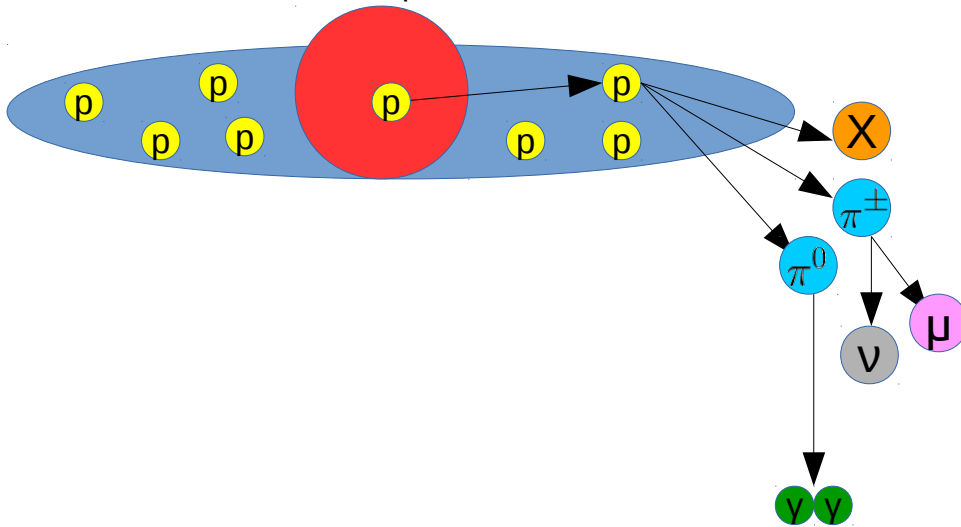


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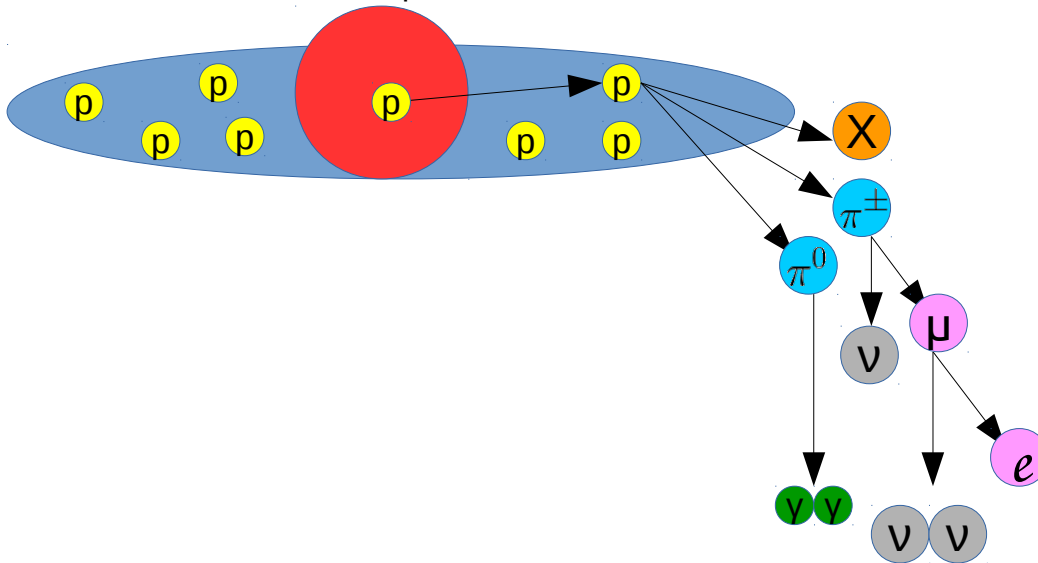


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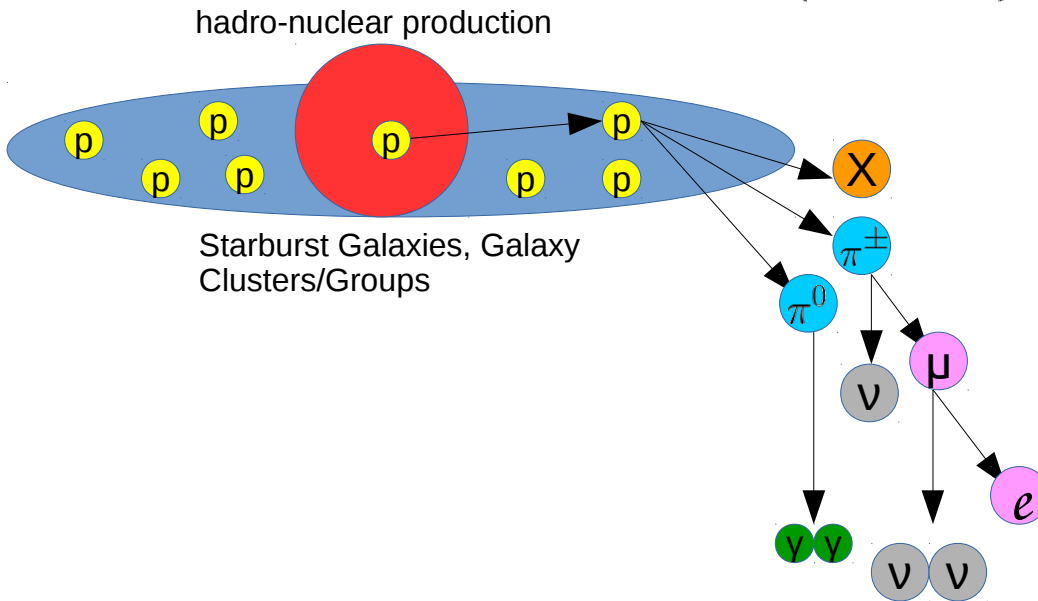
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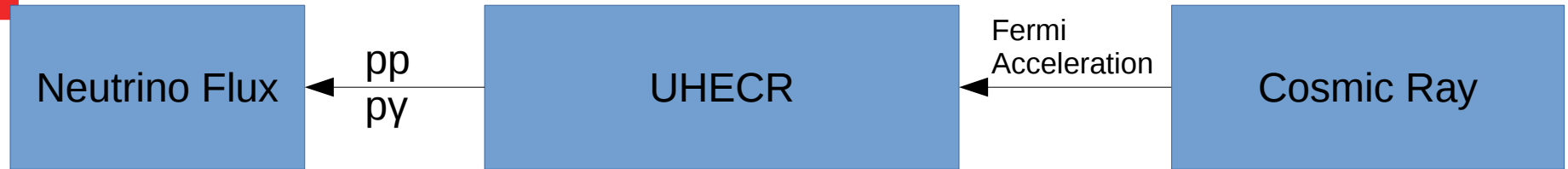
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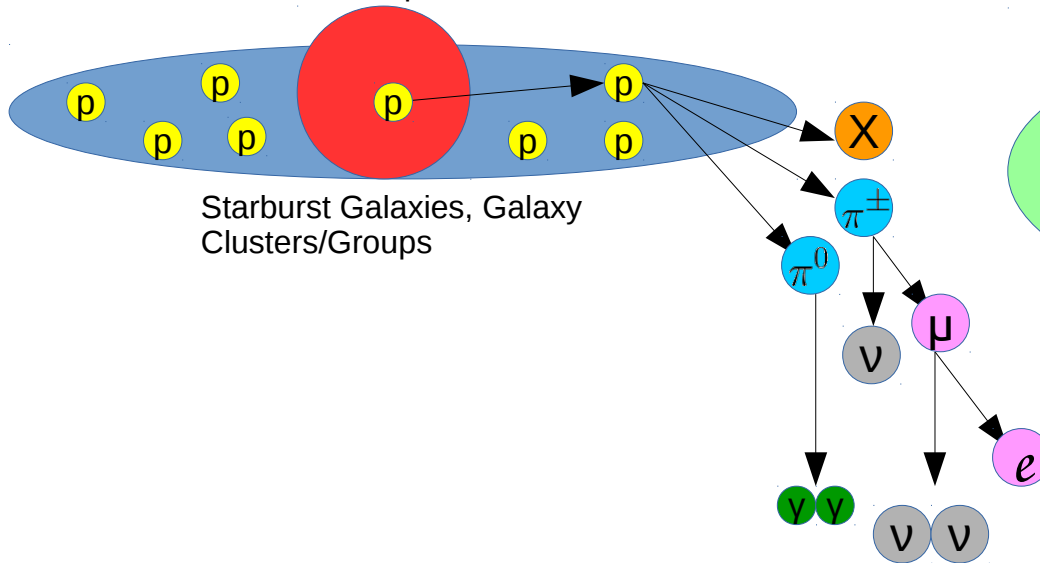
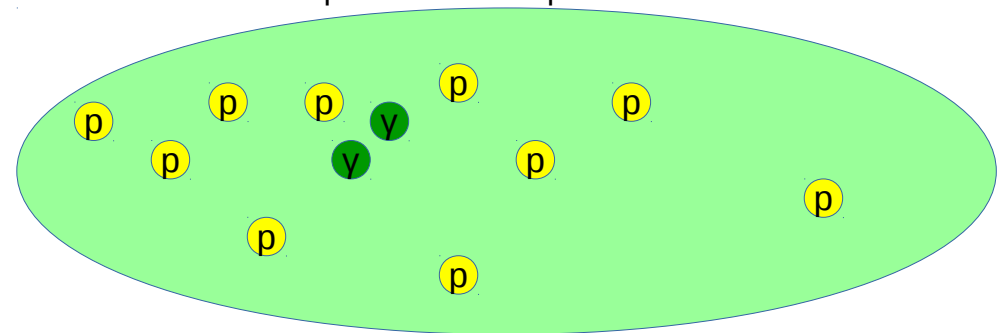
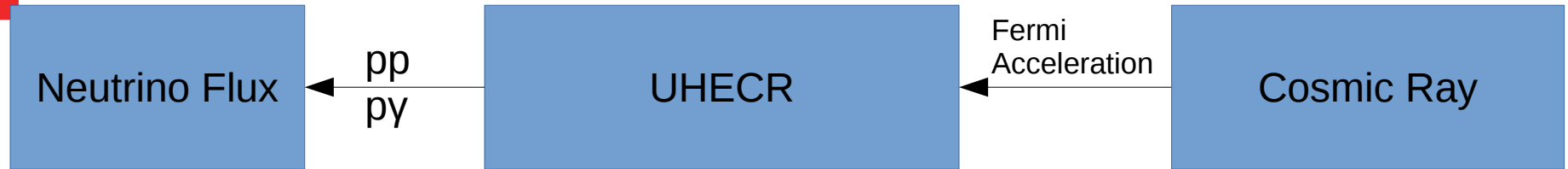


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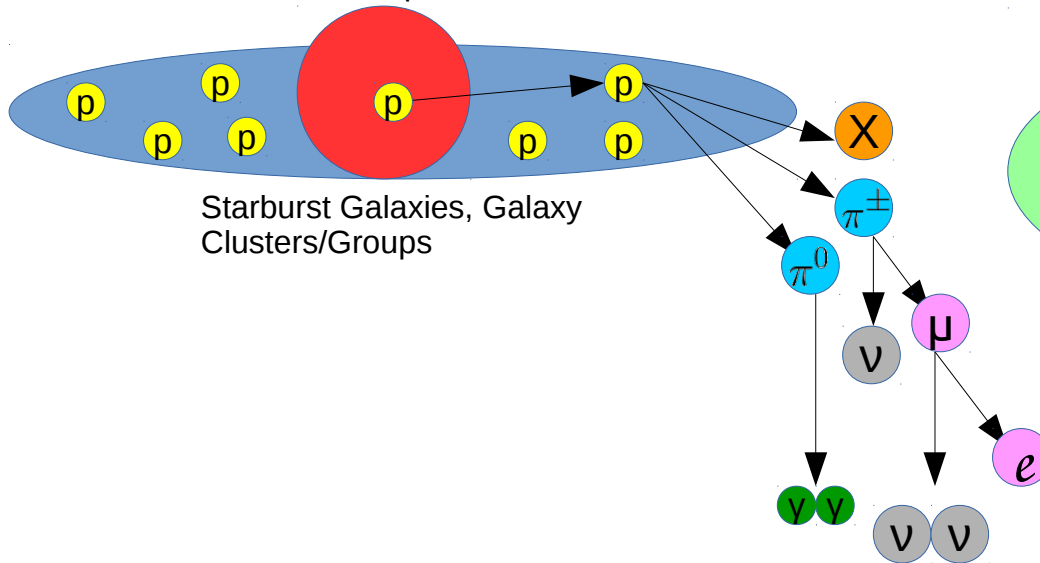
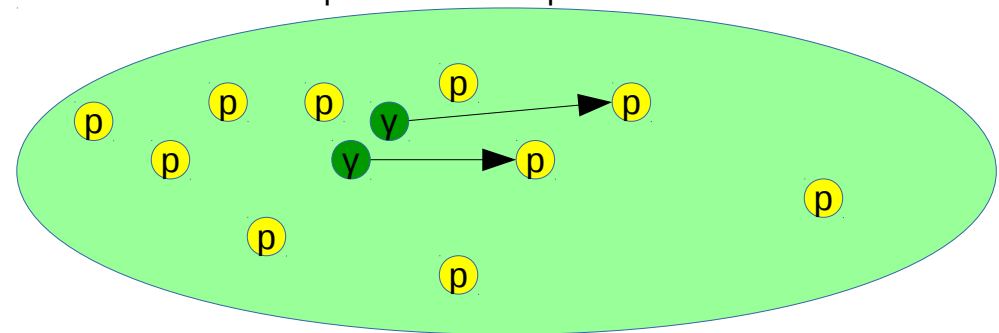


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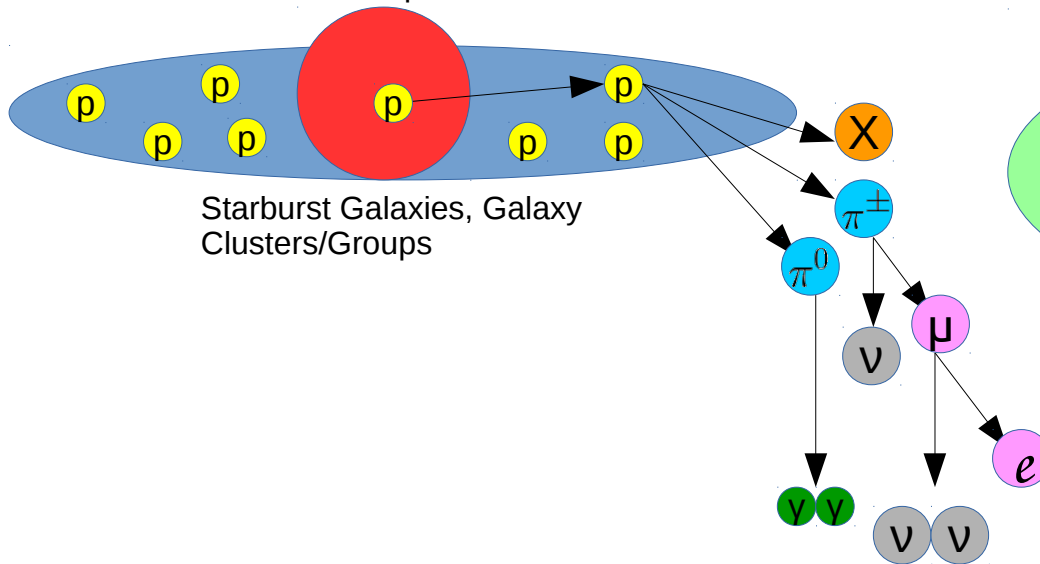
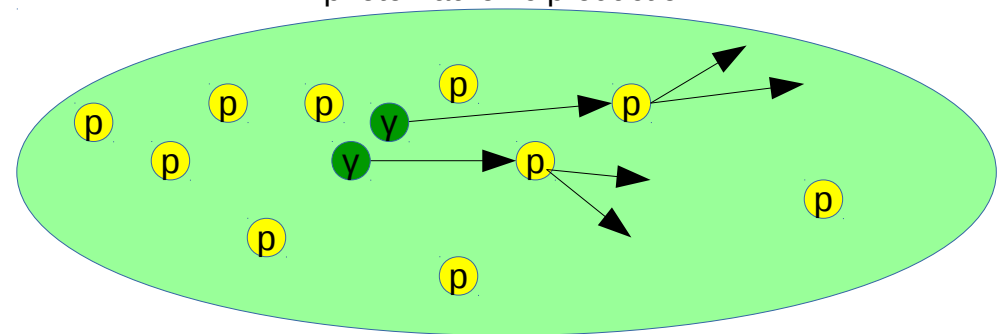
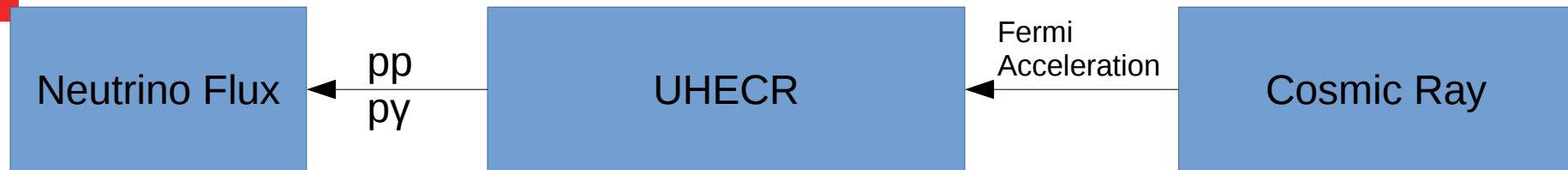


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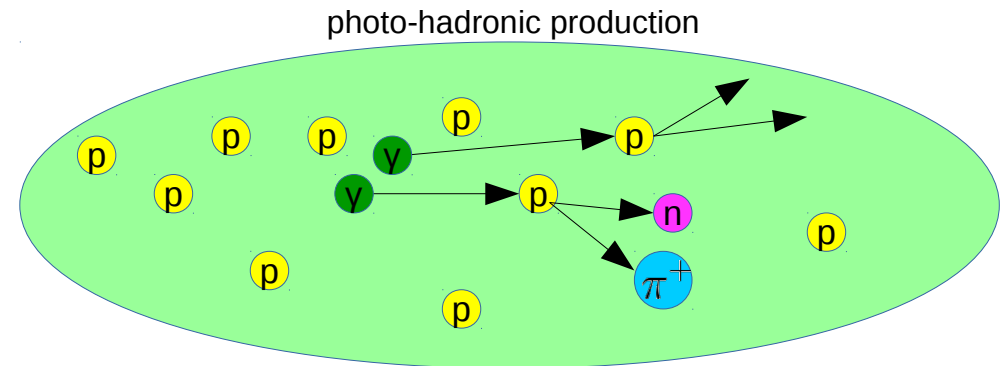
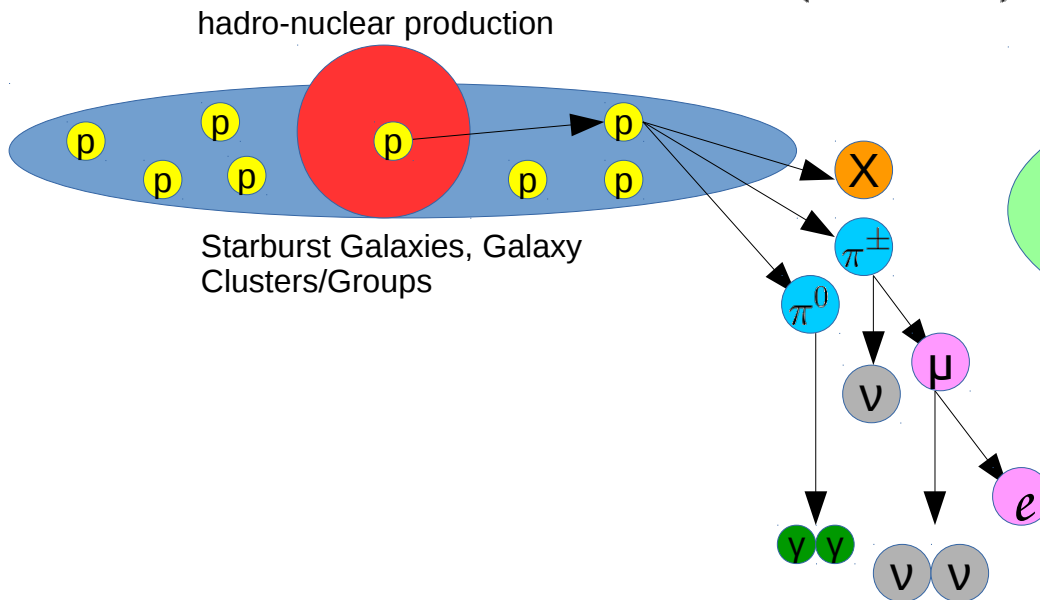
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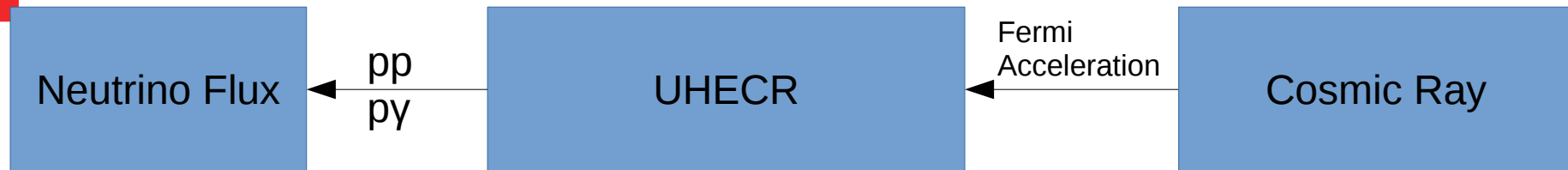
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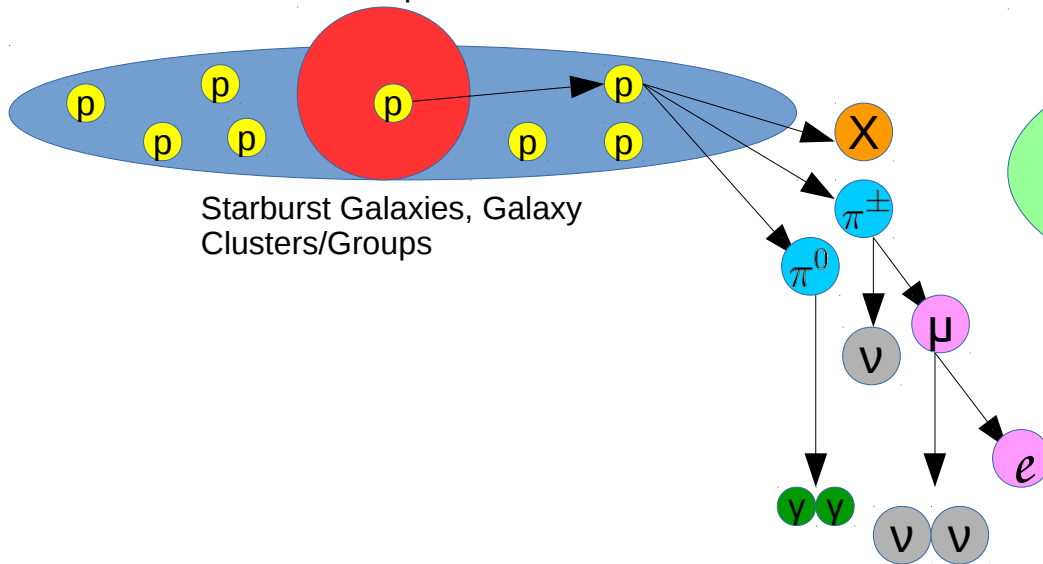
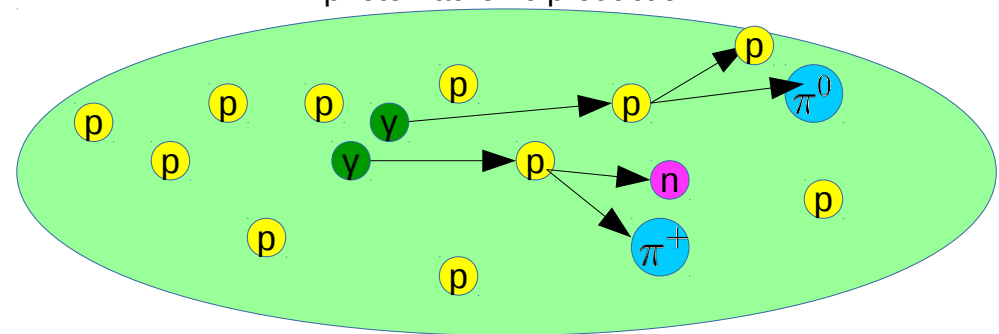
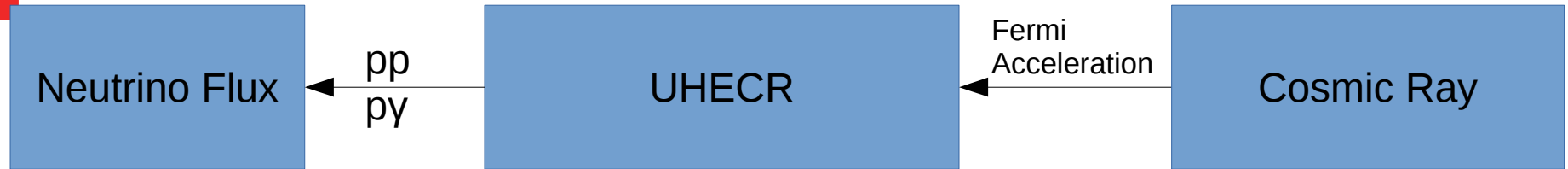


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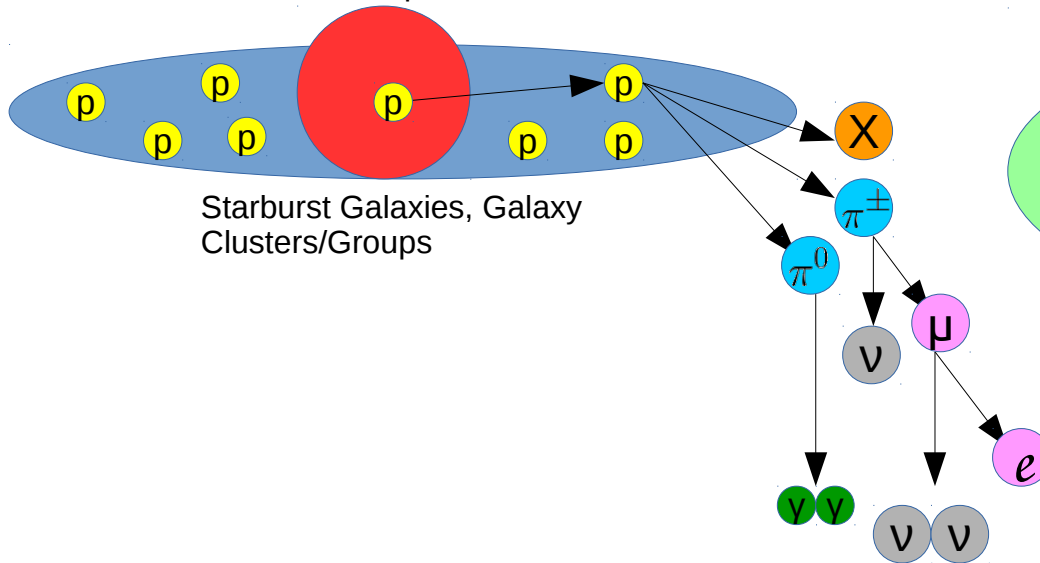
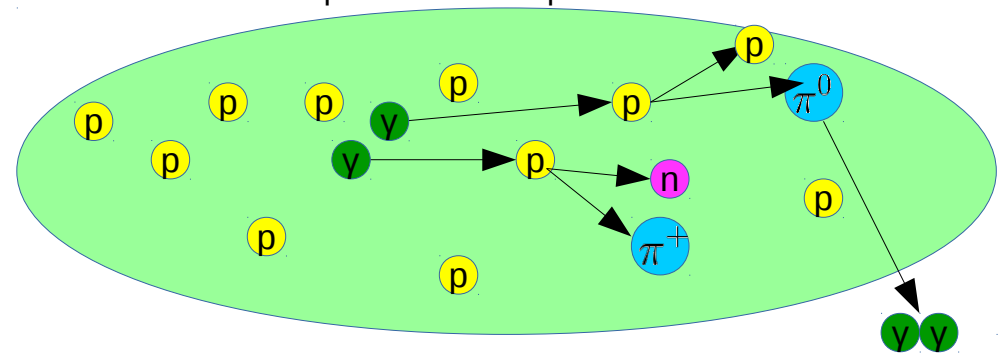
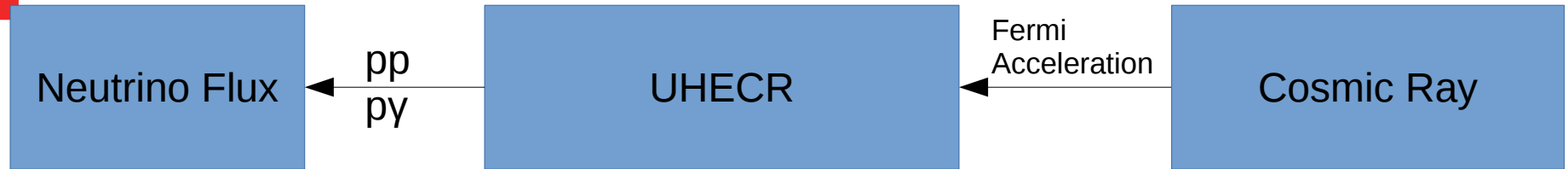


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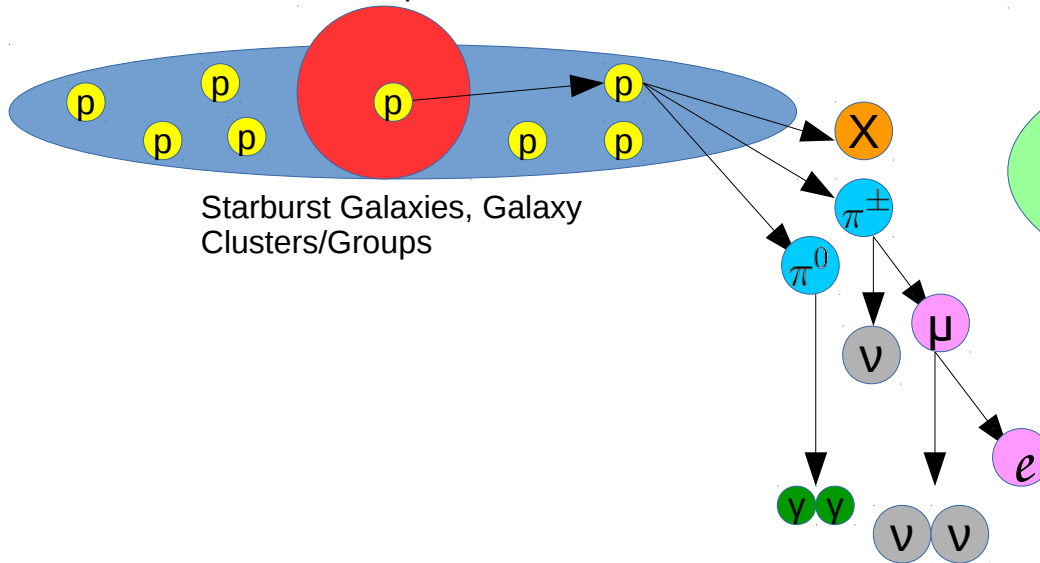
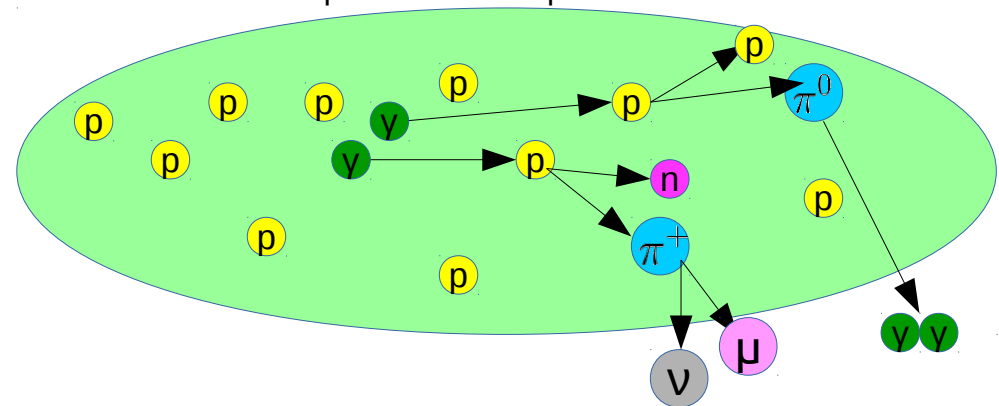
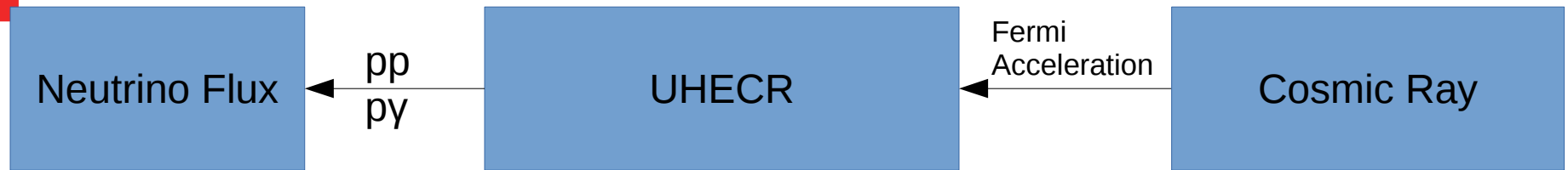


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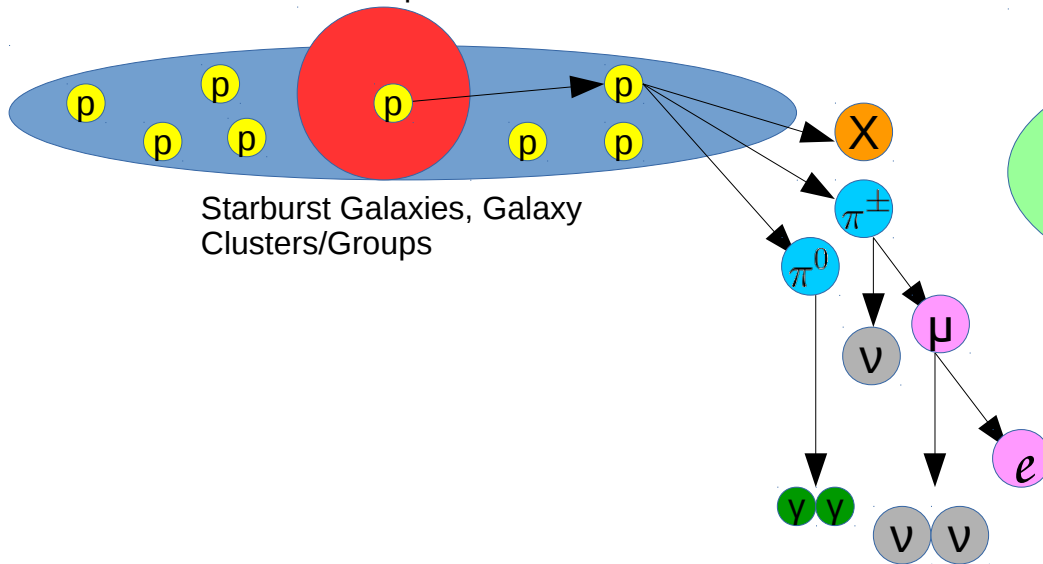
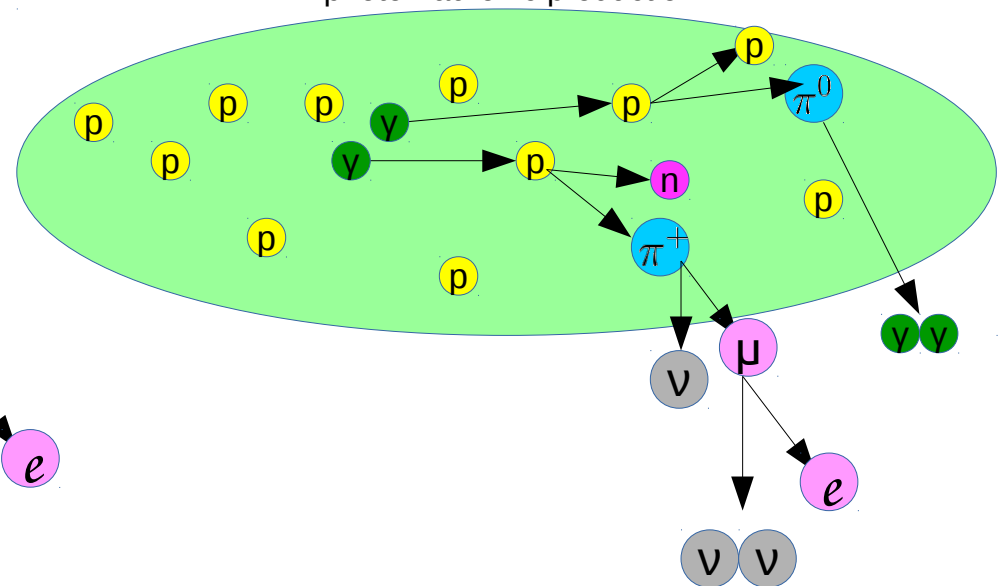


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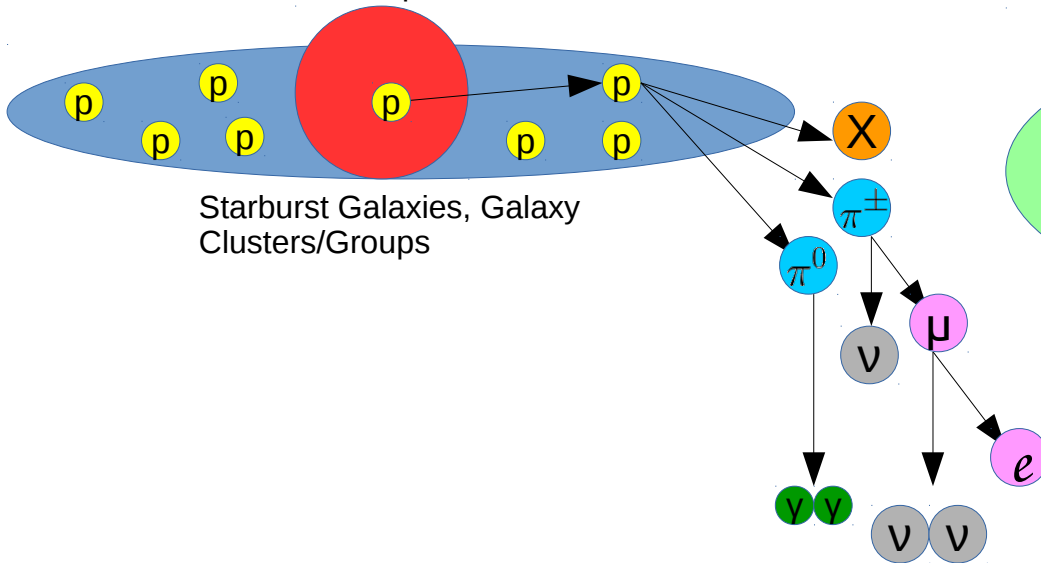
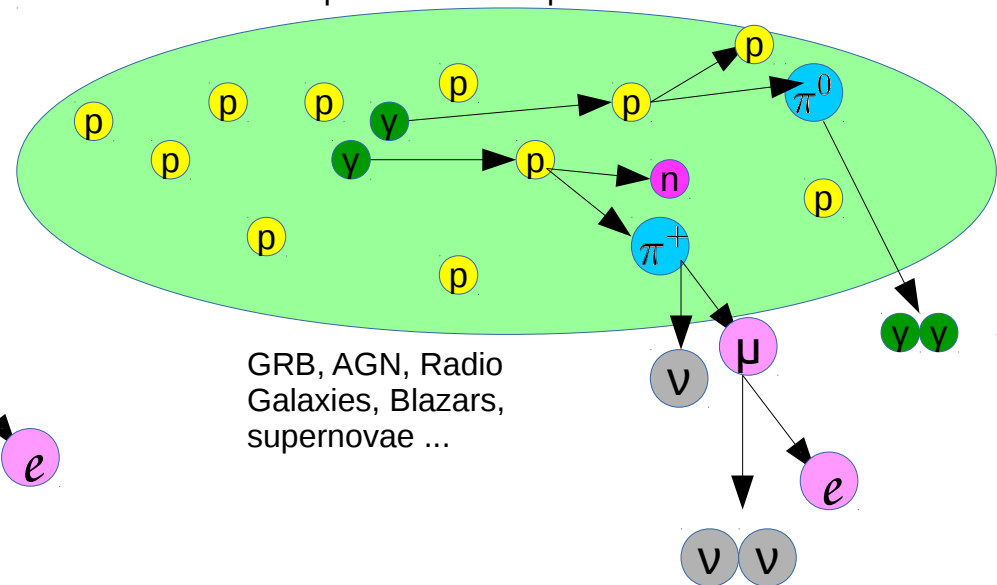
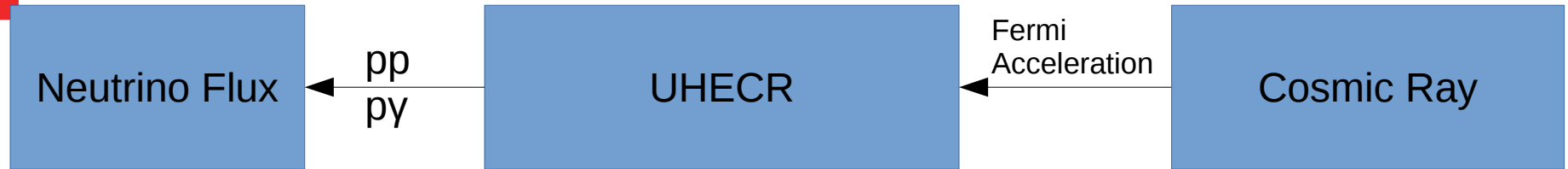


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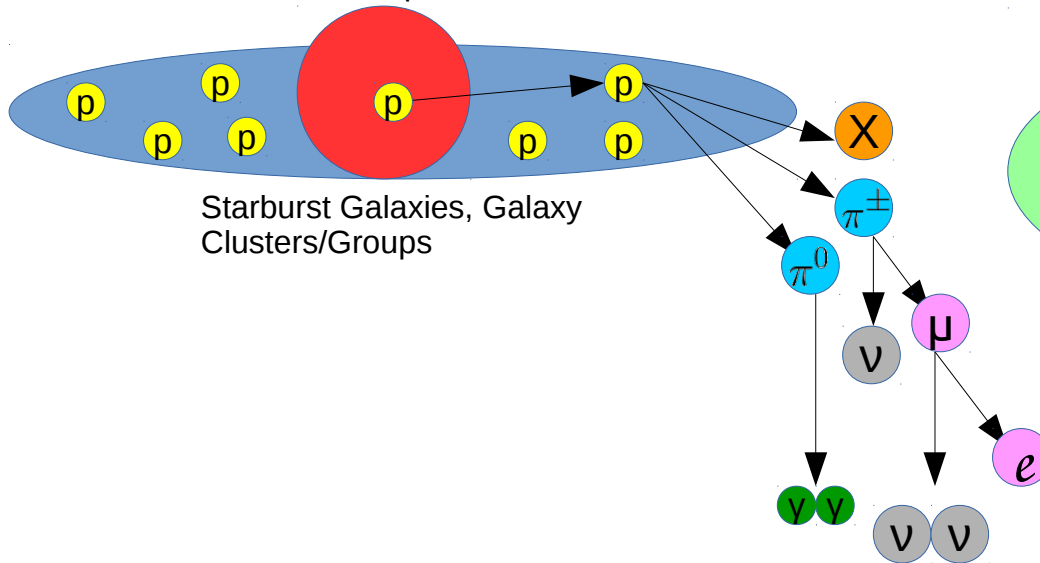
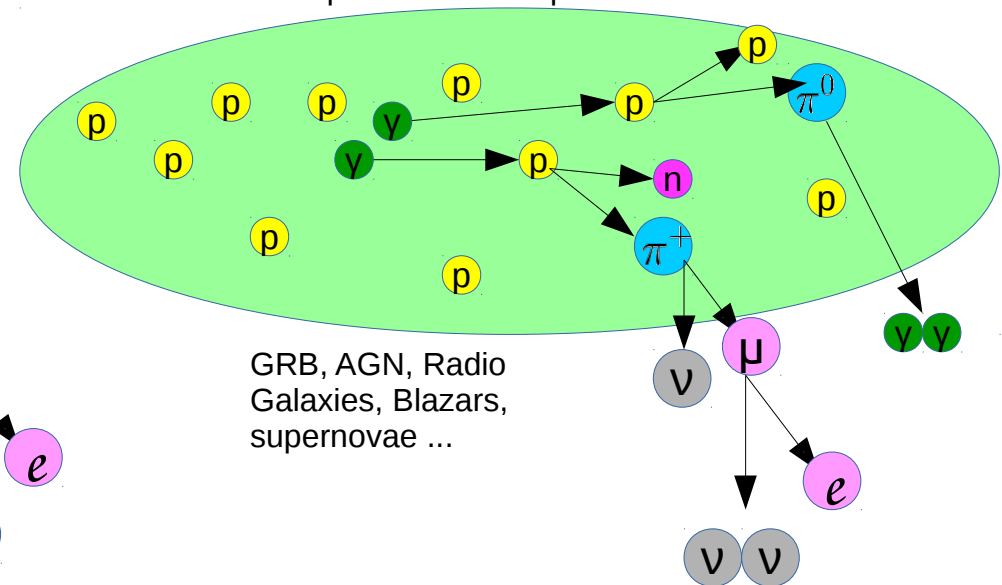
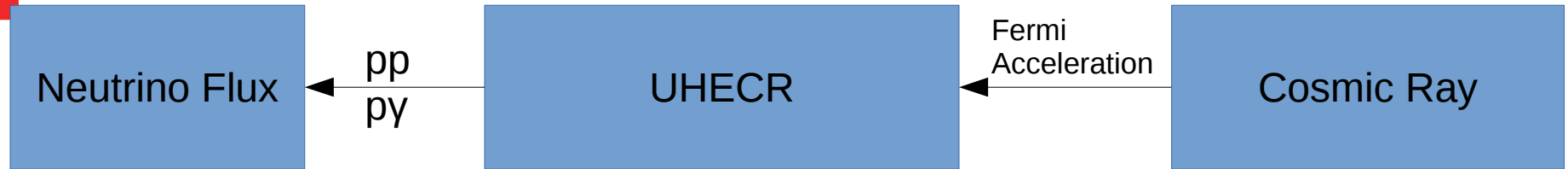


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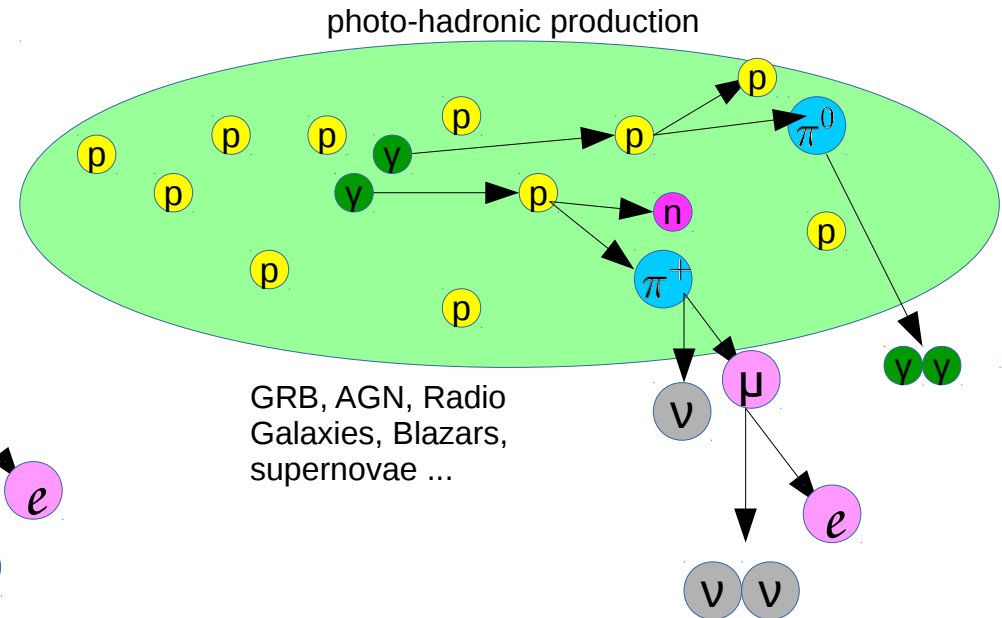
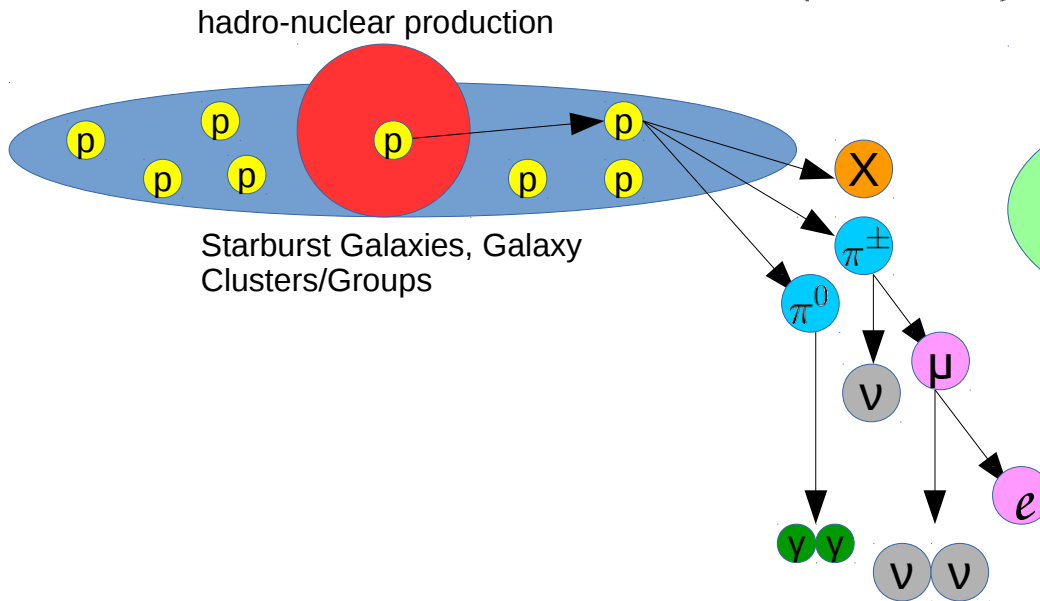
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	pp	pγ
Typical	(1 : 1 : 1)	(1 : 1 : 1)
μ damped	(4 : 7 : 7)	(4 : 7 : 7)





# IceCube Detector

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Mechanism:

$$\nu_l + N \rightarrow \begin{cases} l + X & (CC) \\ \nu_l + X & (NC) \end{cases}$$

Cherenkov radiation from interaction products: leptons and hadrons



# IceCube Detector

## HESE

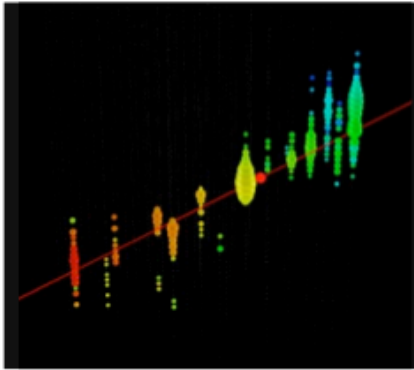
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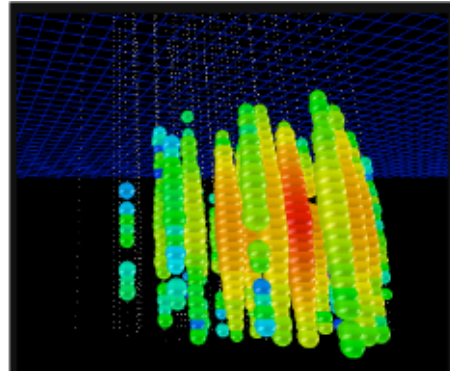
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## HESE



track



cascade

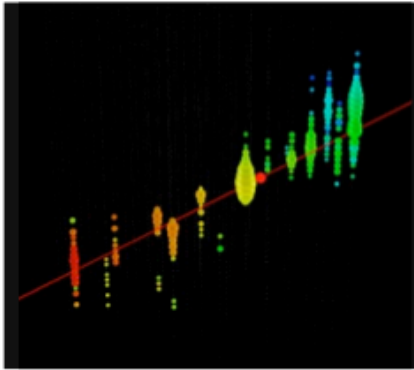
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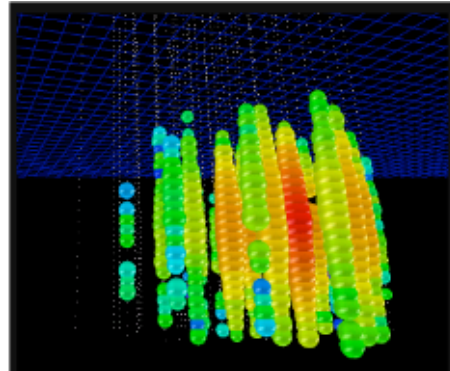
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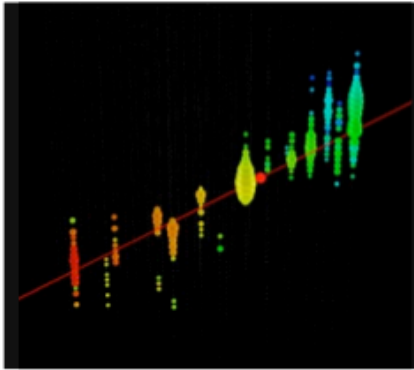
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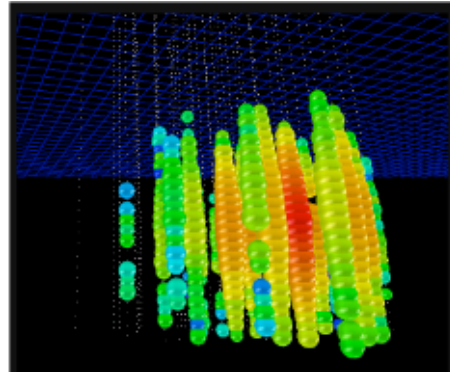
Through-going  
muon Event

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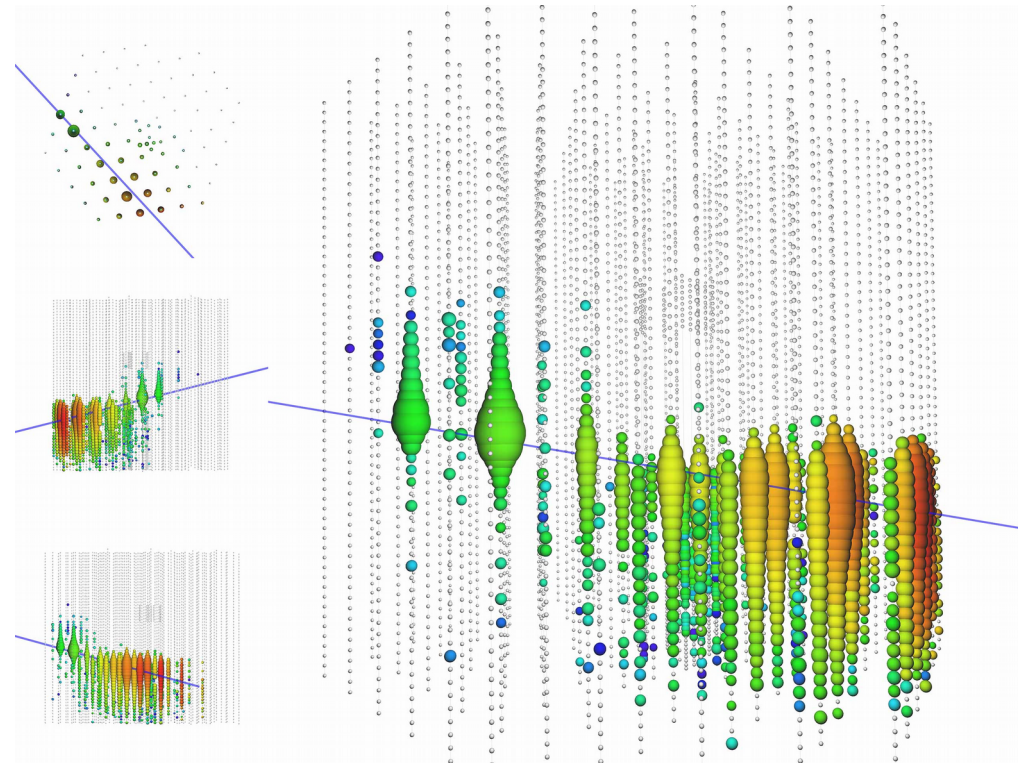
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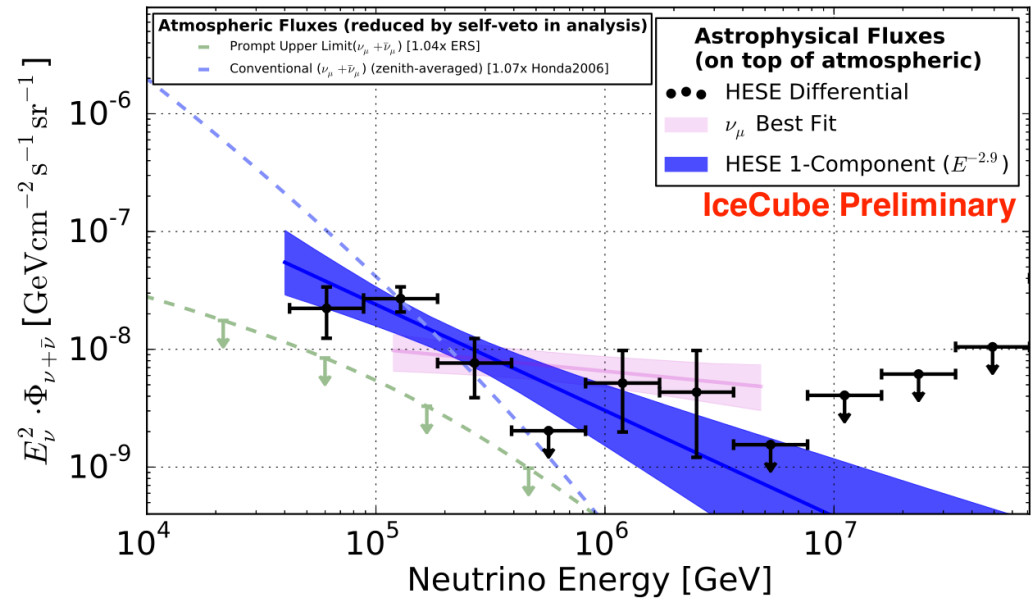
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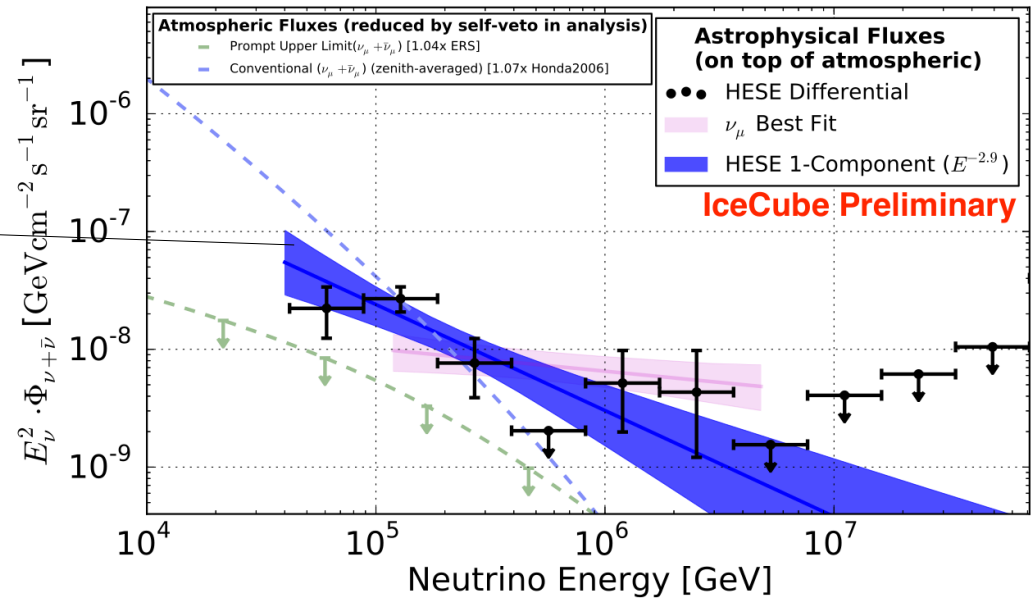


# Motivations

HESE:

$$\Phi_\nu \sim E^{-2.92^{+0.33}_{-0.29}}$$

Throughgoing:

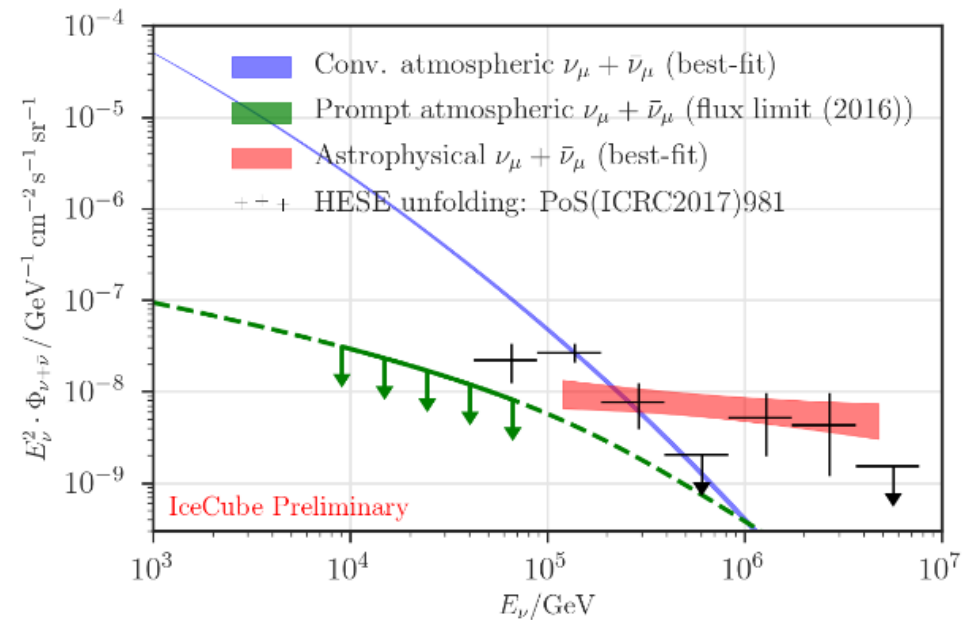
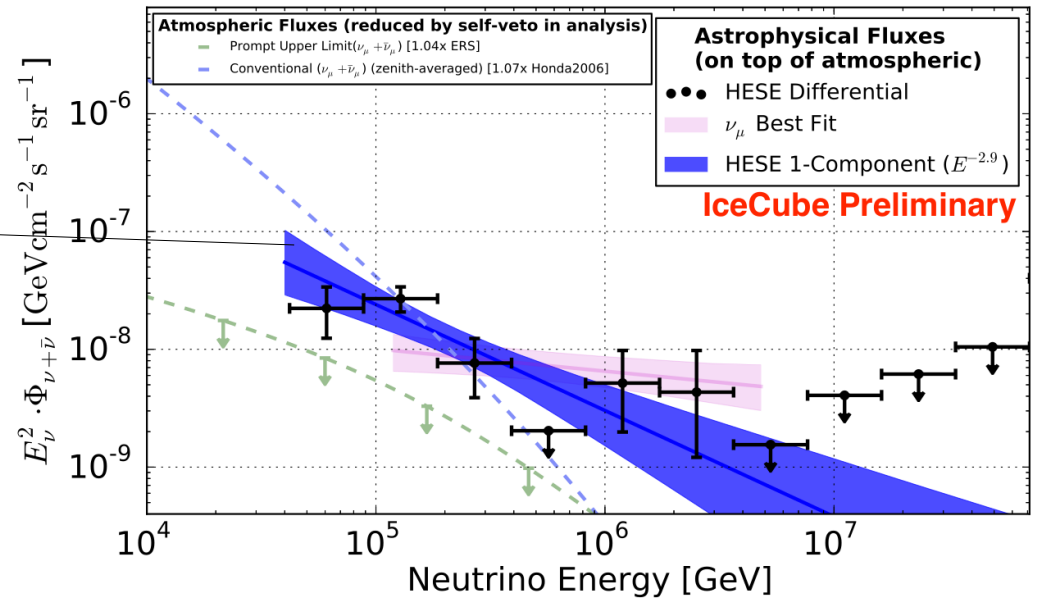


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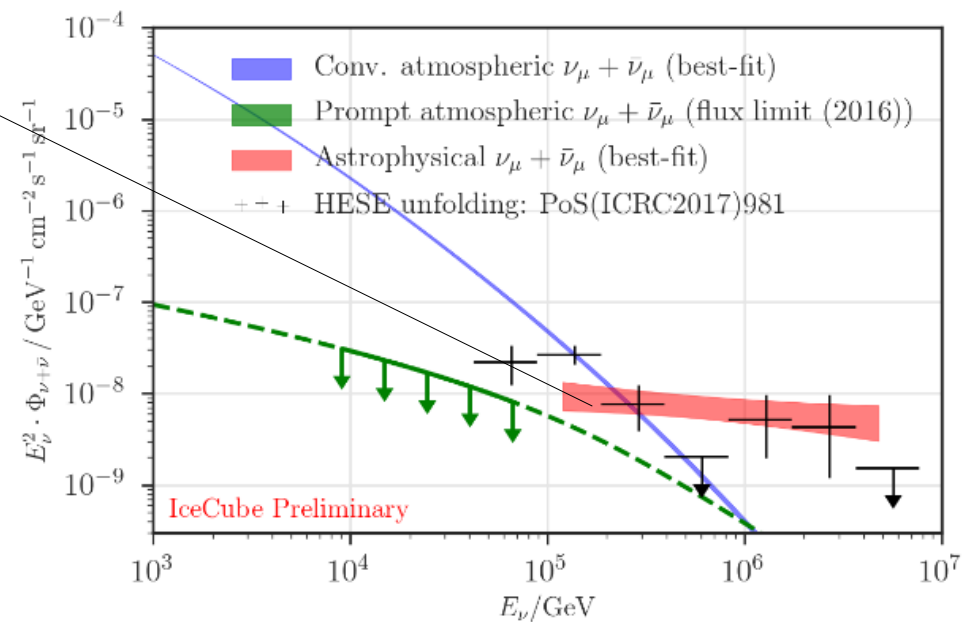
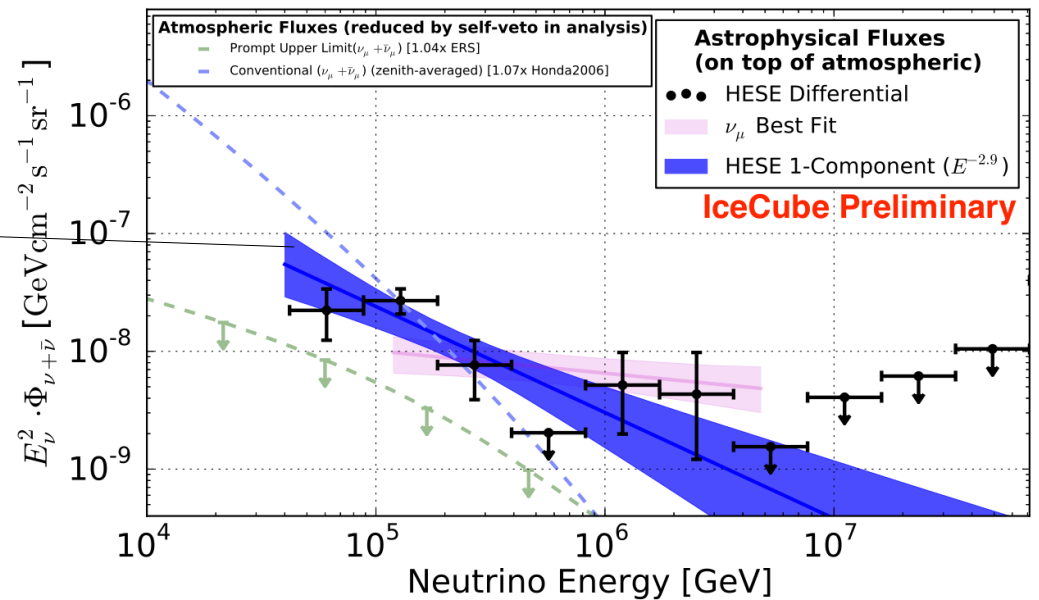
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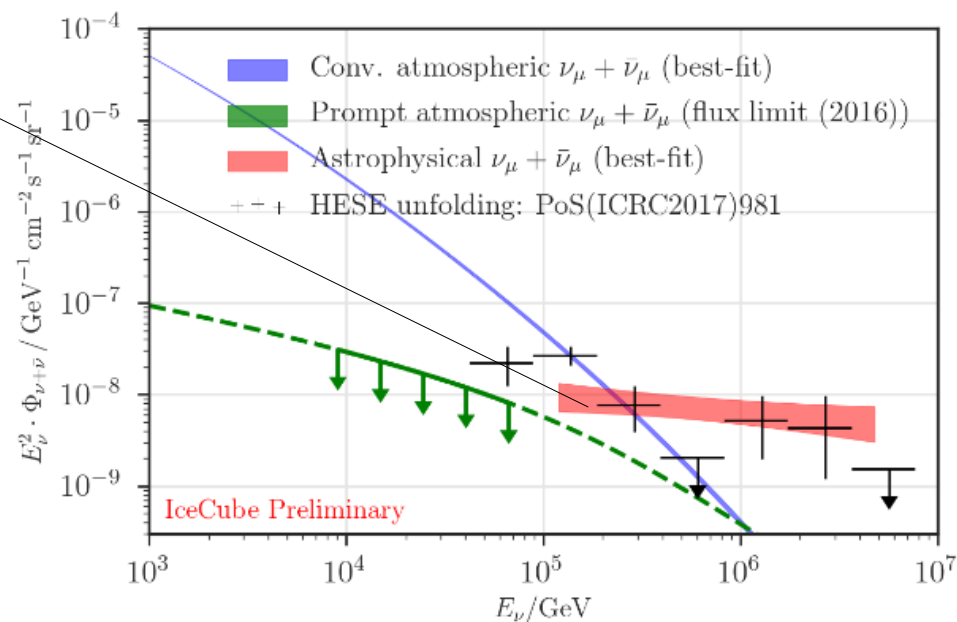
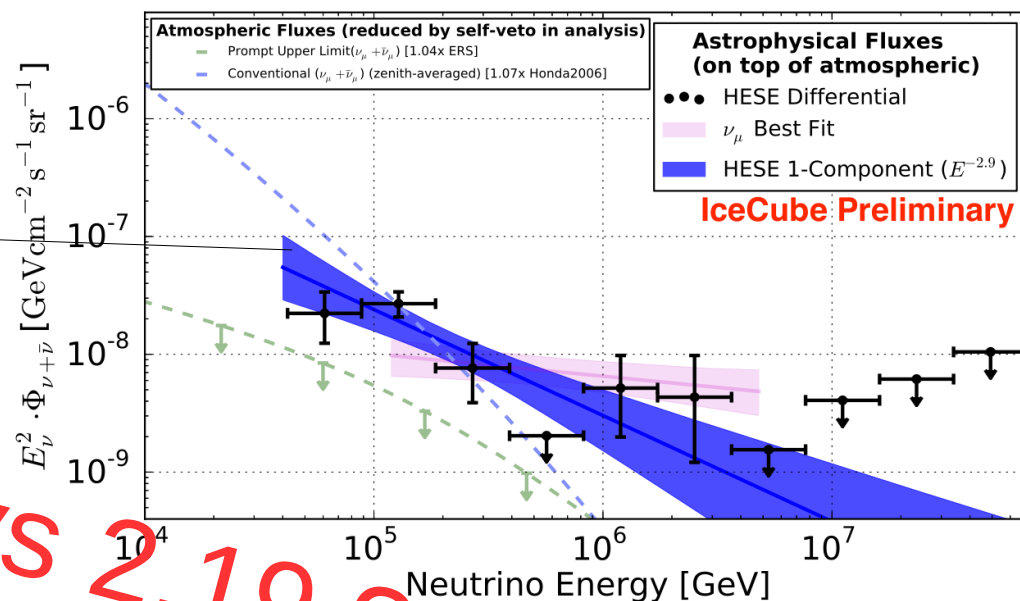
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2.92 vs 2.19 ?



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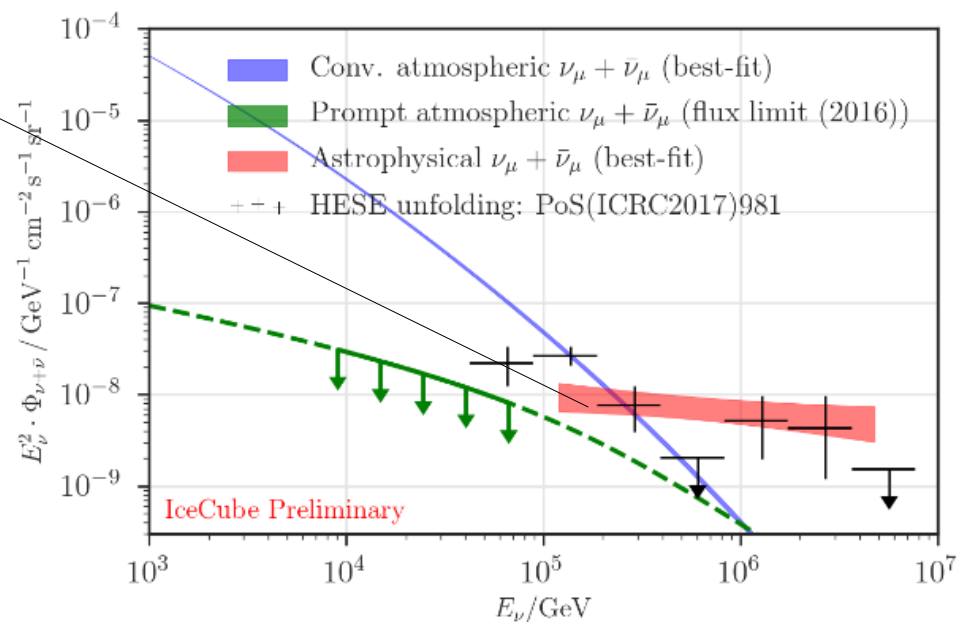
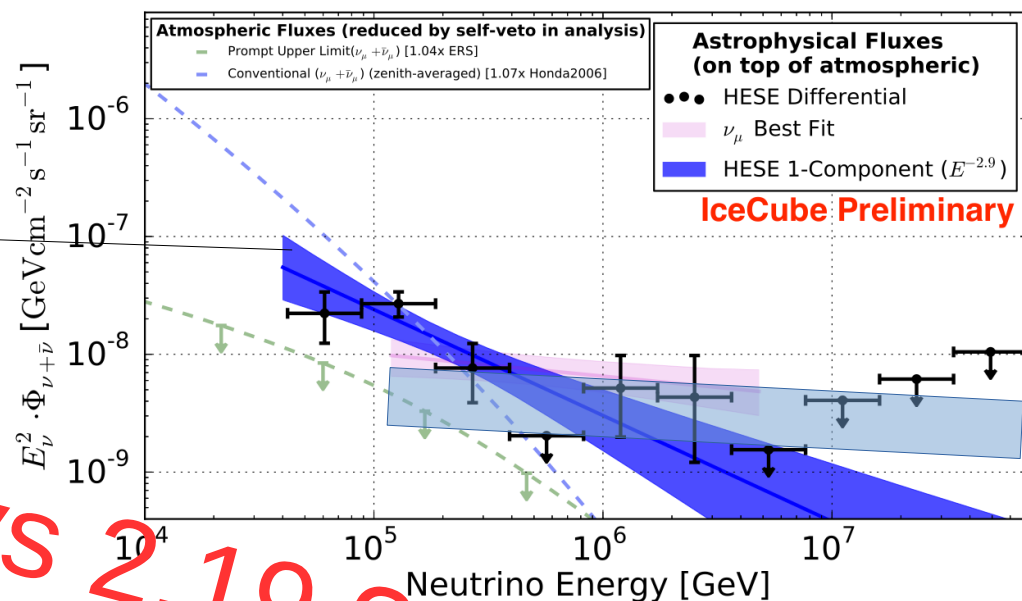
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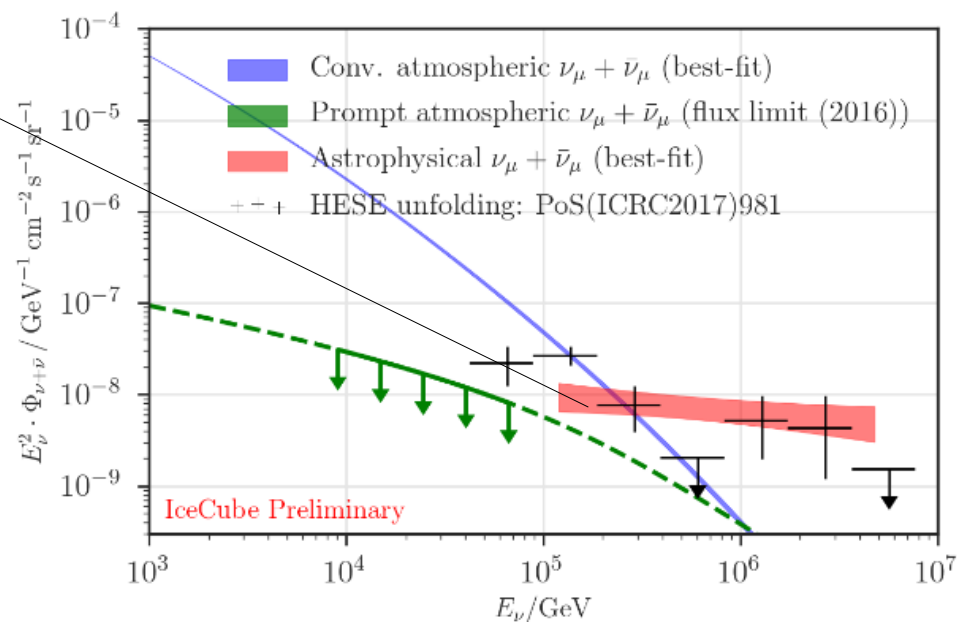
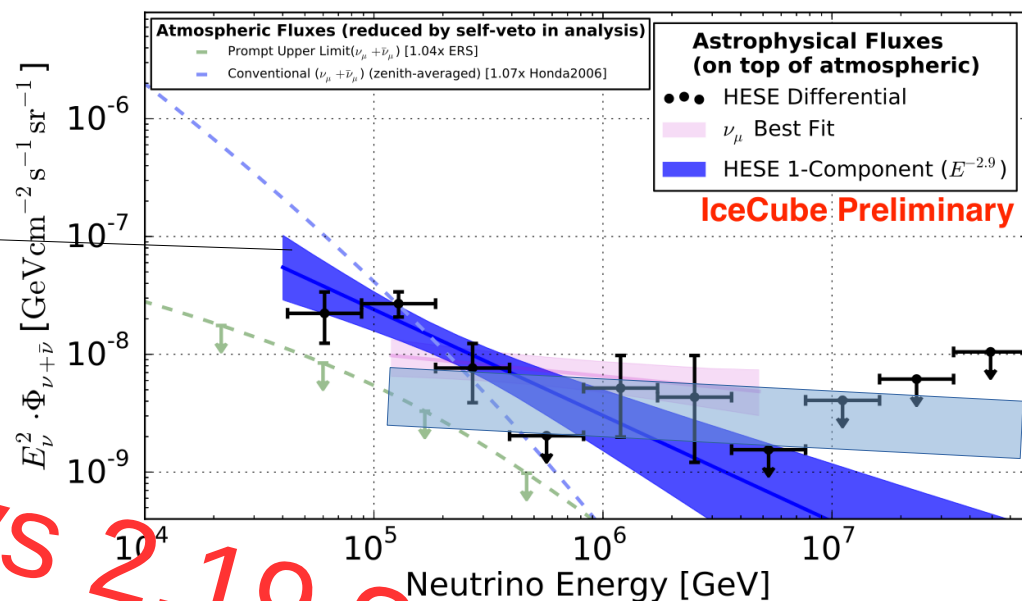
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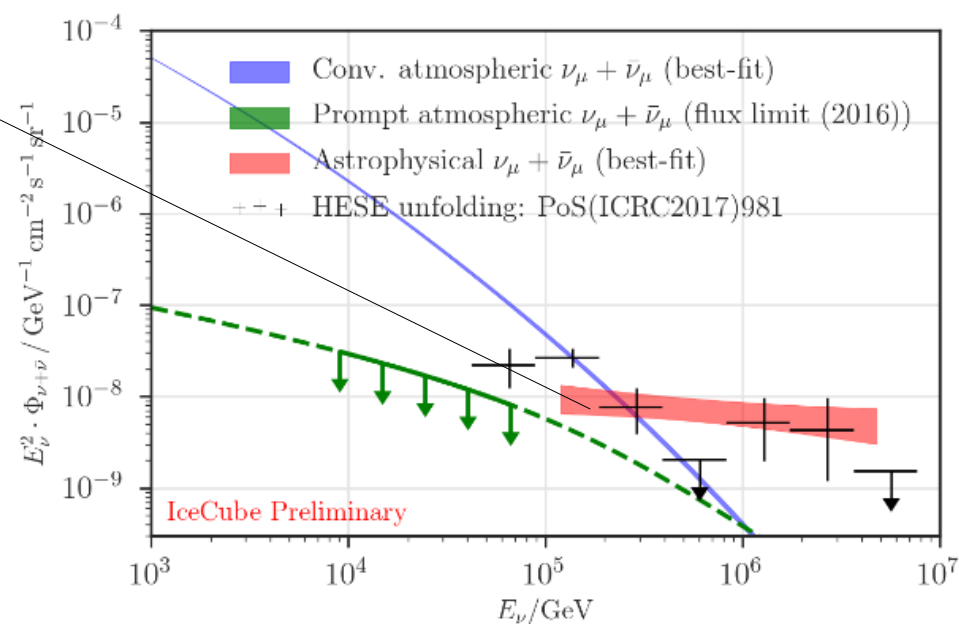
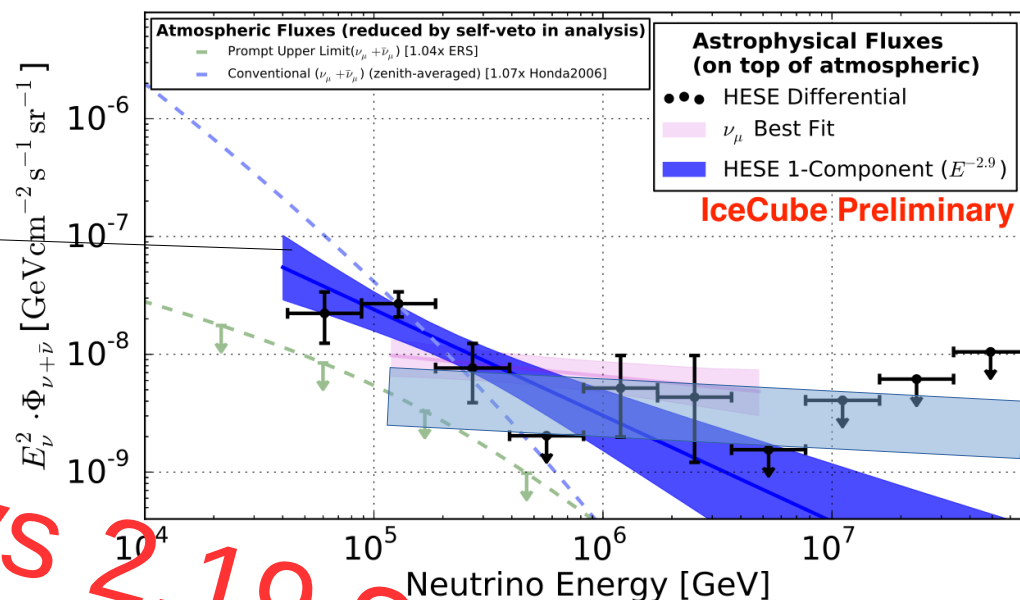
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- This spectrum might not be single component





## **2 Astro Comp Flux: Setup and Fitting**





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Cut off factor

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(111)                      (111) or (477)

Flux

→

Reconstruction

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```
graph LR; Flux[Flux] --> Reconstruction[Reconstruction];
```

The diagram illustrates the process of neutrino flux reconstruction. It starts with the flux  $\Phi_{\nu\ell}(E_\nu)$ , which is then processed through a 'Reconstruction' block to produce the final output. The flux is represented by a blue box labeled 'Flux', and the reconstruction is represented by a blue box labeled 'Reconstruction'. An arrow points from the 'Flux' box to the 'Reconstruction' box. Above the 'Flux' box, the equation for  $\Phi_{\nu\ell}(E_\nu)$  is shown, with annotations for the parameters  $f_{1,\ell}$  and  $f_{2,\ell}$  corresponding to the labels '(111)' and '(111) or (477)' respectively. The flux is also shown as a function of energy  $E_\nu$  in the equation above it.

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(111) (111) or (477)



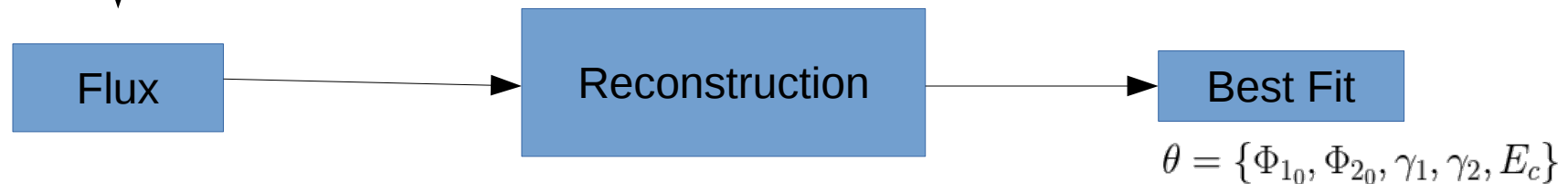
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(111)                      (111) or (477)





# Fitting Results

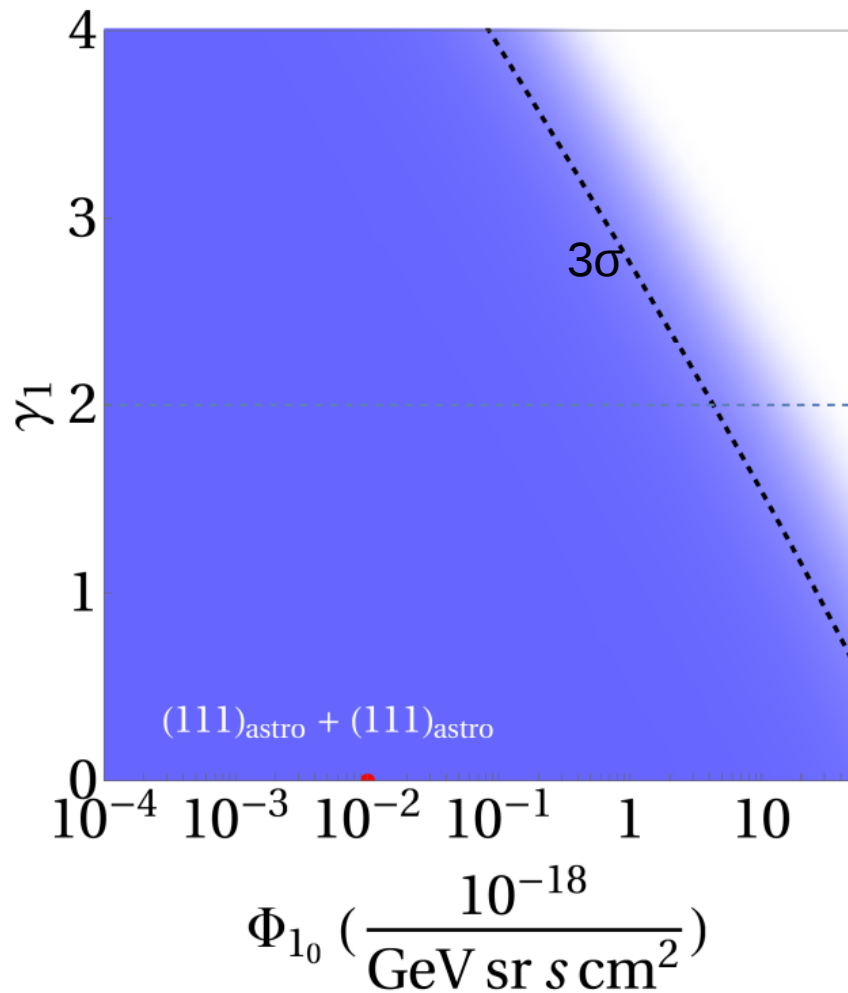
1st Comp.	2nd Comp.	$\Phi_{1_0}$	$\Phi_{2_0}$	$\gamma_1$	$\gamma_2$	$E_c/100 \text{ TeV}$	TS/dof
(1 : 1 : 1)	(1 : 1 : 1)	0.01	2.21	$1.47 \times 10^{-4}$	2.08	0.10	1.91
(1 : 1 : 1)	(4 : 7 : 7)	17.18	0.88	$3.19 \times 10^{-10}$	1.83	0.50	1.48

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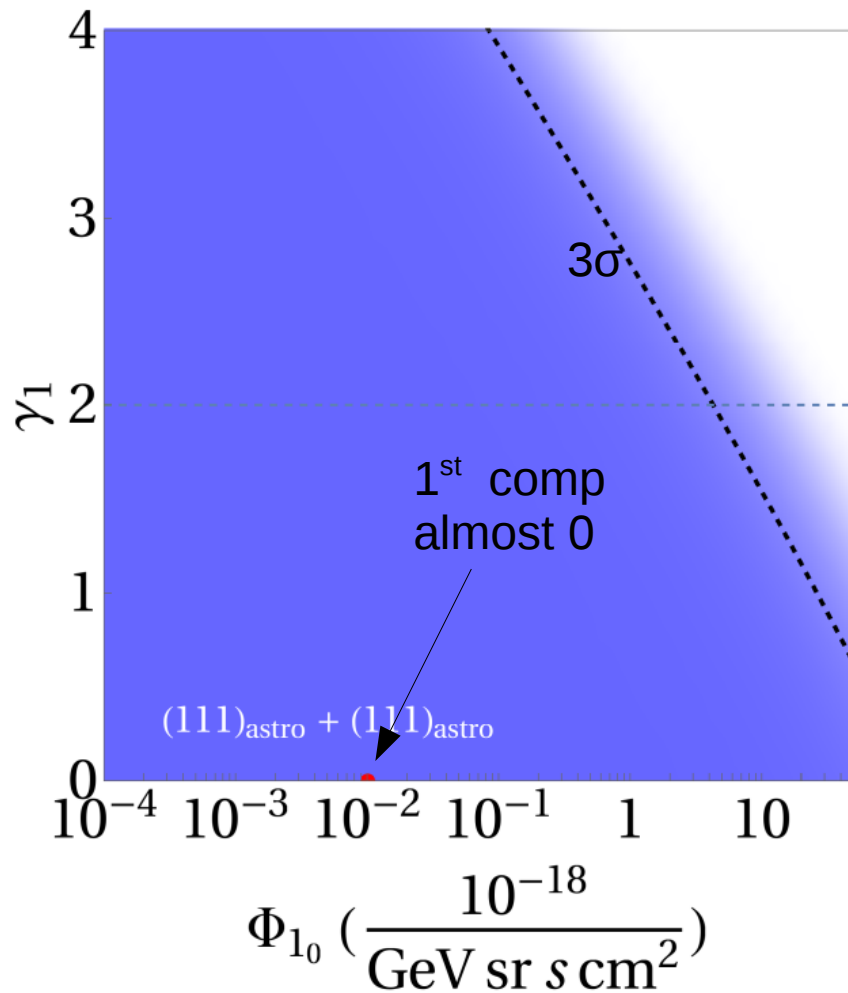
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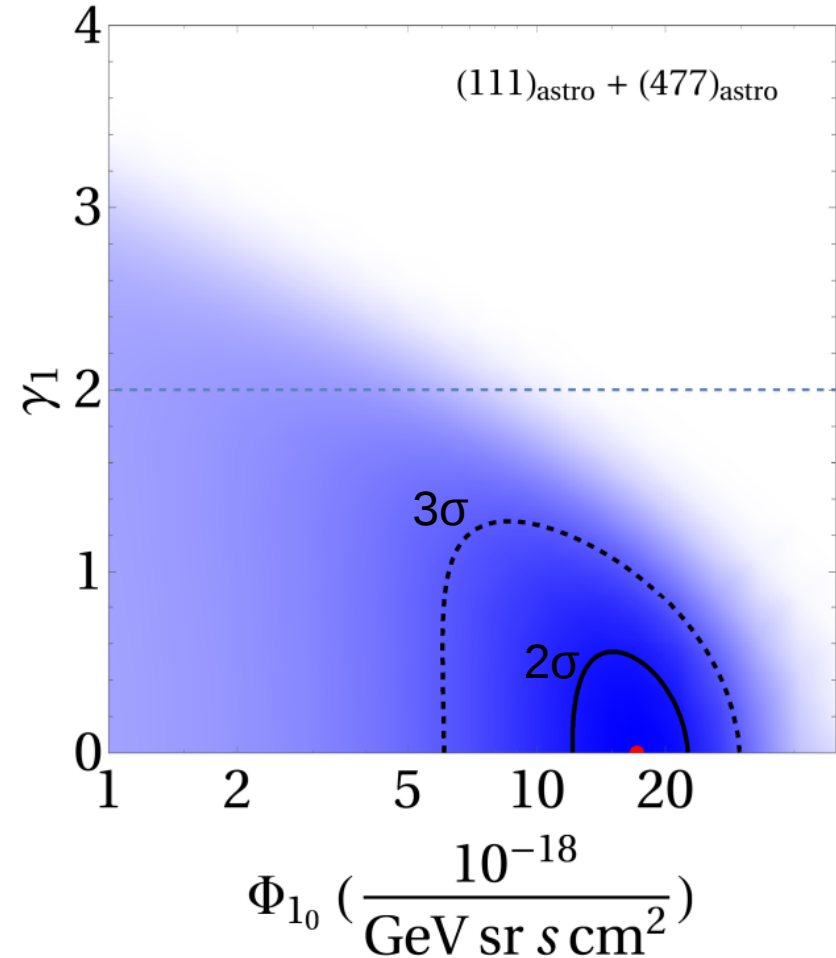
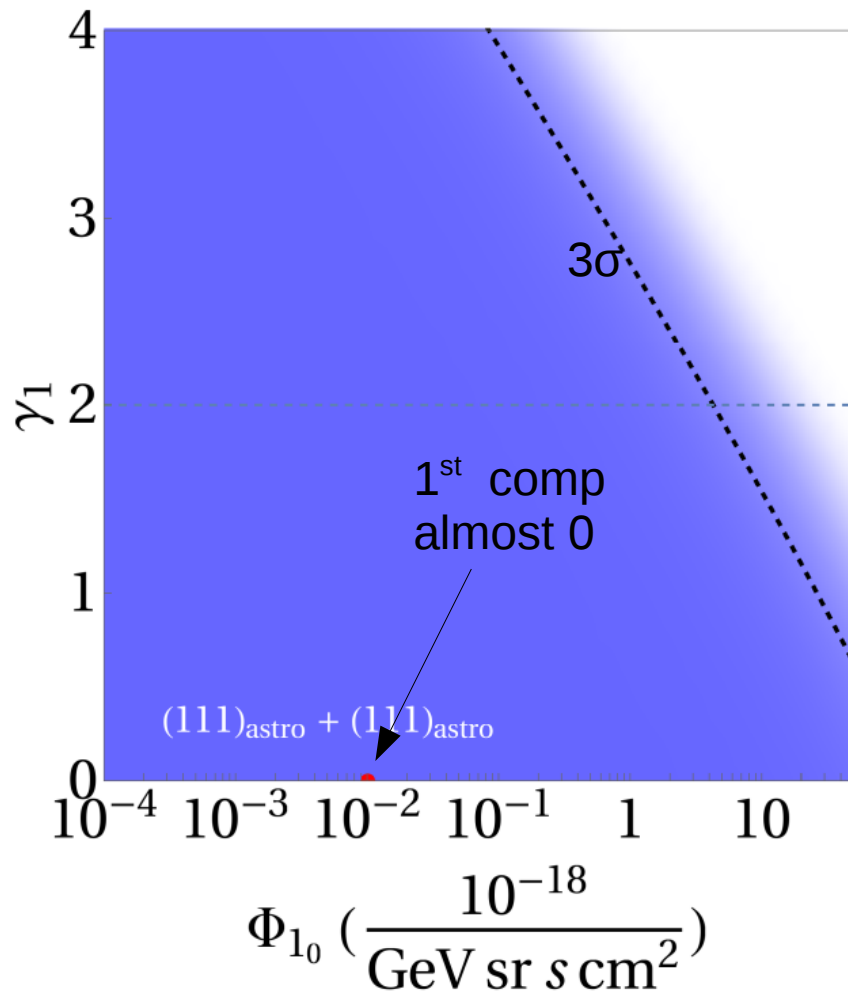
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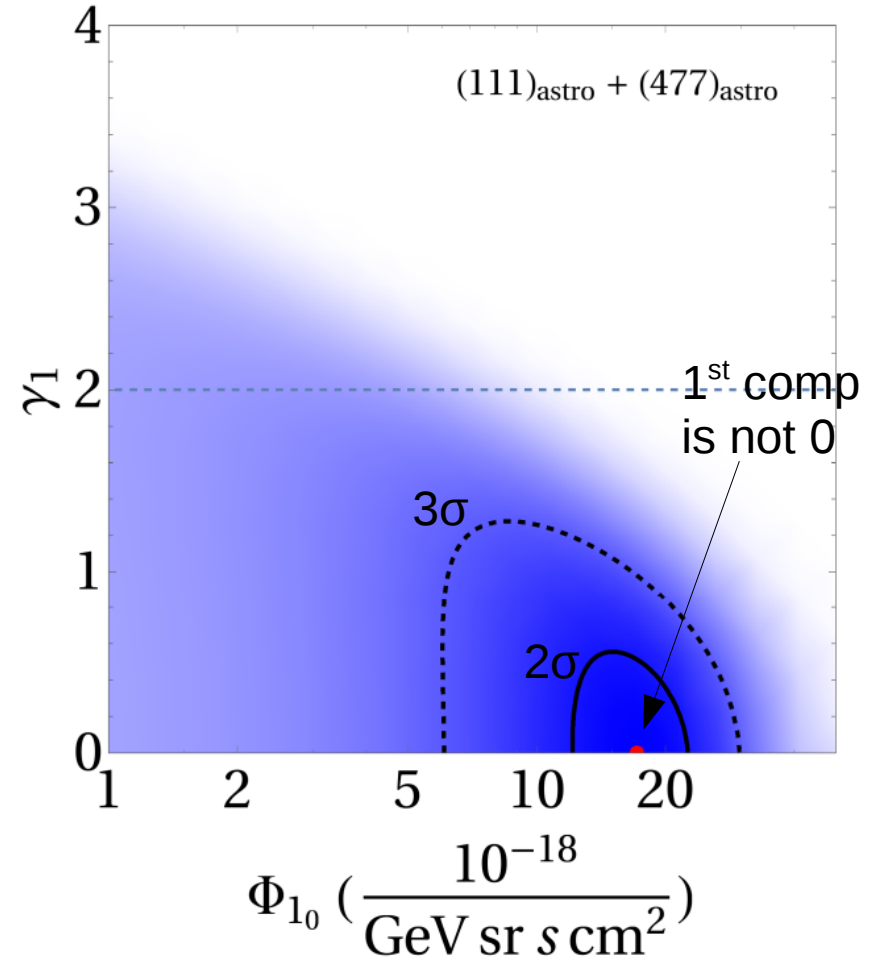
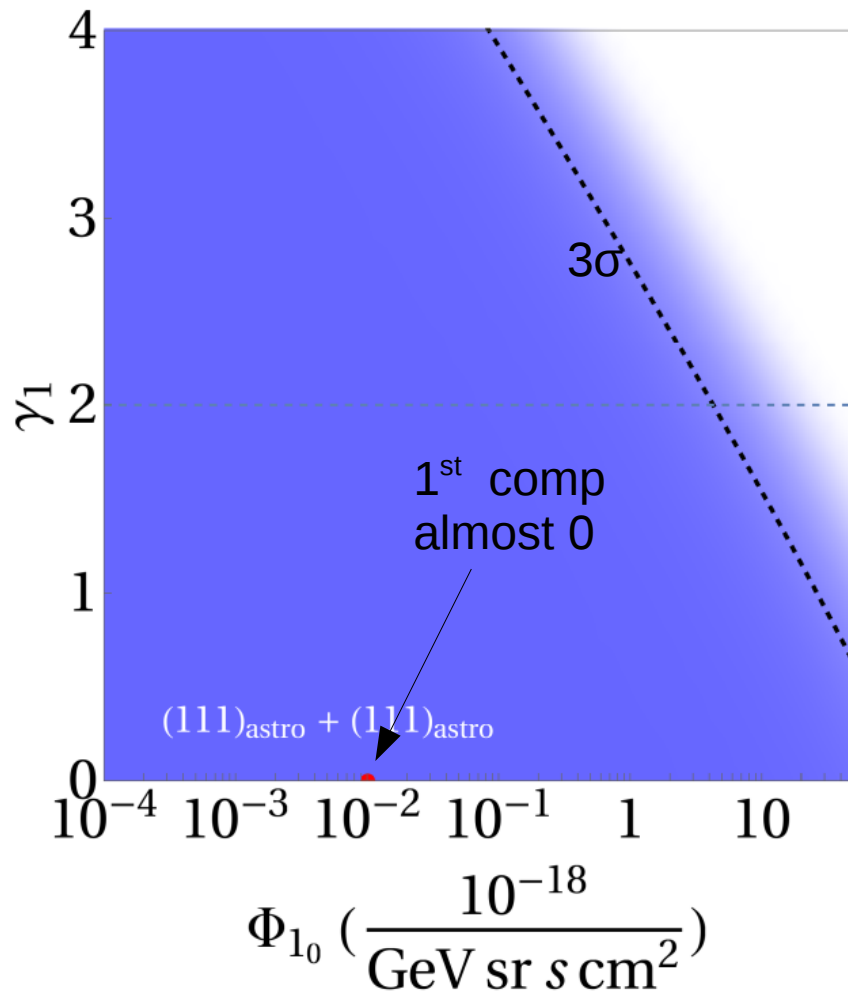
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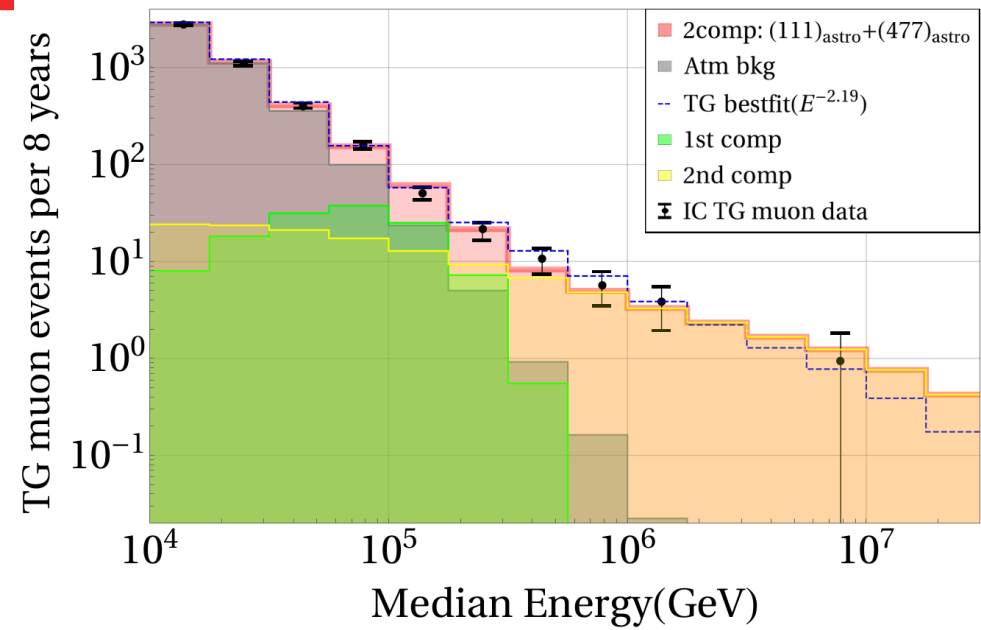
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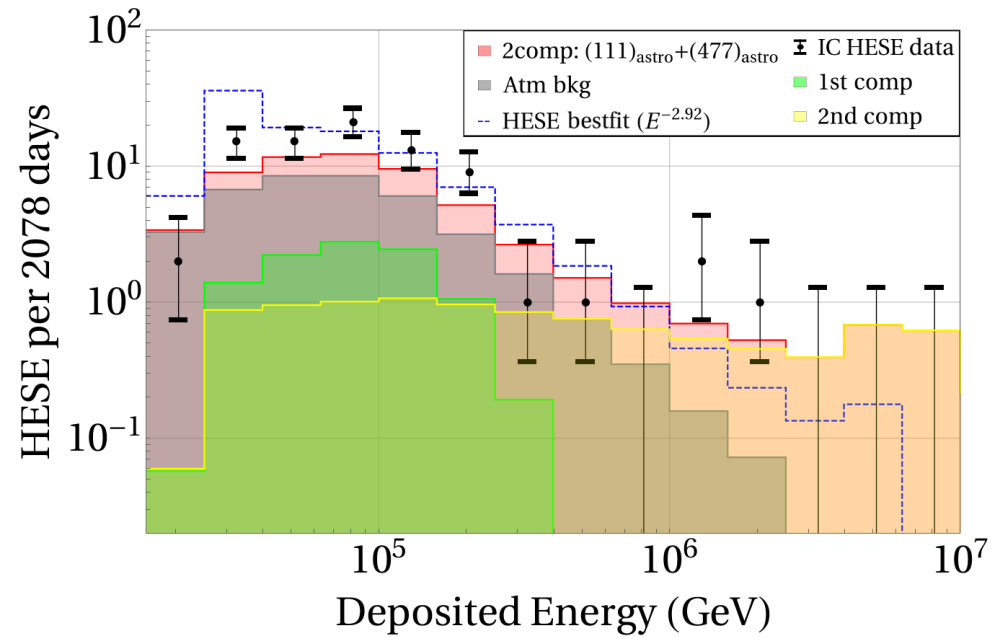
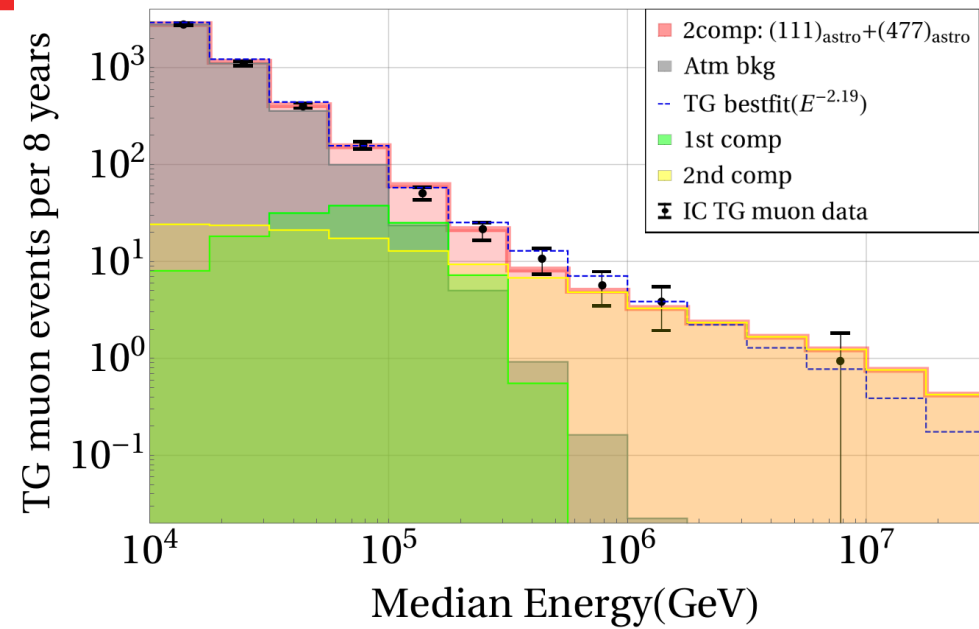
# Best Fit Event Spectrum

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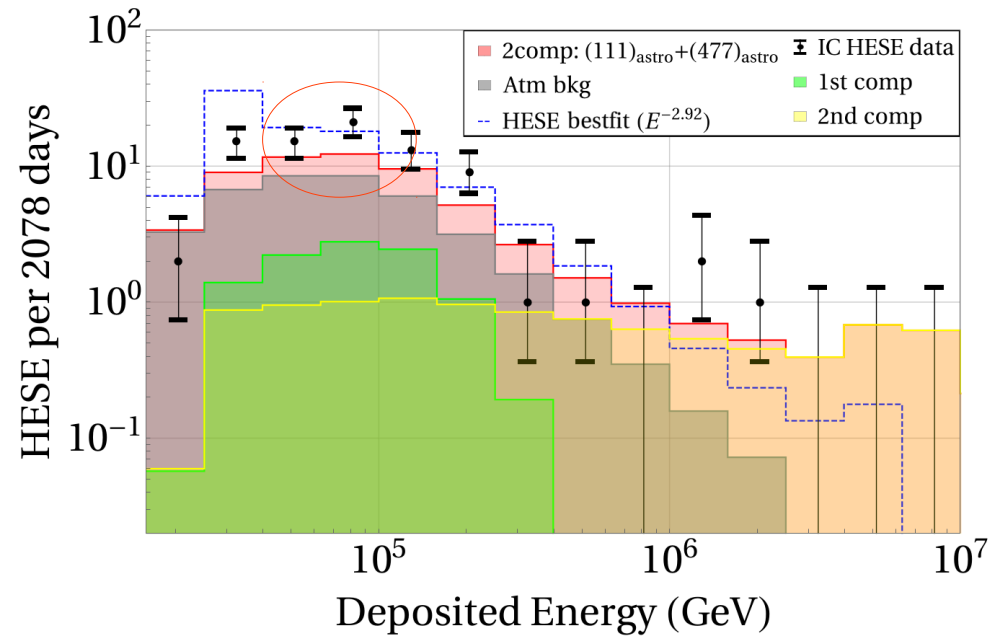
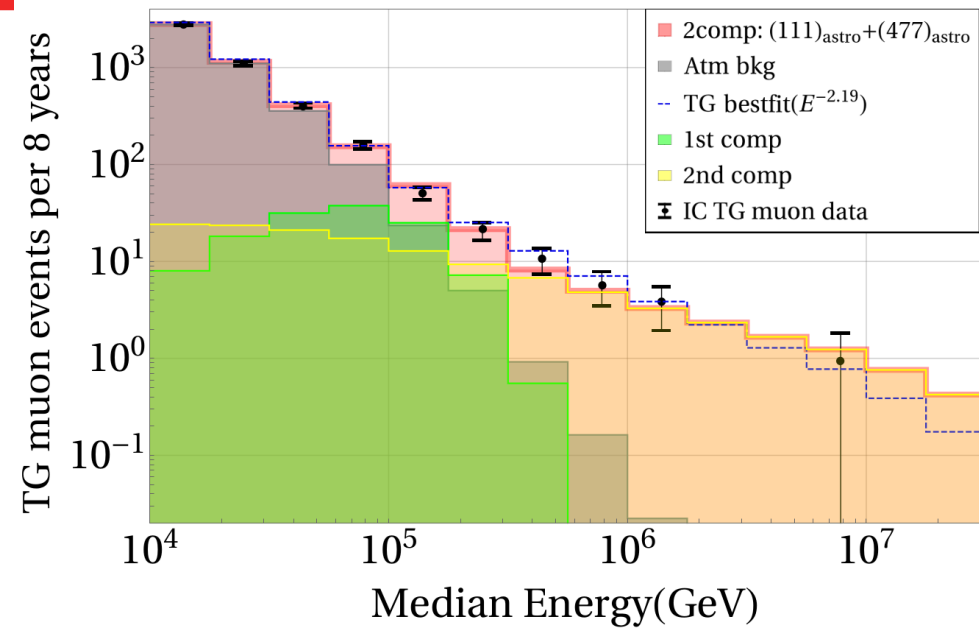




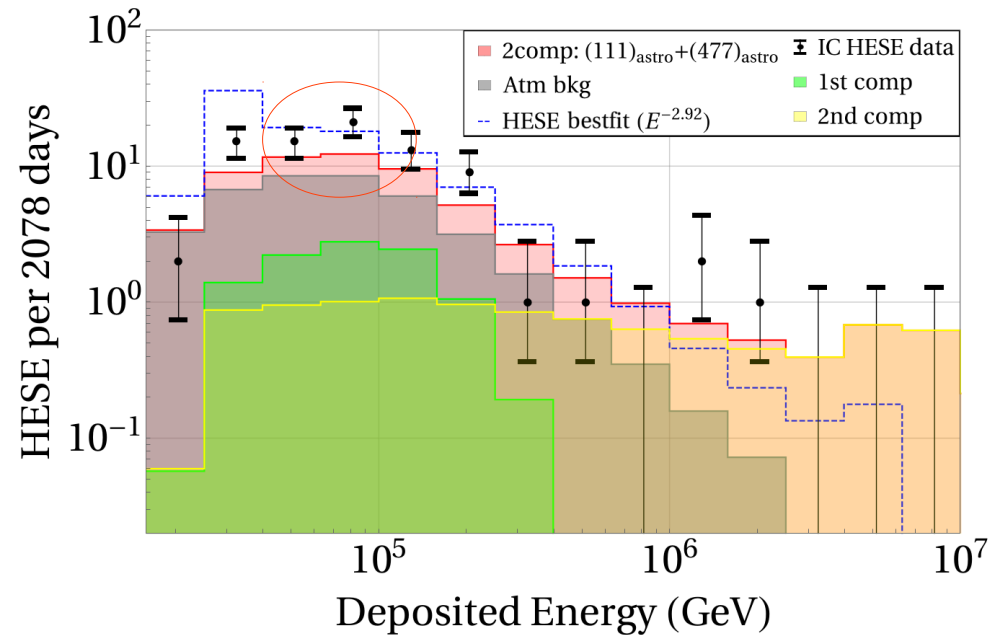
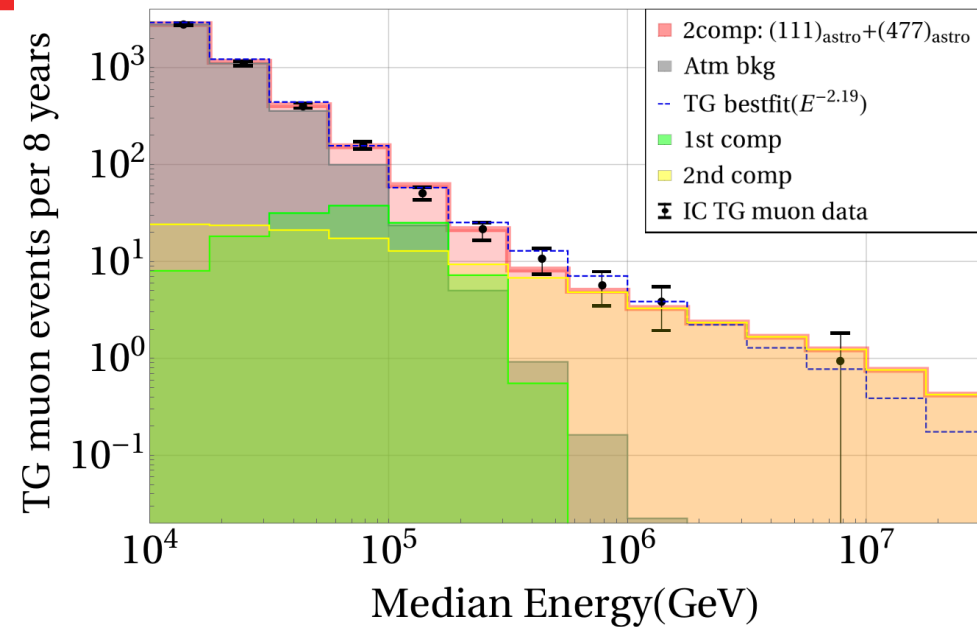
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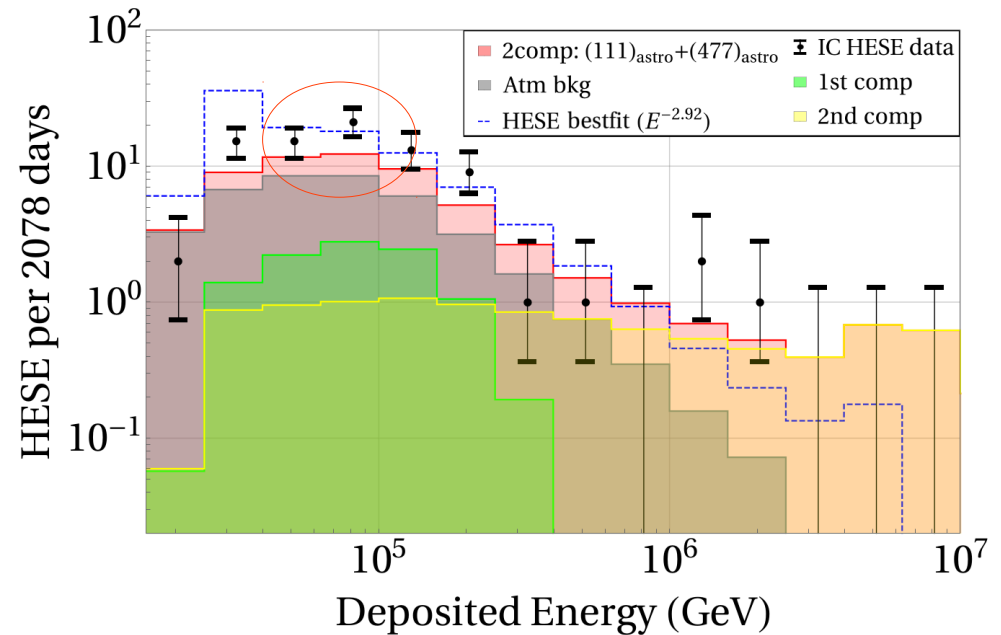
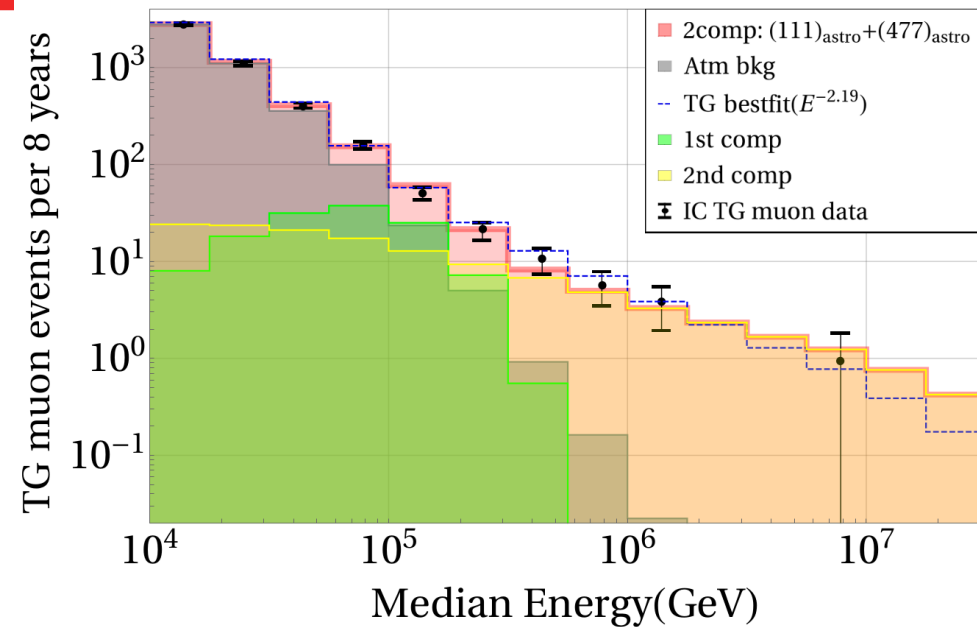


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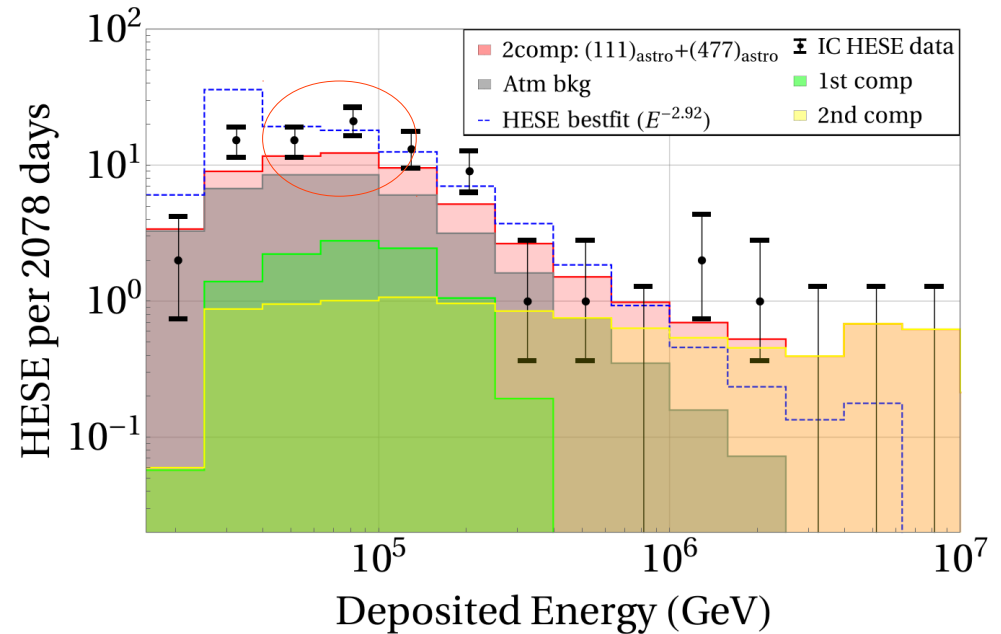
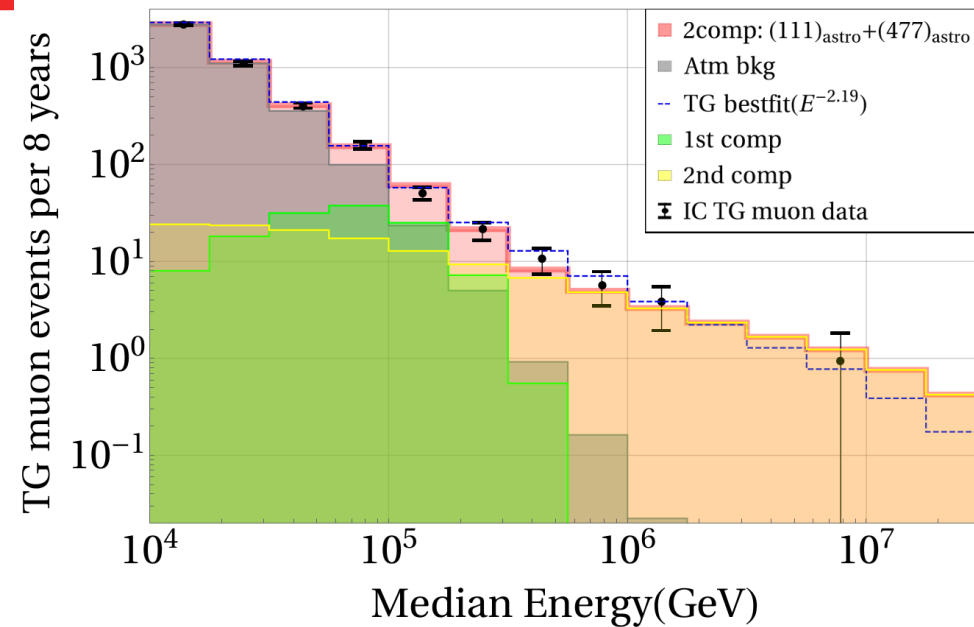
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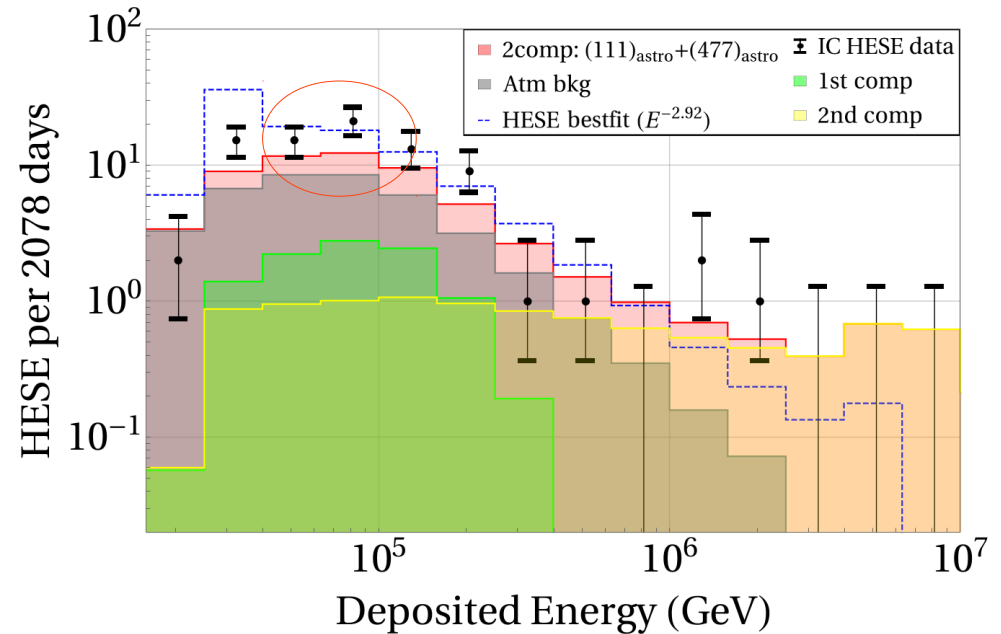
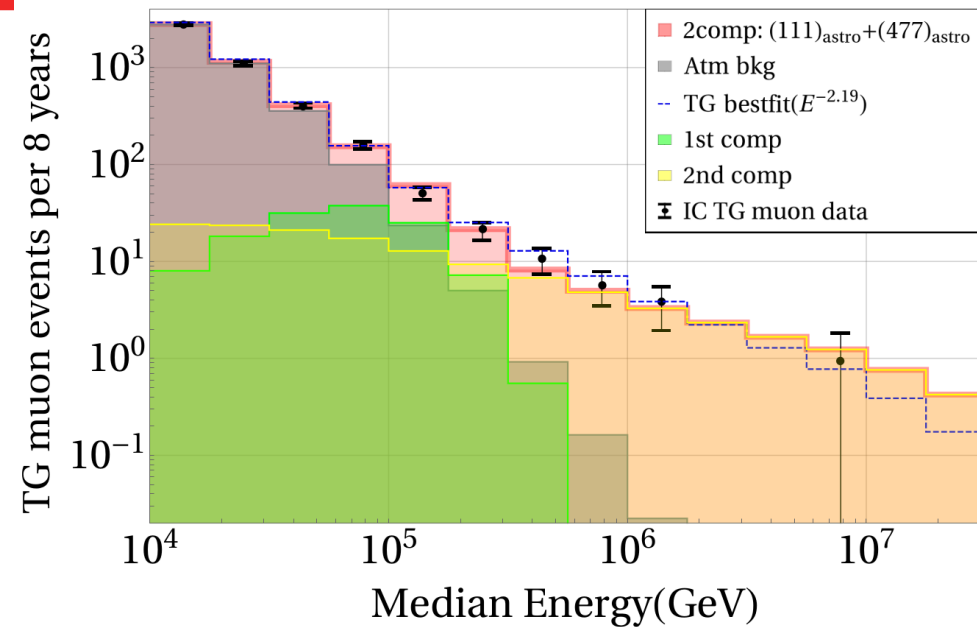
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Glashow Resonance

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## Glashow Resonance

- Statistically, (111+477) fit is slightly favored than (111+111)



# DM+1Comp Flux: Model and Fitting



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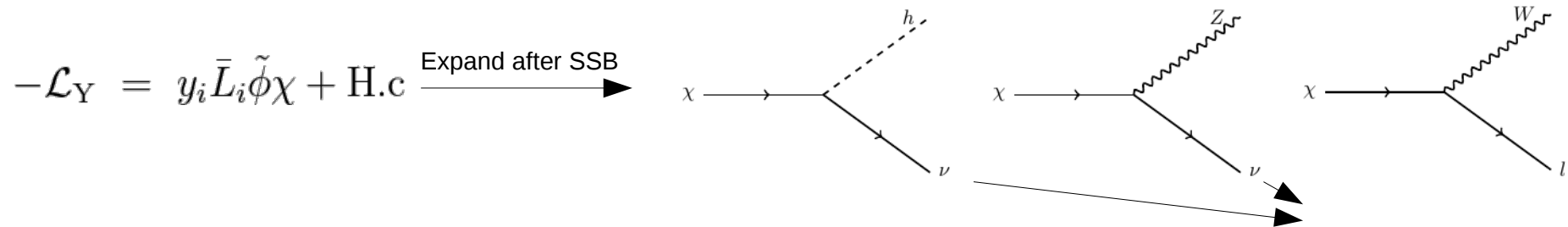
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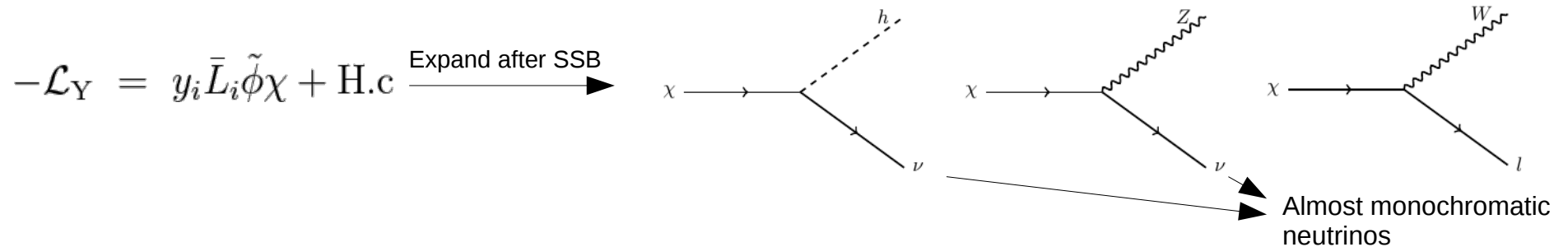
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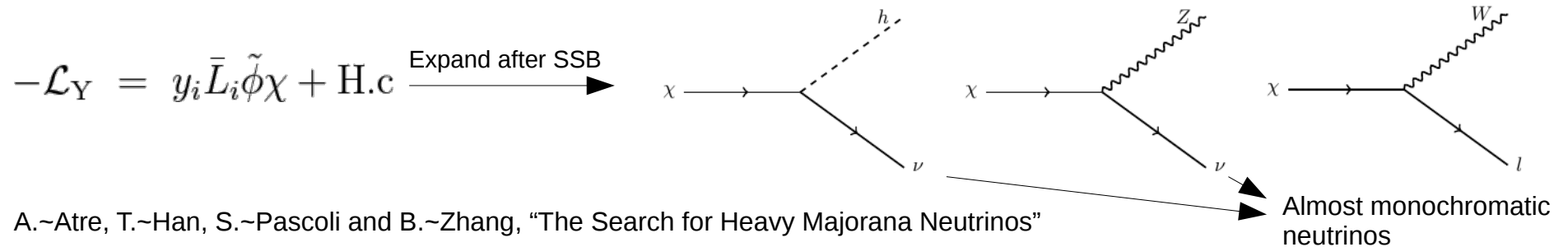
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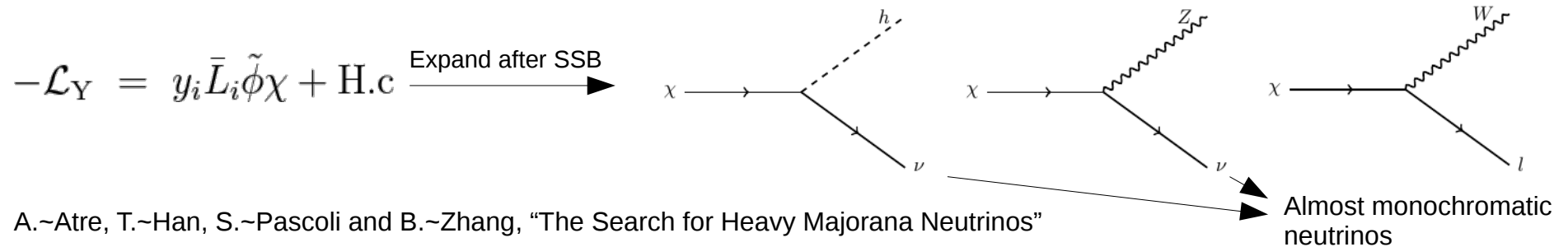
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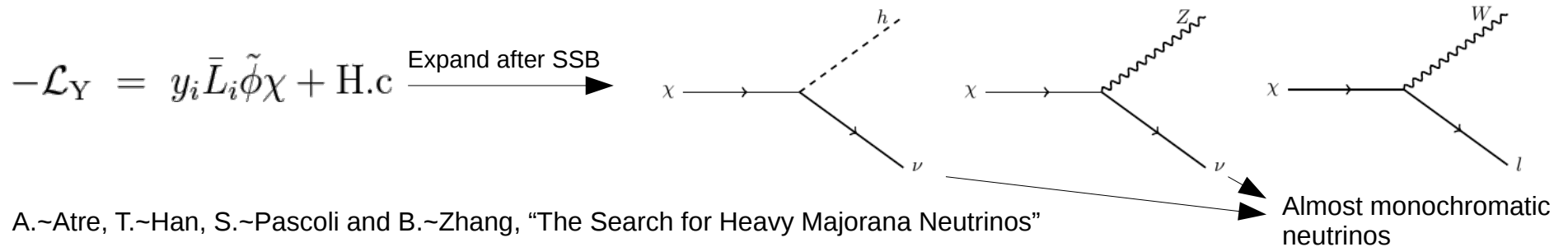
DM decaying process



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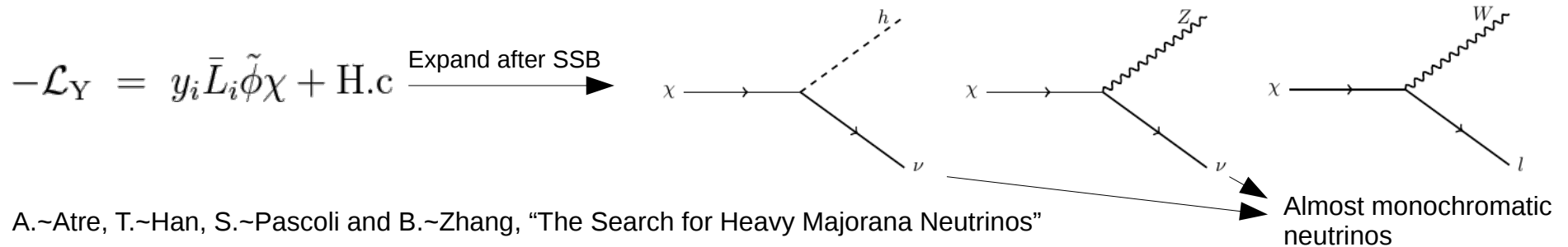


DM decaying process  $\rightarrow$

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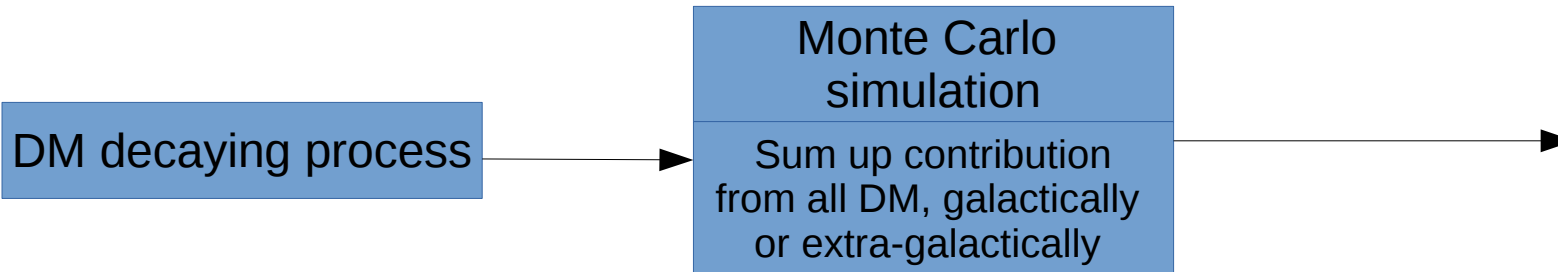
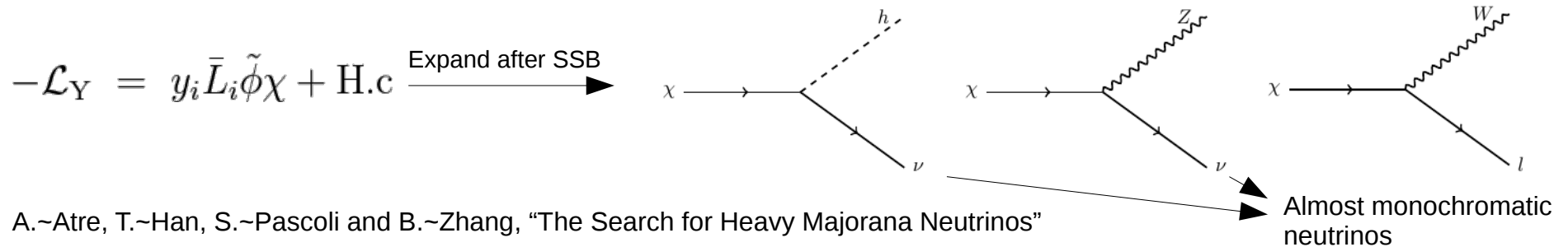
Monte Carlo  
simulation

Sum up contribution  
from all DM, galactically  
or extra-galactically

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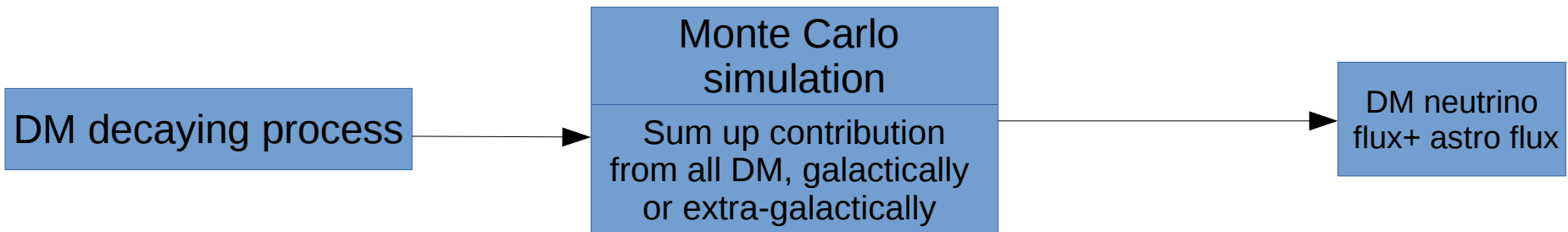
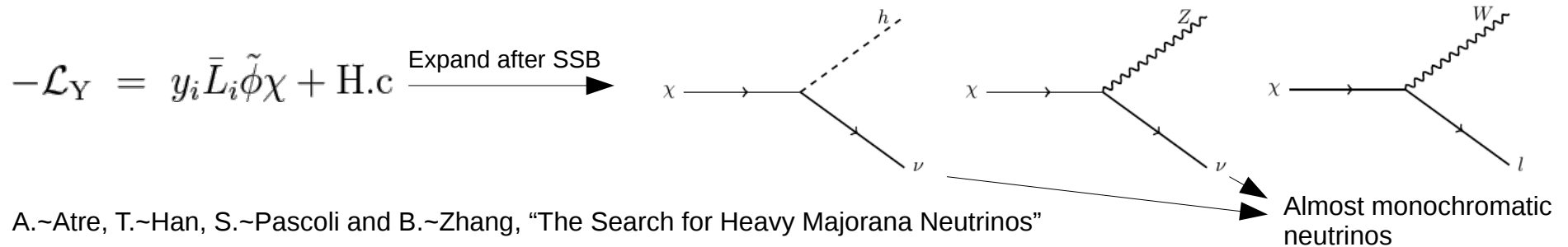
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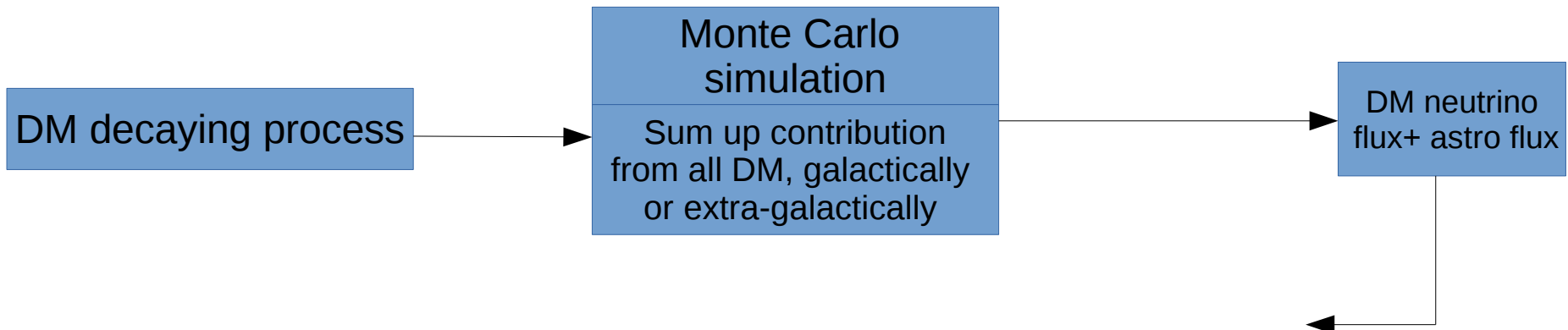
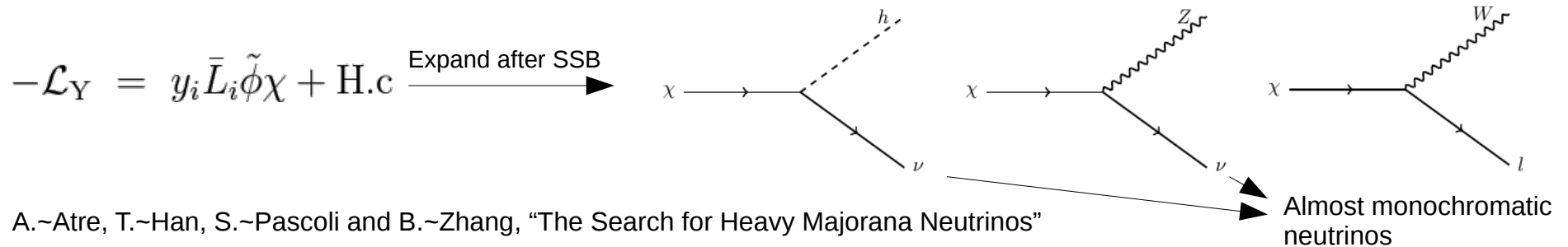
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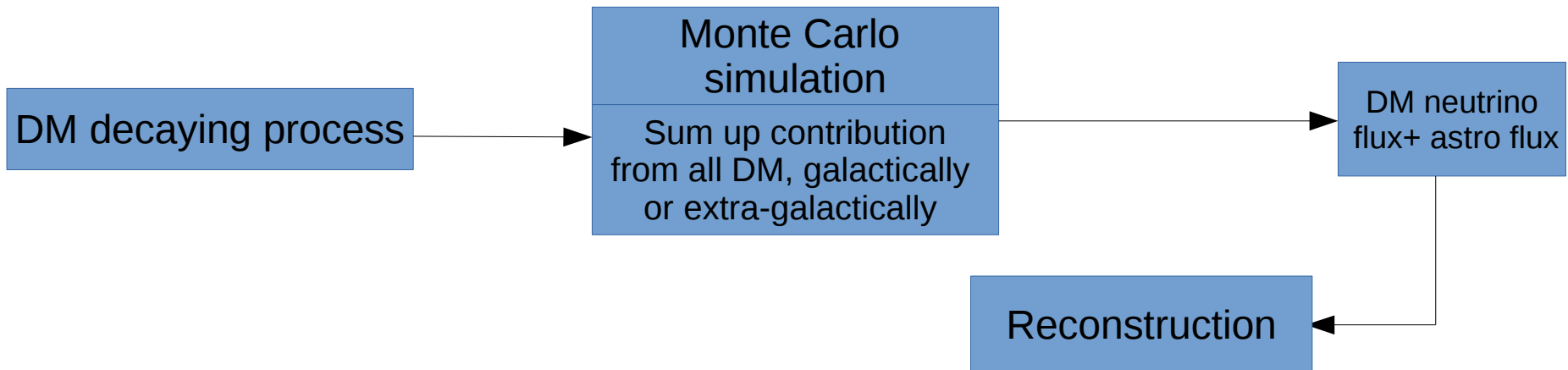
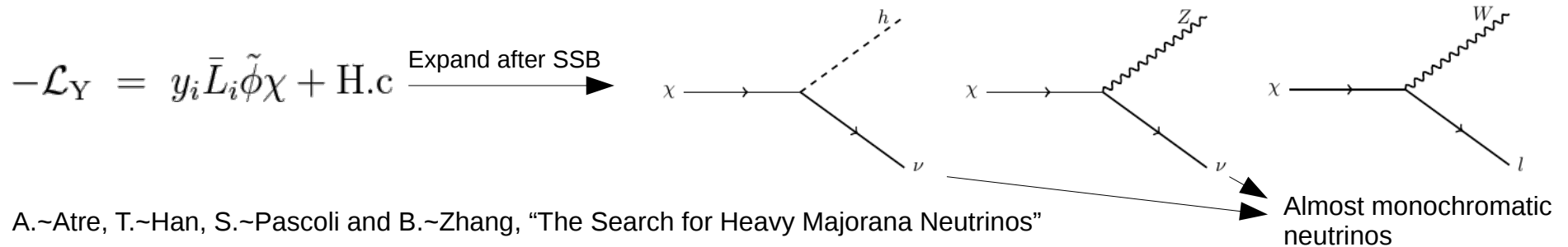
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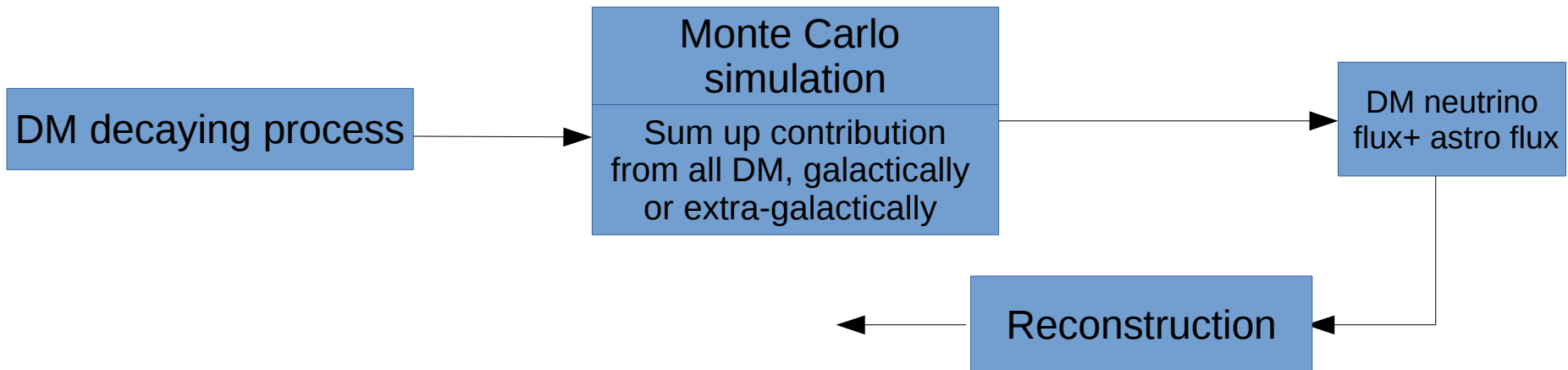
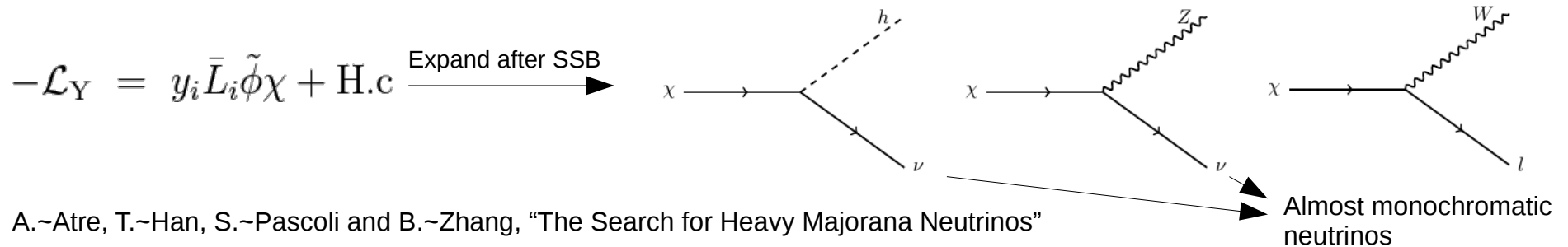
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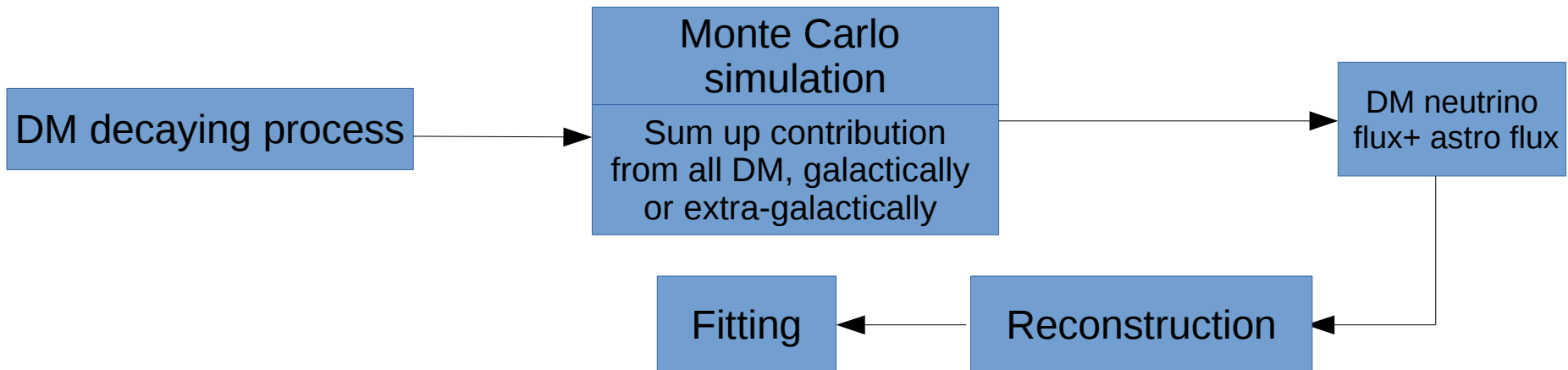
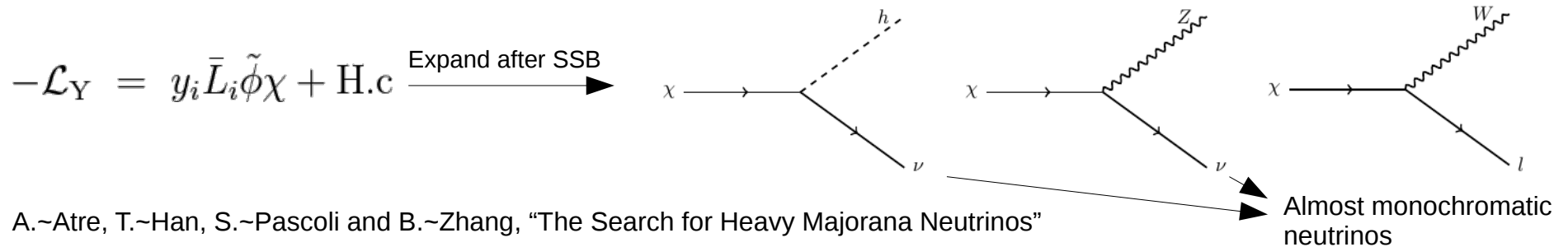
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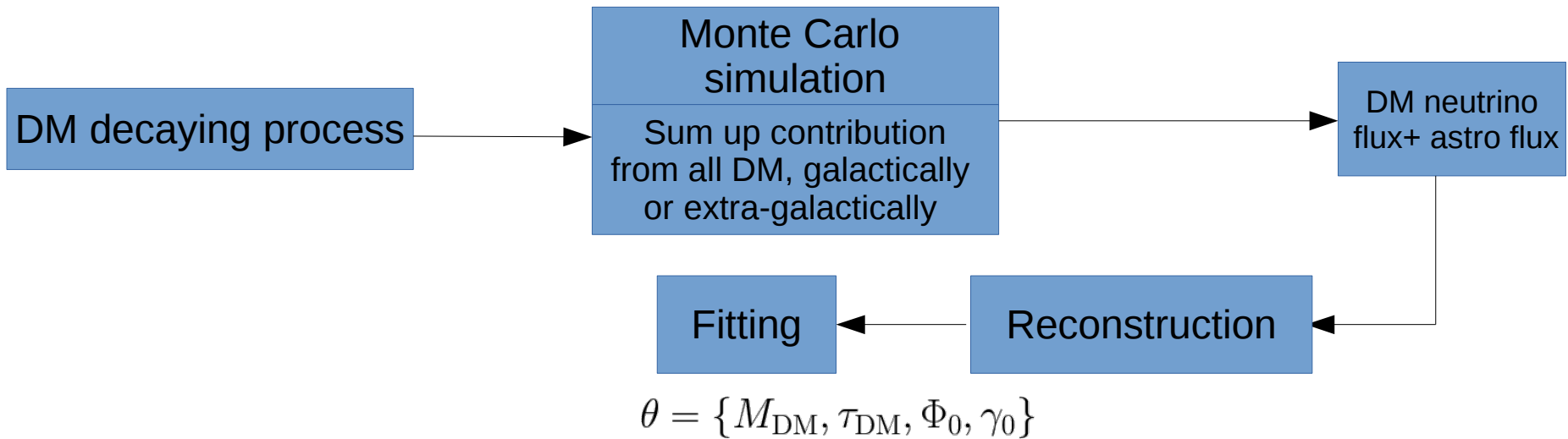
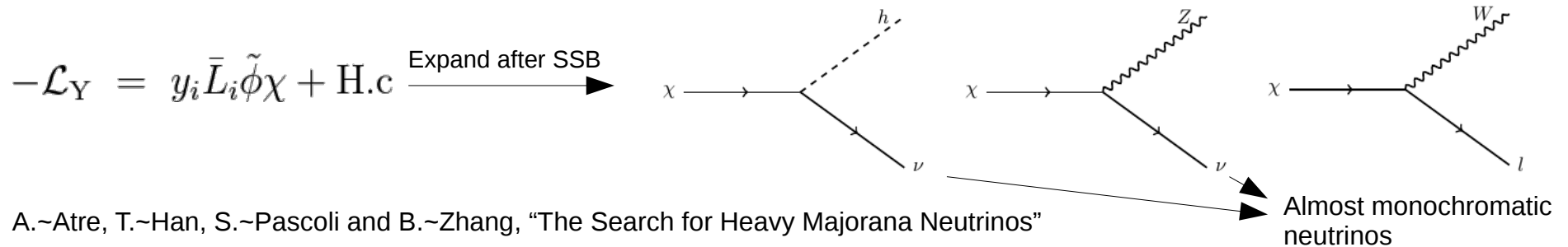




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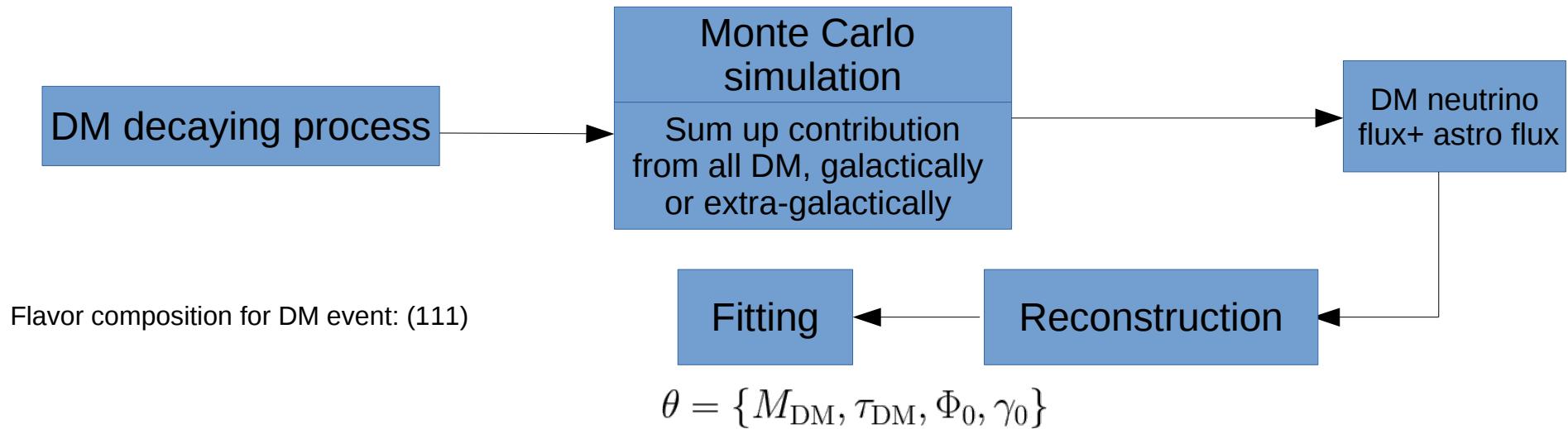
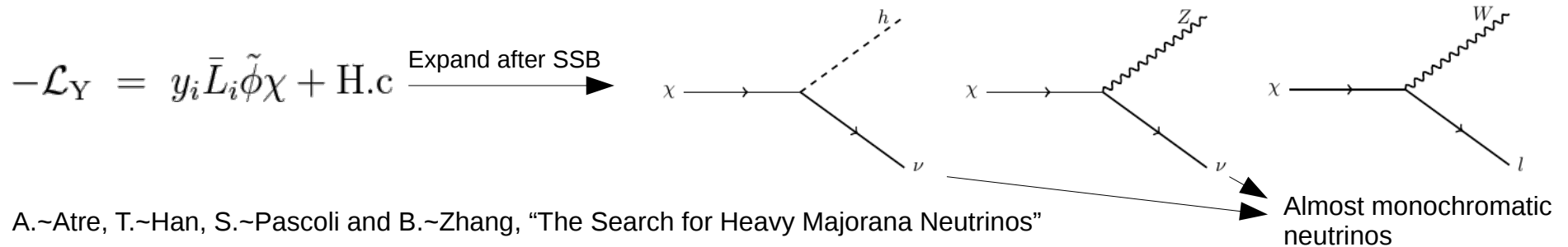
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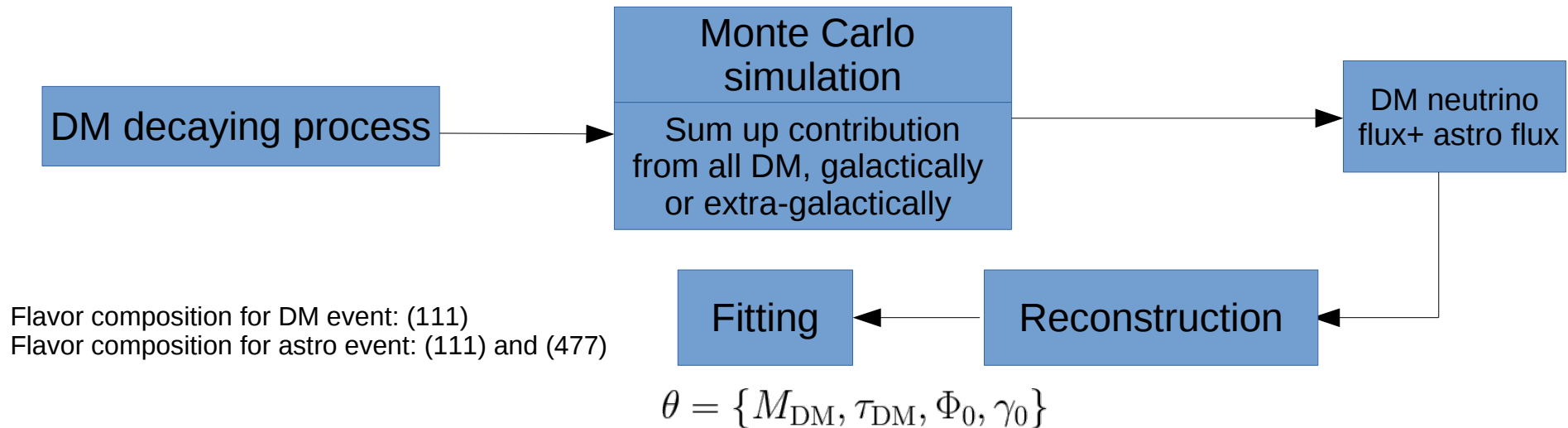
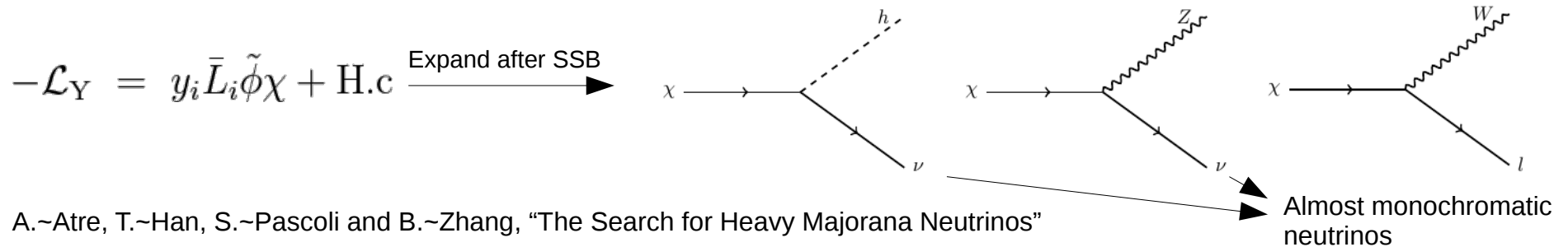
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# Fitting Results

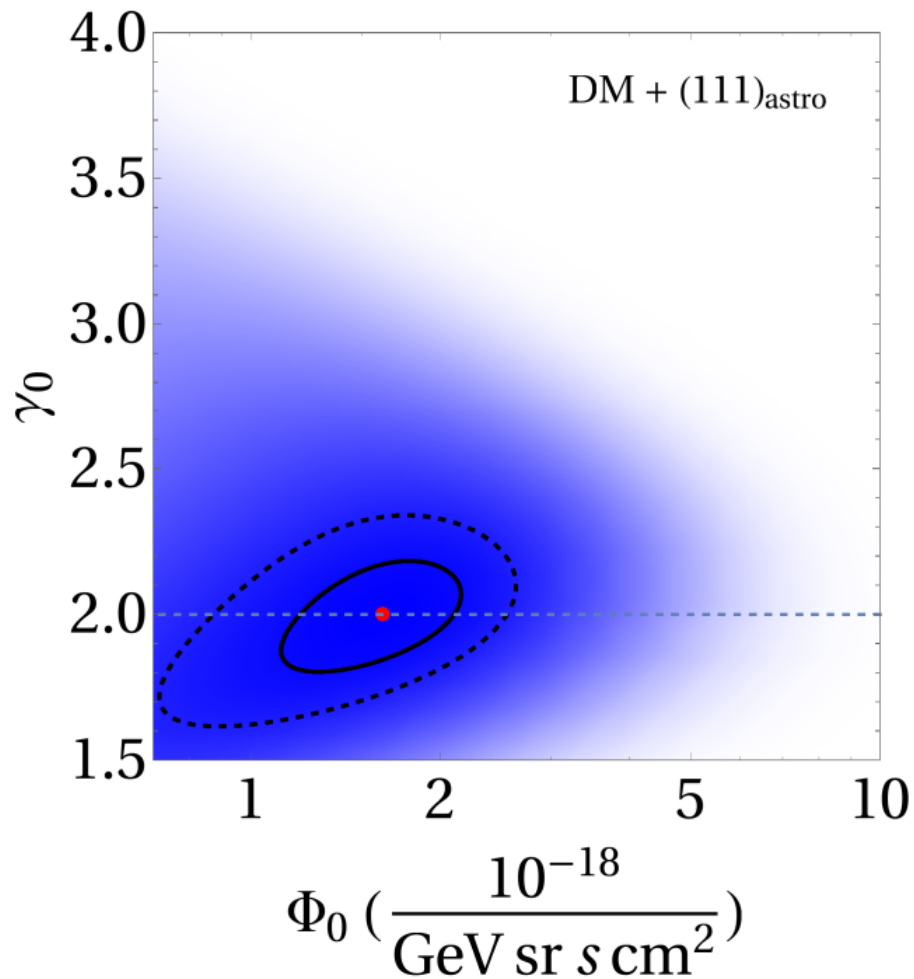
DM (1st comp.)	astro (2nd comp.)	$\Phi_0$	$\gamma_0$	$M_{\text{DM}}$ (TeV)	$\tau_{\text{DM}}(10^{28} \text{ s})$	TS/dof
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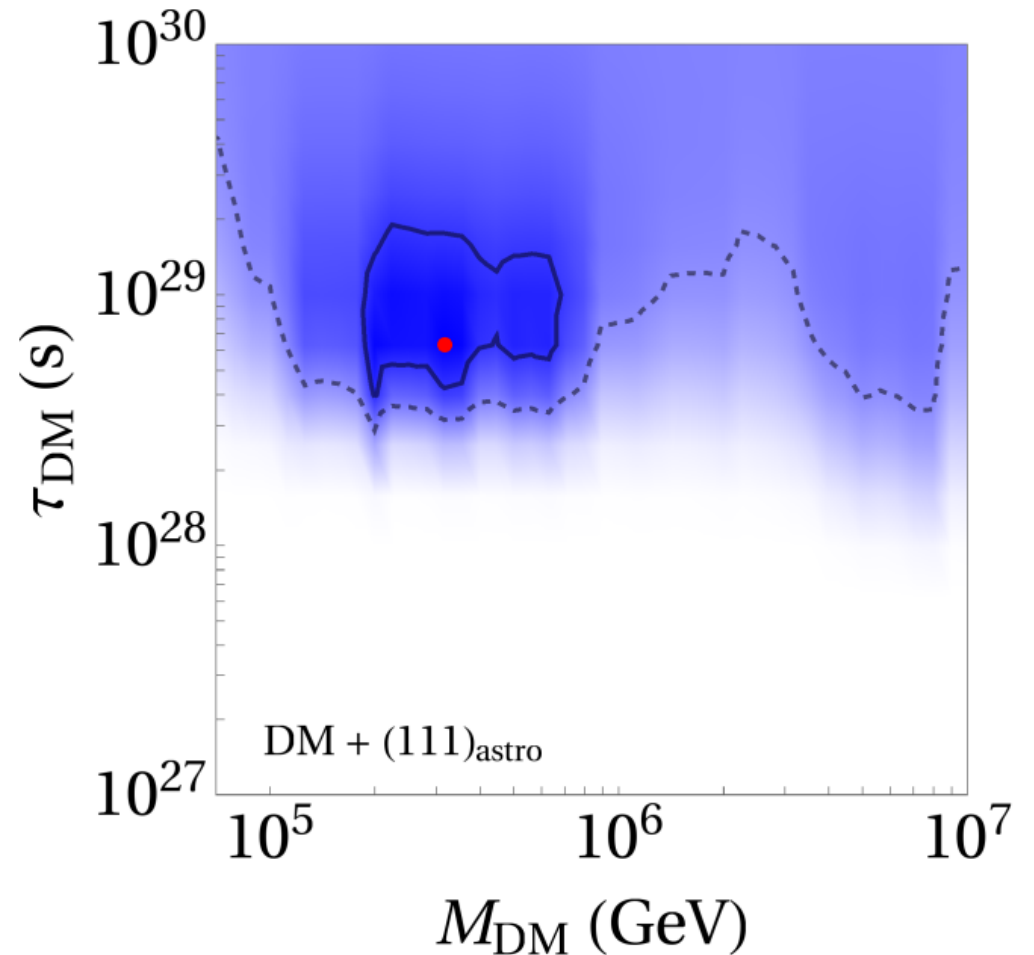
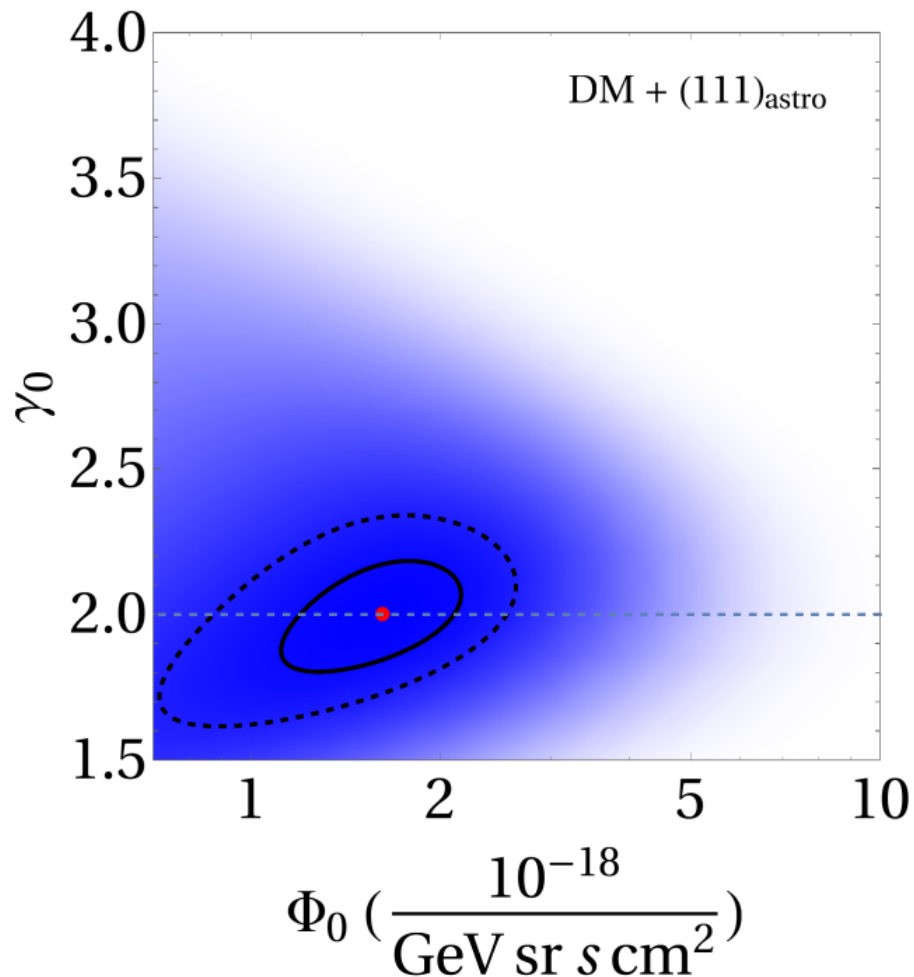
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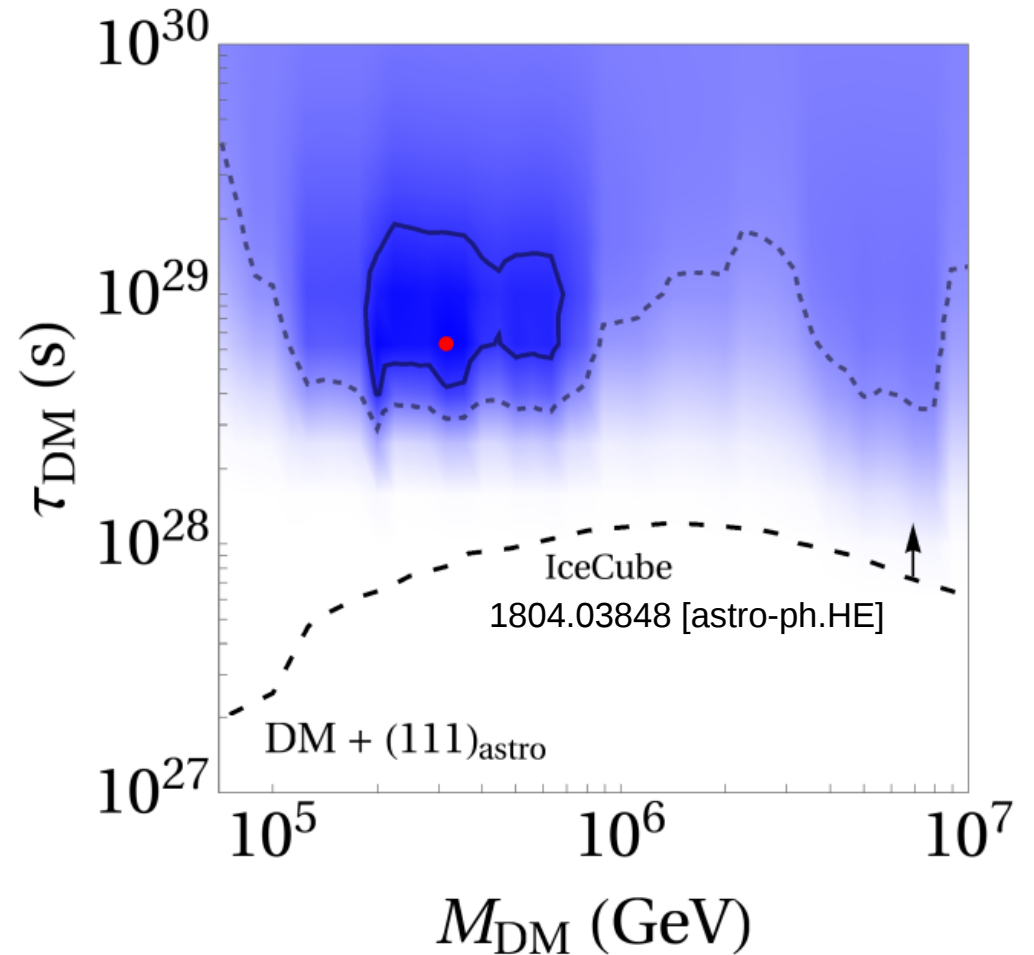
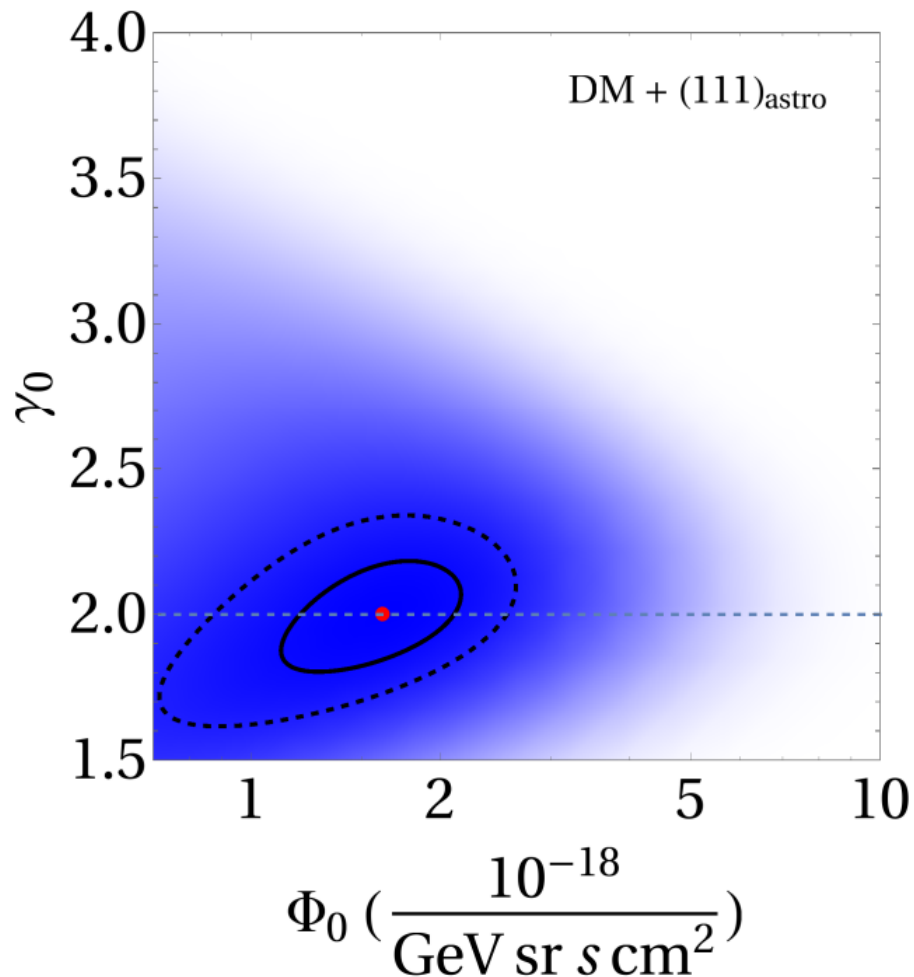
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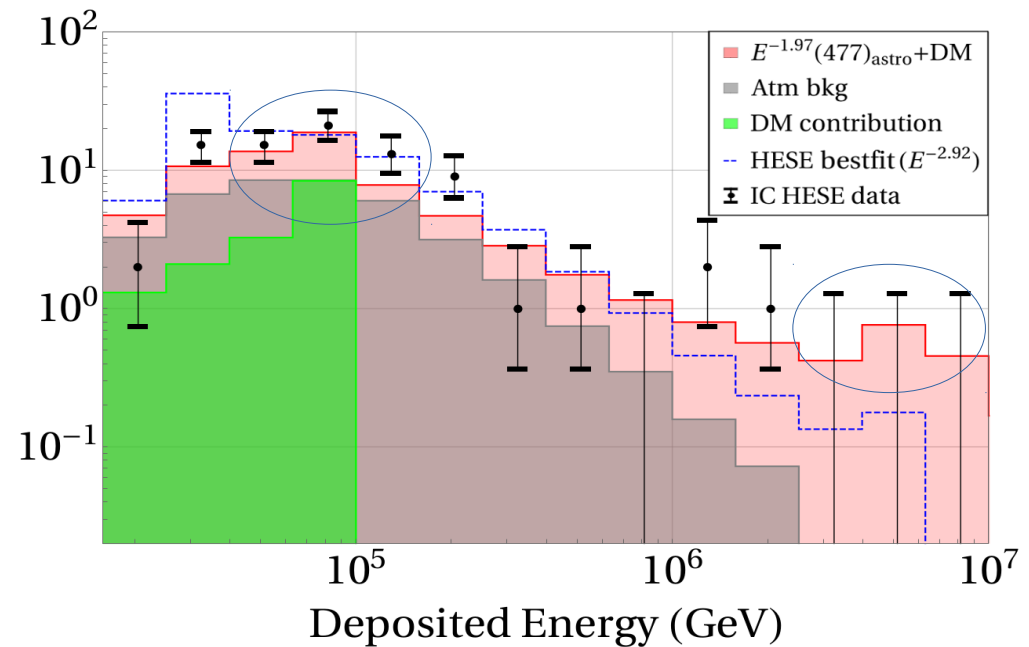
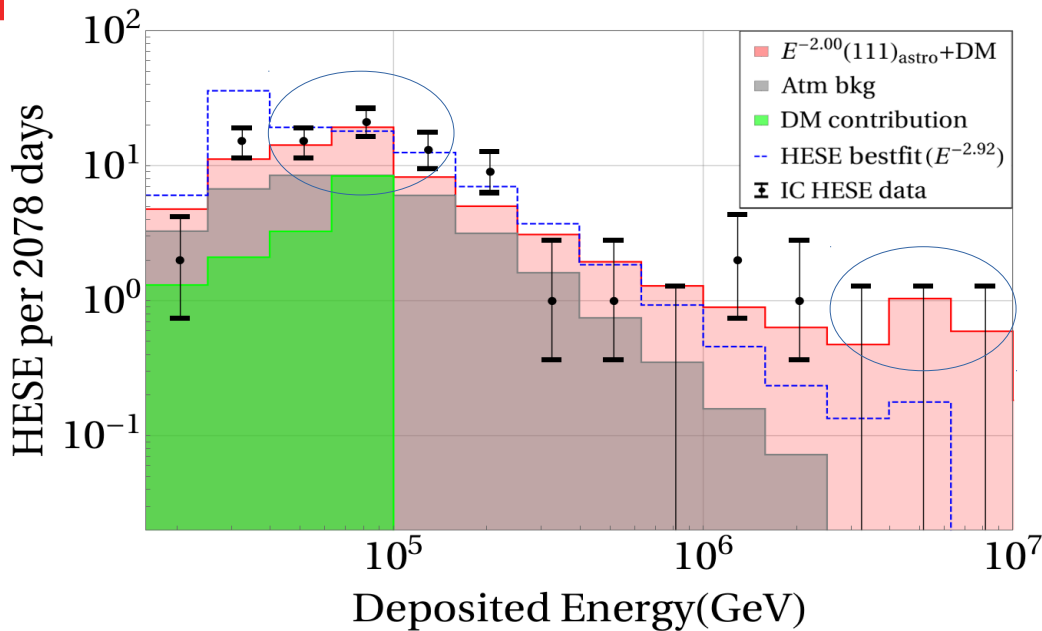
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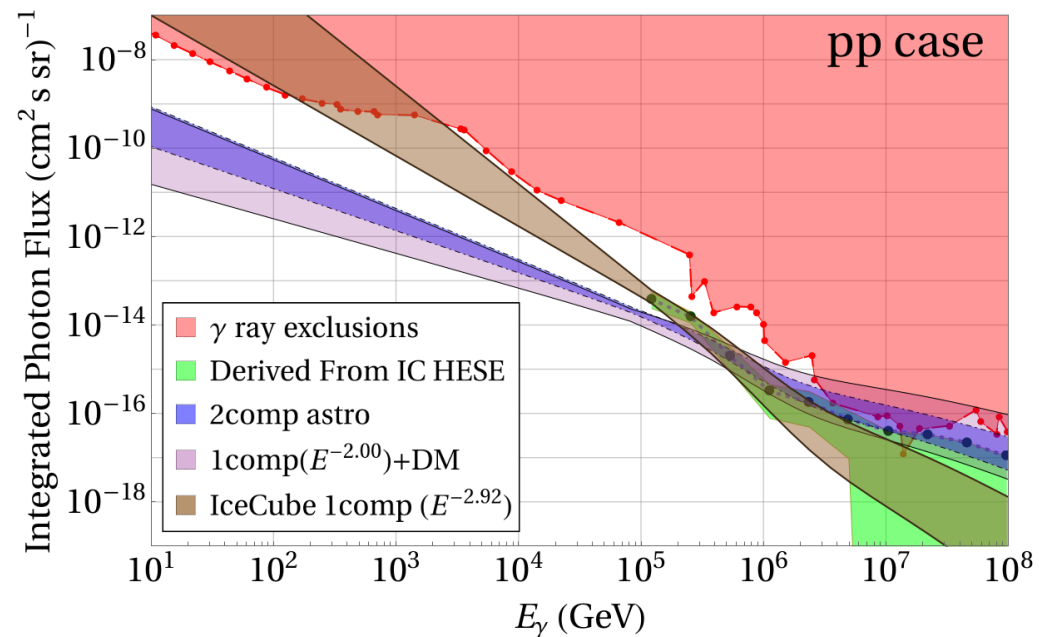
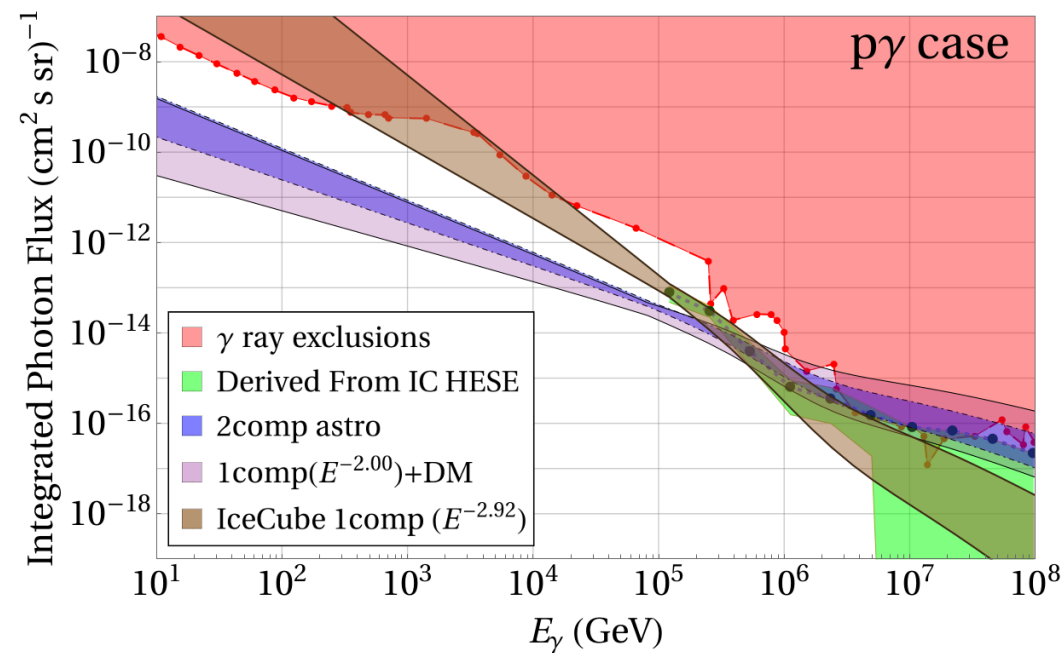
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Estimation of photons flux could be made from neutrino flux

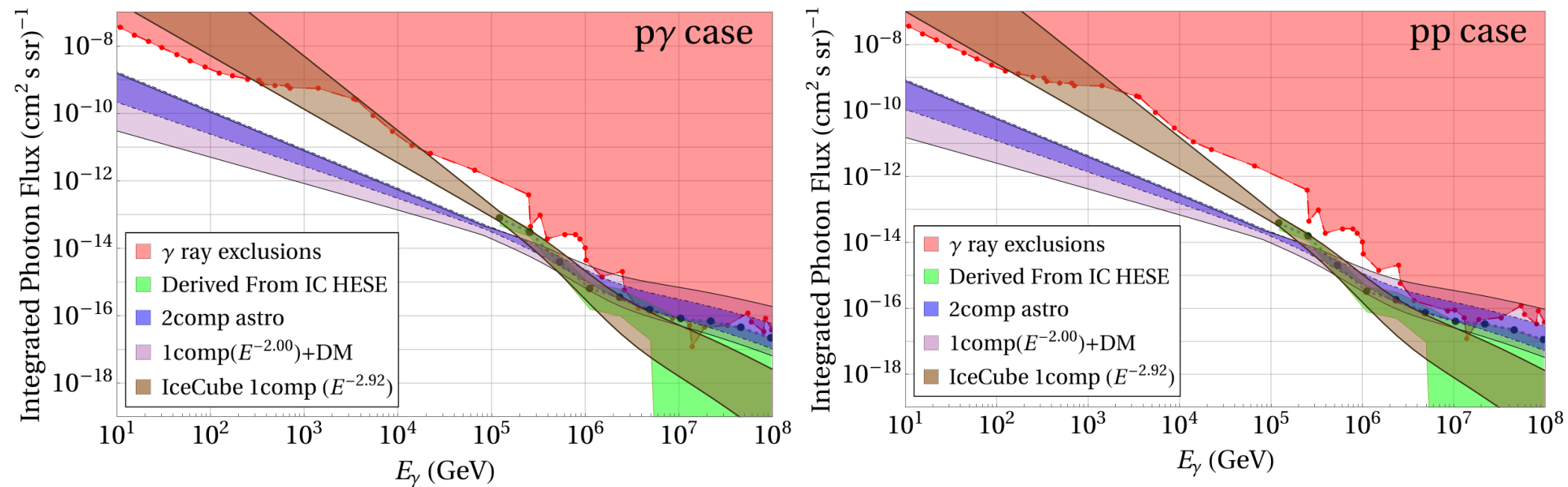
# Verifying Best Fits with Photon Constraint

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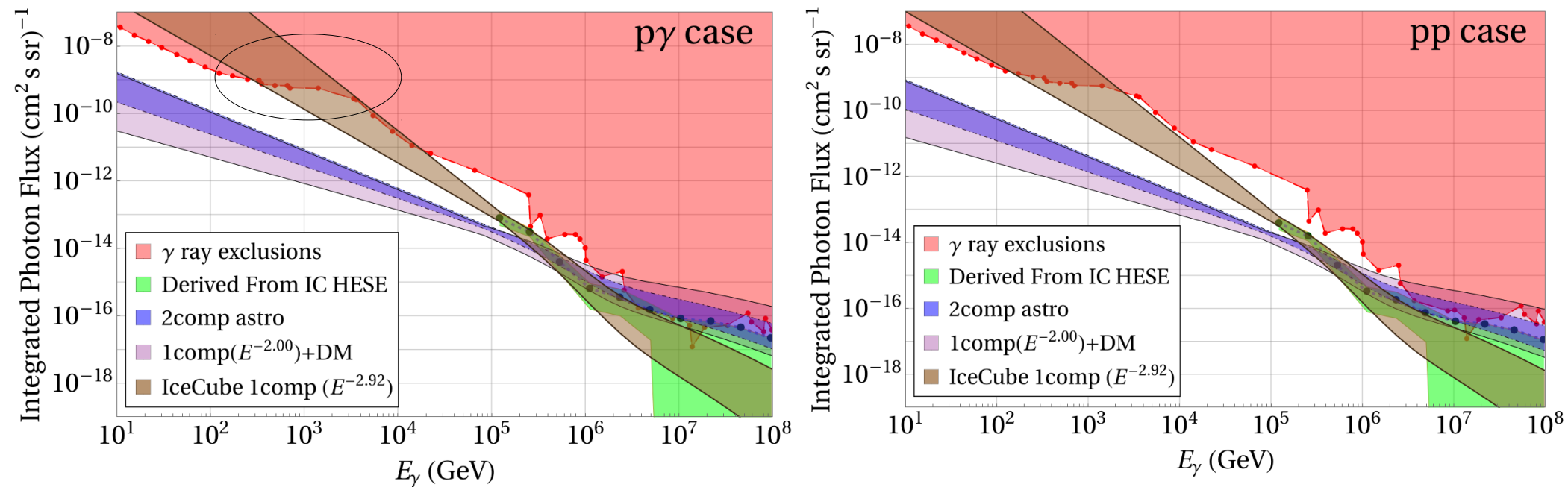
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Comparing the photon estimated flux with gamma ray constraints from CASA-MIA, MILARGO, FERMI-LAT, GRAPES, KASCADE, ARGO, HAWC, HESS and VERITAS:

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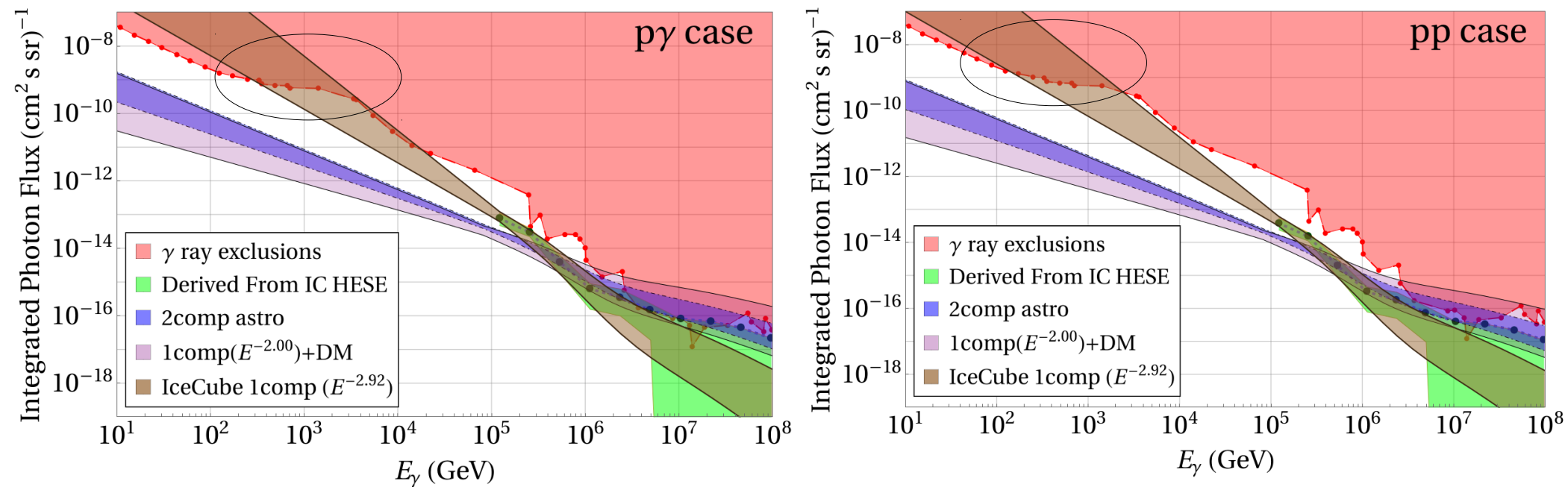
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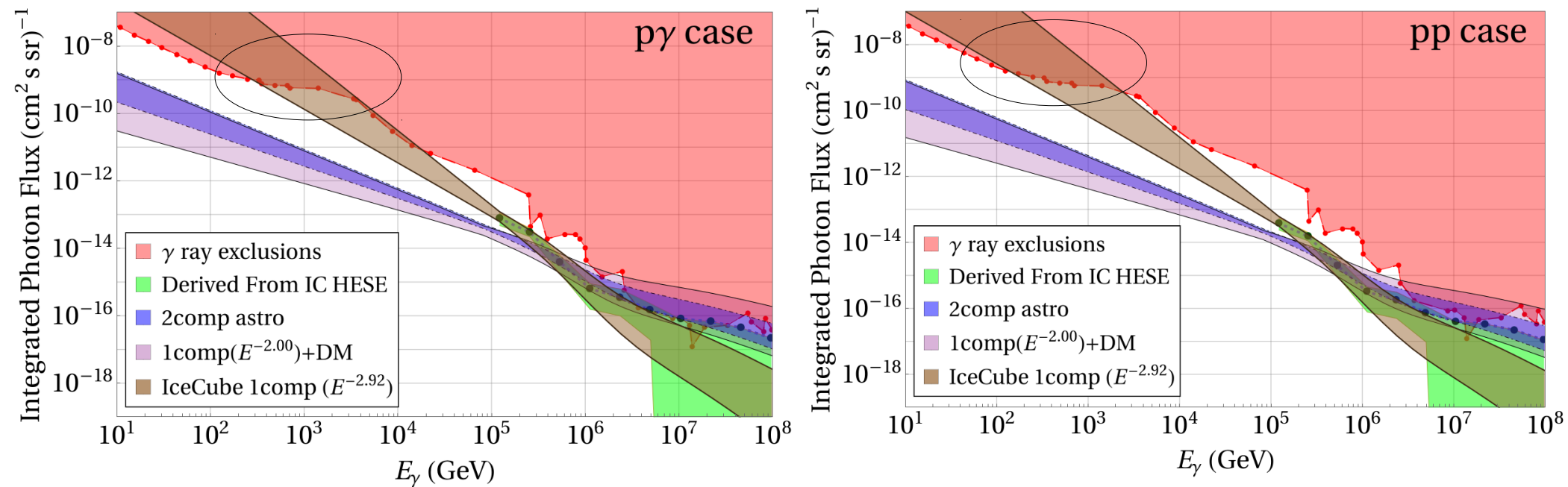
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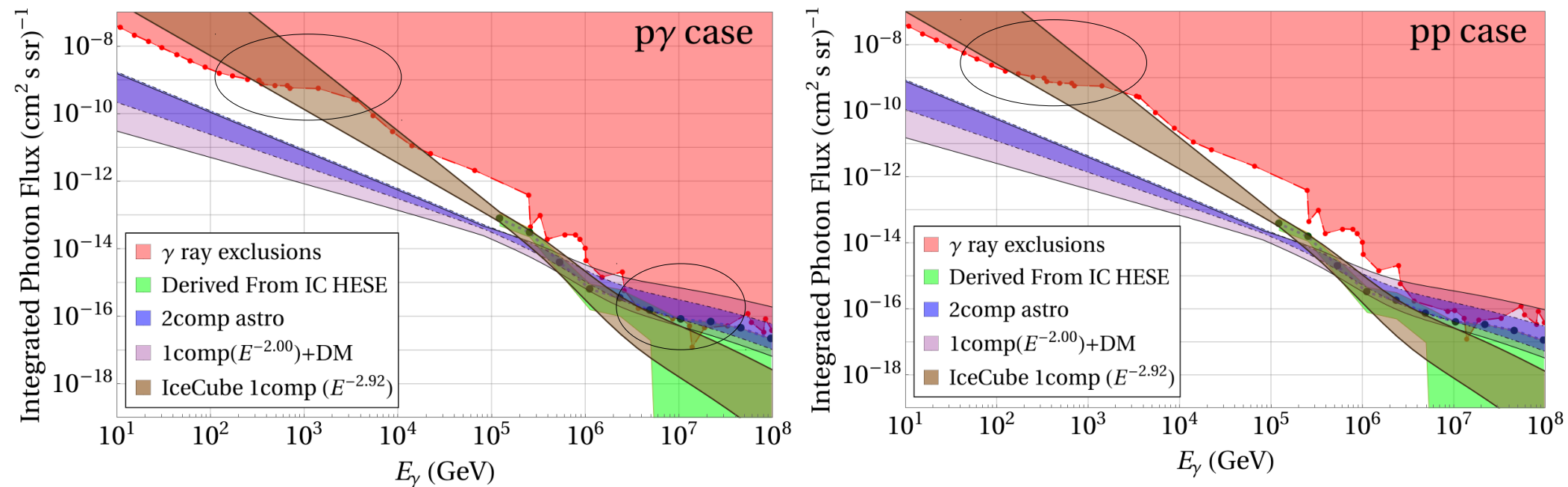


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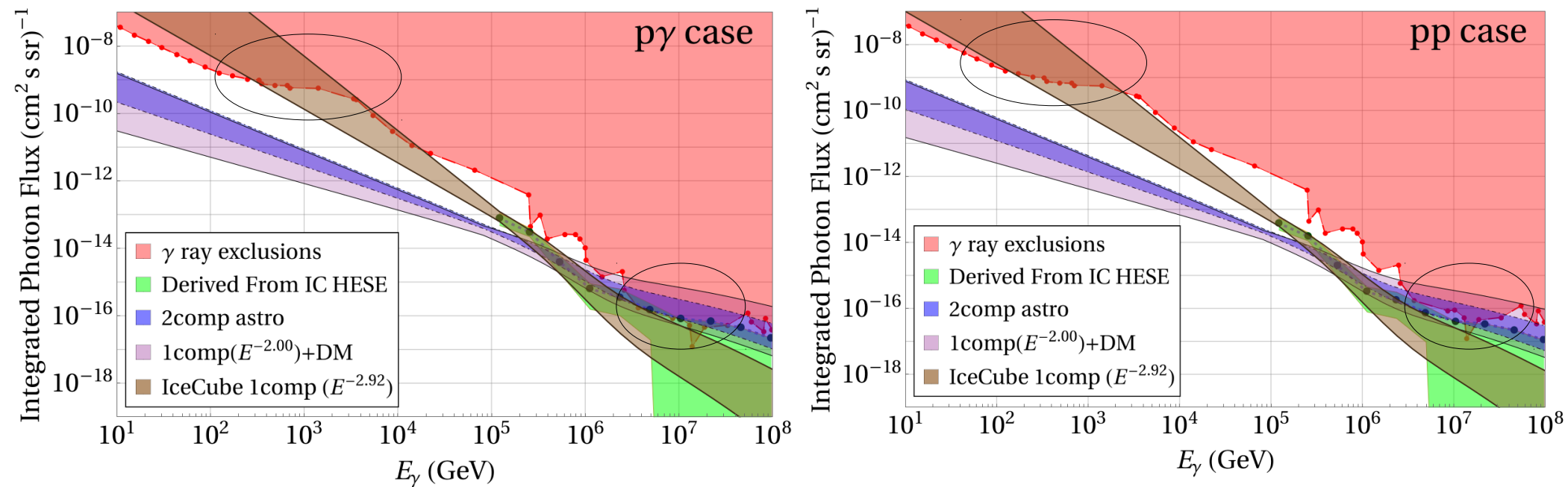
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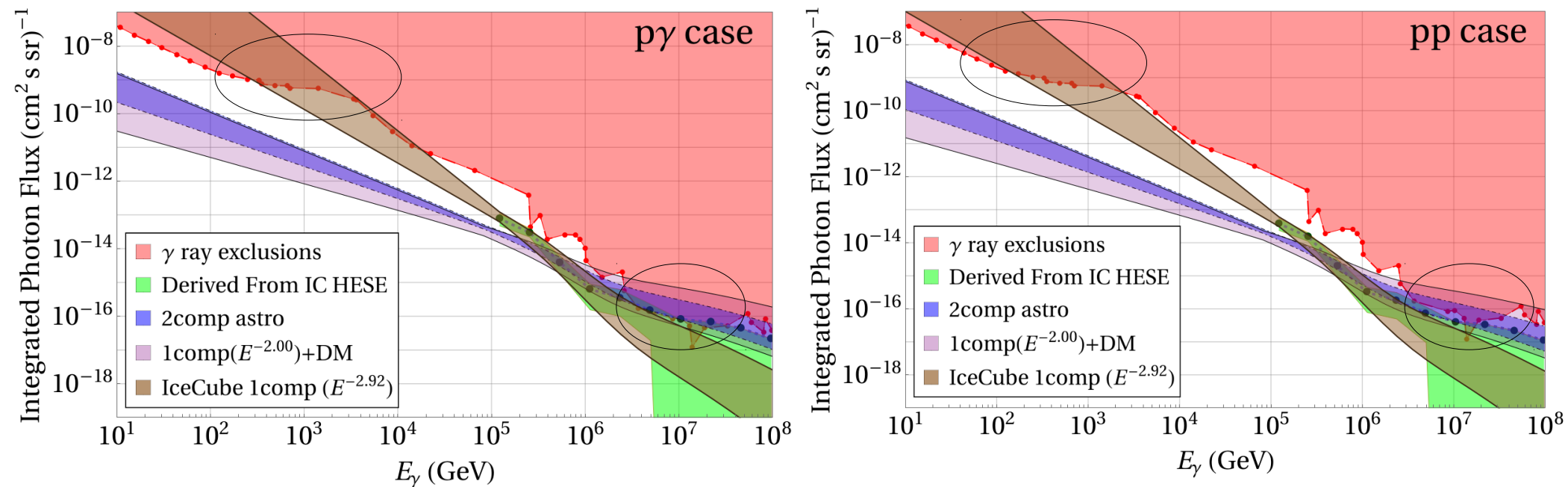


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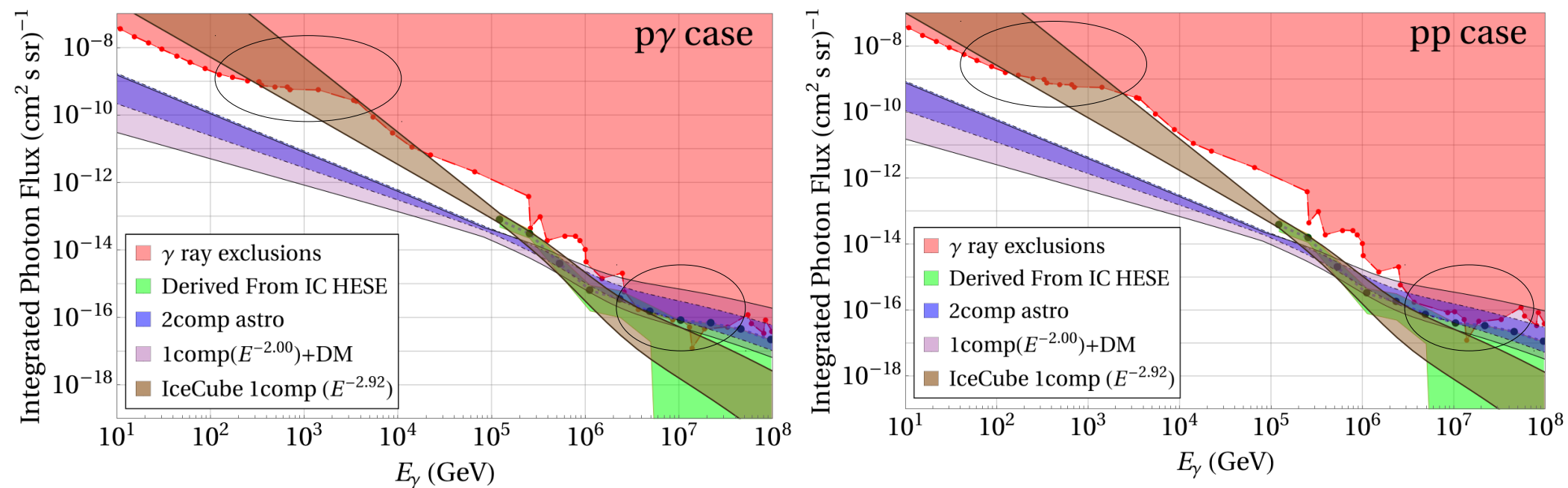


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2. DM+1comp is more favored than 2comp case and, in each cases, (477) case is slightly favored than (111).
3. For DM+1comp, the astrophysical flux index comes out to be 2.
4. Compared with photon constraints, DM+1comp case also has more room to survive

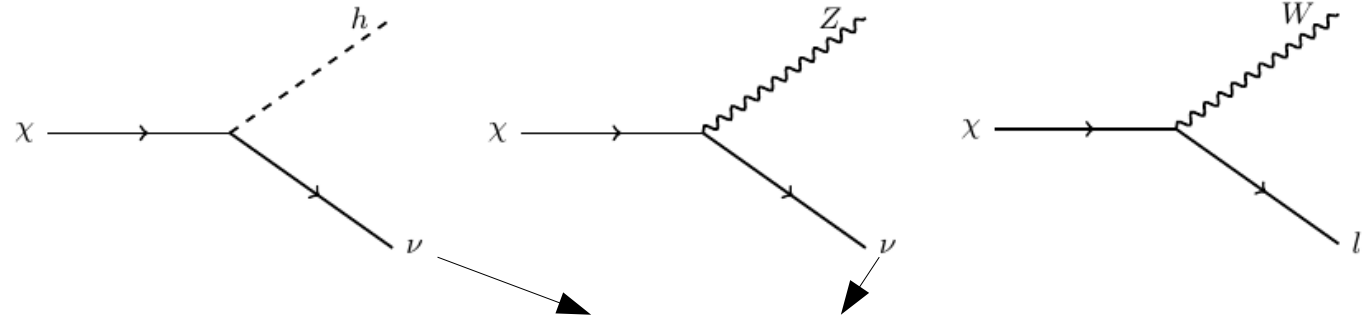


**Thank you!**

# Fermionic Dark Matter Decay

$$-\mathcal{L}_Y = y_i \bar{L}_i \tilde{\phi} \chi + \text{H.c}$$

Expand  
after SSB



Providing almost monochromatic  
neutrinos

$$-\mathcal{L}_{\text{int}} = V_{\ell\chi} \left( \frac{g}{\sqrt{2}} W_{\mu}^{+} \bar{\chi} \gamma^{\mu} P_L \ell^{-} + \frac{g}{2 \cos \theta_w} Z_{\mu} \bar{\chi} \gamma^{\mu} P_L \nu_{\ell} + \frac{g \cdot M_{\text{DM}}}{2 M_W} h \bar{\chi} P_L \nu_{\ell} \right) + \text{H.c.}$$

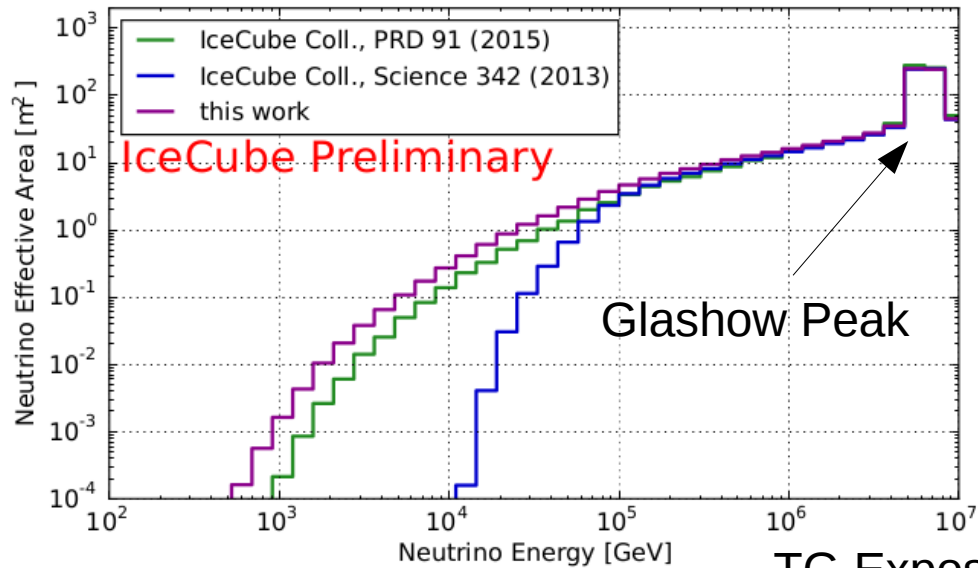
Neutrinos from the decay: Monochromatic parts  $E_{\nu\text{max}} \approx \frac{M_{\text{dm}}}{2}$  + further decay products from h, Z and W

$$\Gamma_{\text{DM}} \simeq \frac{3g^2}{16\pi} |V_{\ell\chi}|^2 \frac{M_{\text{DM}}^3}{M_W^2}$$

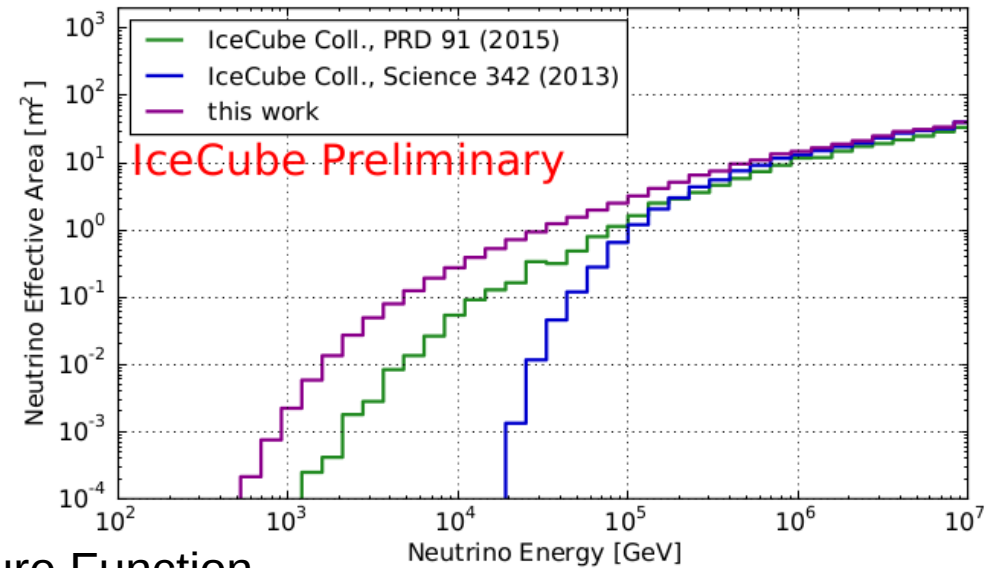
Mixing factors with different flavors, assumed to be the same for all flavors.

# Effective Area and Exposure Function

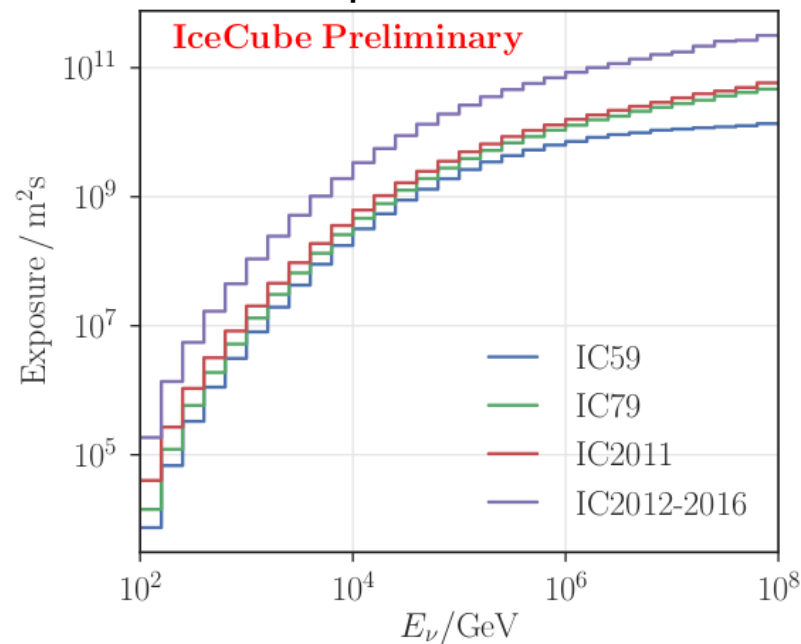
HESE e neutrino effective area



HESE muon neutrino effective area



TG Exposure Function



## 2 Comp Reconstruction

To simulate the IceCube data detecting process for our 2 comp neutrino flux, we need to reconstruct the neutrino flux into events.

$$N_i^{\text{HESE}} = \int d\Omega \int_{E_{i,\min}}^{E_{i,\max}} dE \sum_{\ell=e,\mu,\tau} \Phi_{\nu_\ell}(E) \cdot T \cdot A_{\nu_\ell}(E, \Omega)$$
$$N_i^{\text{TG}} = \int d\Omega \int_{E_{i,\min}}^{E_{i,\max}} dE \sum_{\ell=e,\mu,\tau} \Phi_{\nu_\ell}(E) \cdot F_{\nu_\ell}(E, \Omega)$$

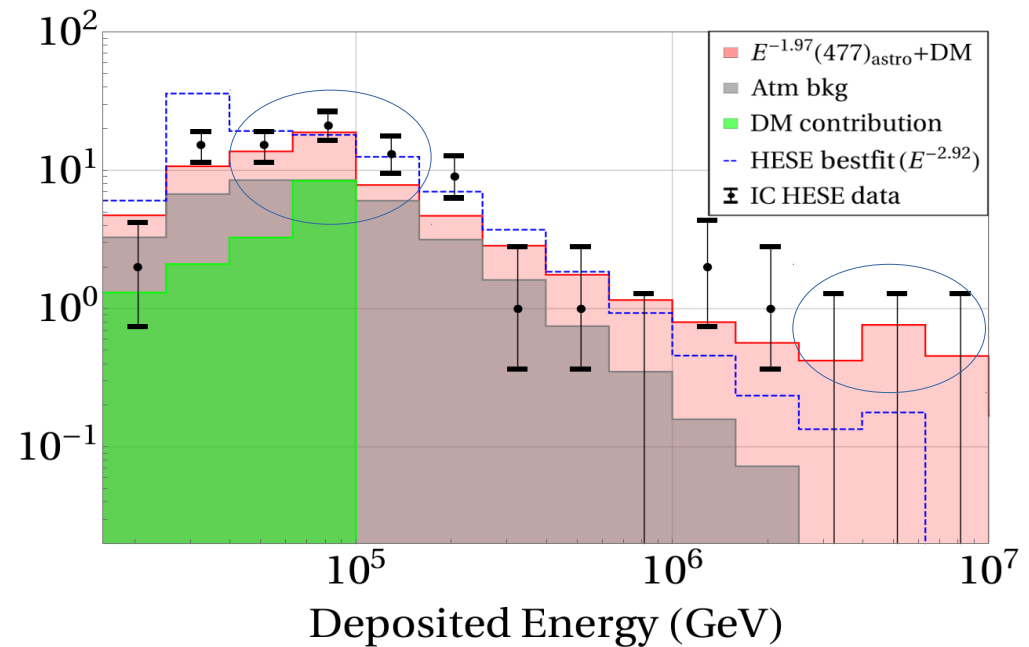
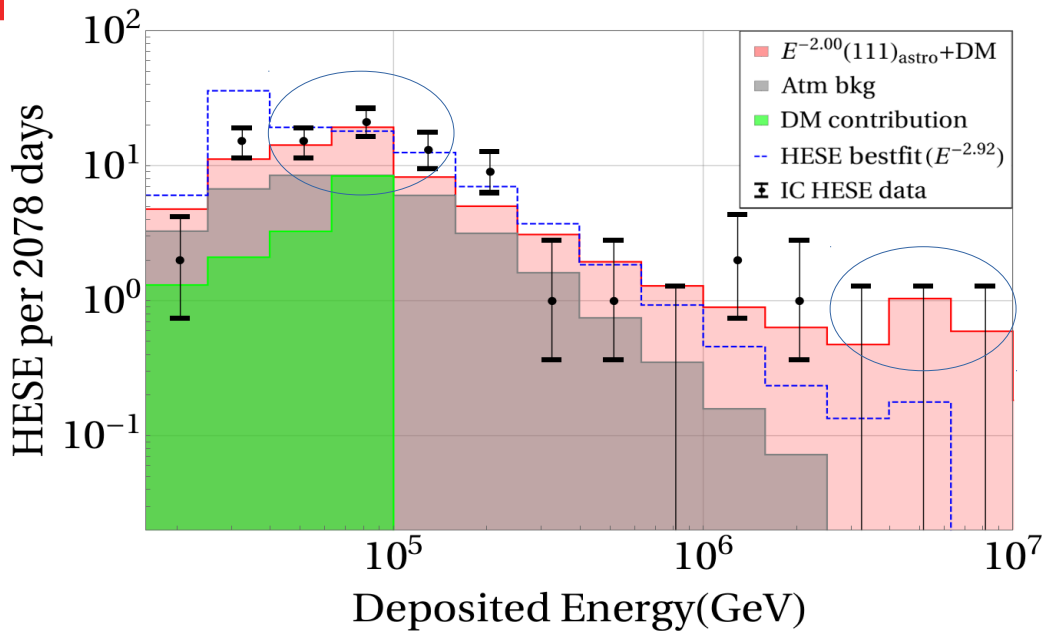
Decided by IceCube detector's configuration and run time

$A_{\nu_\ell}(E, \Omega)$  : HESE effective area, sum of cross sections for all the particles in the detector, an effective total cross section

$F_{\nu_\ell}(E, \Omega)$  : TG effective exposure function, effective area multiplied by time T

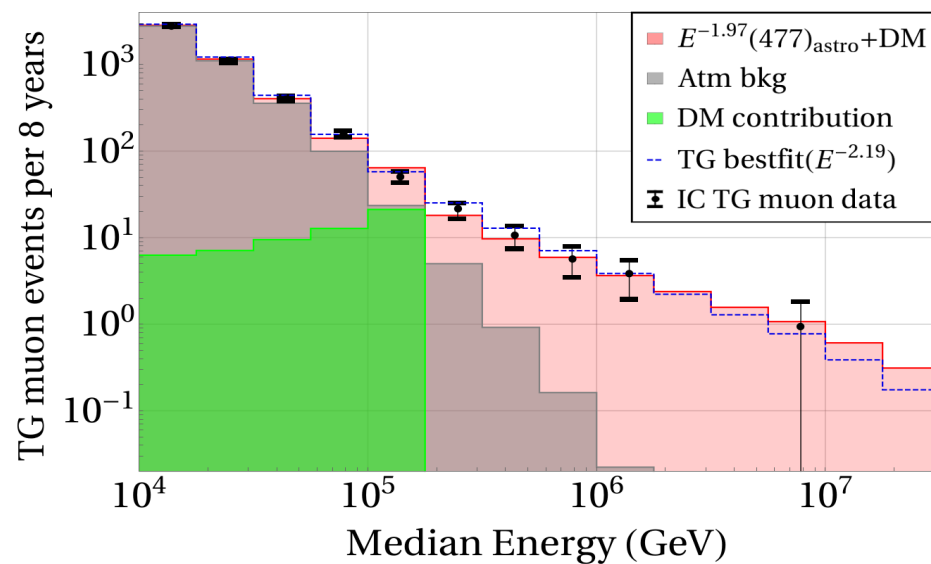
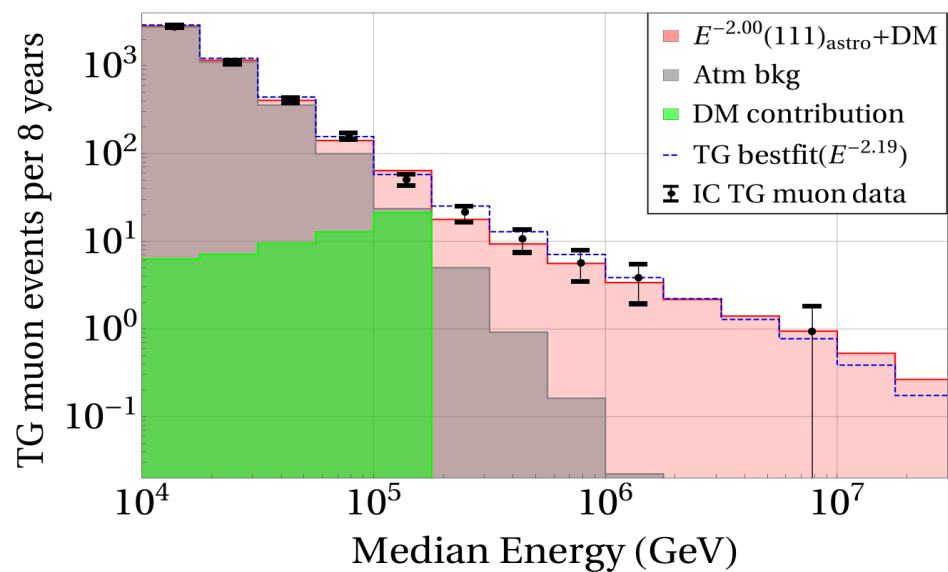
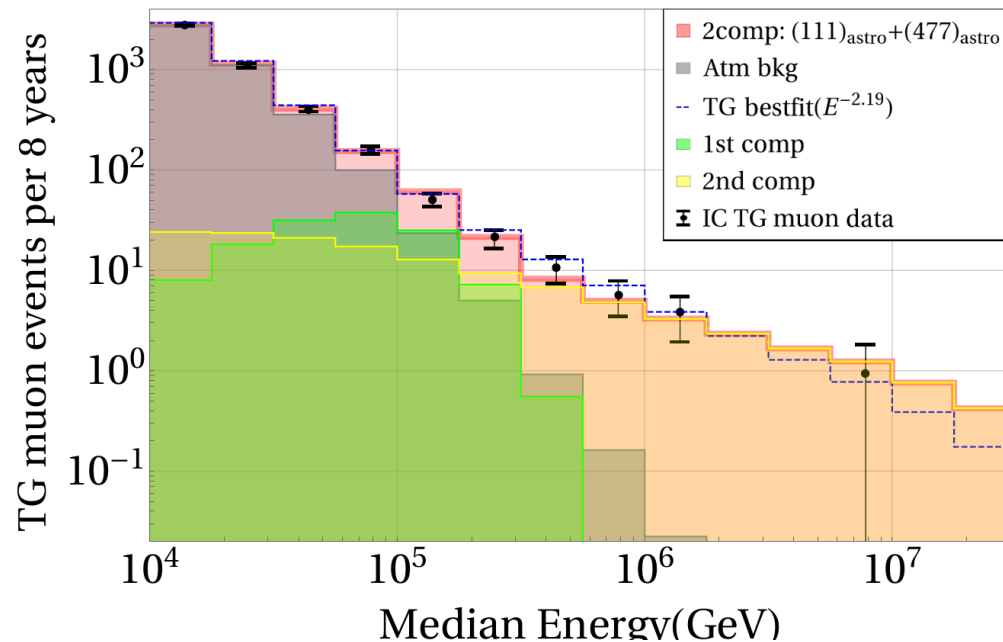
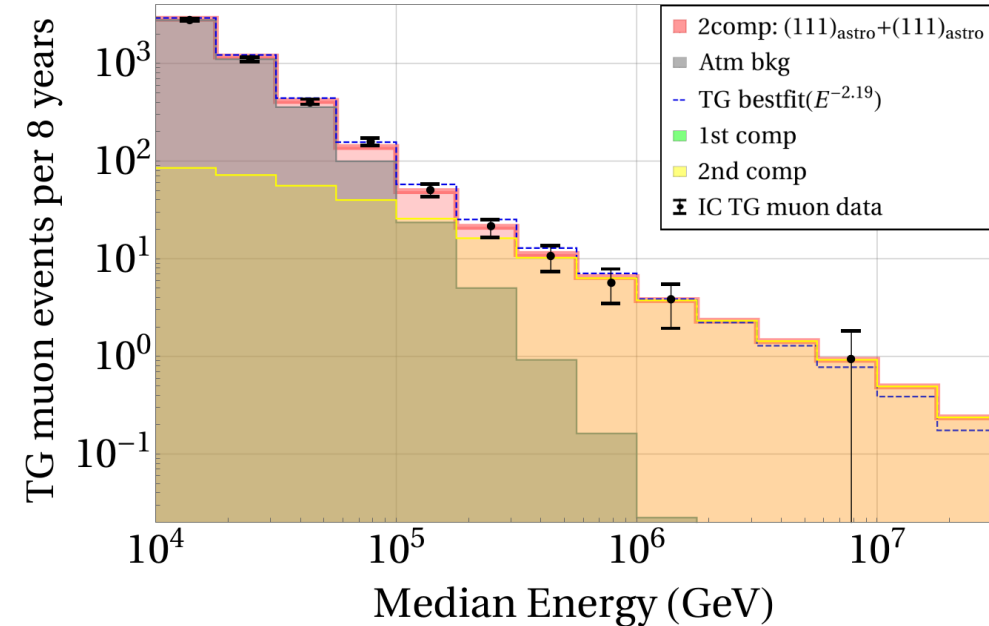
E for HESE is the deposited energy while E for TG is the median energy. Both are different but connected to real neutrino energy.

# Best Fit Event Spectrum



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# TG Plots





# Neutrino Compositions At Source

	pp	pγ
Typical	$\nu_e : \nu_\mu : \nu_\tau : \bar{\nu}_e : \bar{\nu}_\mu : \bar{\nu}_\tau$ $= \left( \frac{1}{6} : \frac{1}{3} : 0 : \frac{1}{6} : \frac{1}{3} : 0 \right)$	$\nu_e : \nu_\mu : \nu_\tau : \bar{\nu}_e : \bar{\nu}_\mu : \bar{\nu}_\tau$ $= \left( \frac{1}{3} : \frac{1}{3} : 0 : 0 : \frac{1}{3} : 0 \right)$
μ damped	$\nu_e : \nu_\mu : \nu_\tau : \bar{\nu}_e : \bar{\nu}_\mu : \bar{\nu}_\tau$ $= \left( 0 : \frac{1}{2} : 0 : 0 : \frac{1}{2} : 0 \right)$	$\nu_e : \nu_\mu : \nu_\tau : \bar{\nu}_e : \bar{\nu}_\mu : \bar{\nu}_\tau$ $= (0 : 1 : 0 : 0 : 0 : 0)$

But, these are the ratios at source !!!

consider  $f_e : f_\mu : f_\tau \equiv (\nu_e + \bar{\nu}_e) : (\nu_\mu + \bar{\nu}_\mu) : (\nu_\tau + \bar{\nu}_\tau)$

$$\begin{pmatrix} f_e \\ f_\mu \\ f_\tau \end{pmatrix}_{\oplus} = \frac{1}{18} \begin{pmatrix} 10 & 4 & 4 \\ 4 & 7 & 7 \\ 4 & 7 & 7 \end{pmatrix} \begin{pmatrix} f_e \\ f_\mu \\ f_\tau \end{pmatrix}_s$$

Assuming TBM Mixing, taking oscillation into account

	pp	pγ
Typical	(1 : 1 : 1)	(1 : 1 : 1)
μ damped	(4 : 7 : 7)	(4 : 7 : 7)

# Propagation of Neutrinos in Vacuum

$$|\nu_\alpha\rangle = \sum_k U_{\alpha k}^* |\nu_k\rangle$$

PMNS Matrix, Similar to CKM matrix in quark mixing

$$|\nu_\alpha(L, T)\rangle = \sum_\beta \left( \sum_{k=1}^3 U_{\alpha k}^* e^{-iE_k T + i p_k L} U_{\beta k} \right) |\nu_\beta\rangle$$

$$P_{\nu_\alpha \rightarrow \nu_\beta}(L) = \sum_k |U_{\alpha k}|^2 |U_{\beta k}|^2 + 2 \operatorname{Re} \sum_{k>j} U_{\alpha k}^* U_{\beta k} U_{\alpha j} U_{\beta j}^* \exp \left( -i \frac{\Delta m_{kj}^2 L}{2E} \right)$$

Averaged out for large L

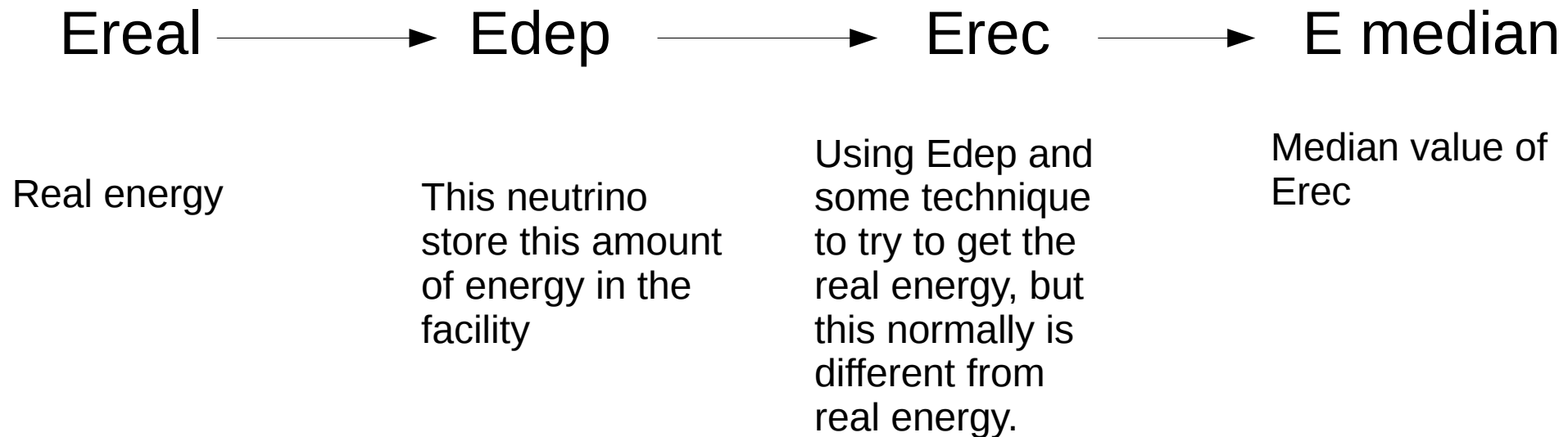
consider  $f_e : f_\mu : f_\tau \equiv (\nu_e + \bar{\nu}_e) : (\nu_\mu + \bar{\nu}_\mu) : (\nu_\tau + \bar{\nu}_\tau)$

$$\begin{pmatrix} f_e \\ f_\mu \\ f_\tau \end{pmatrix}_\oplus = \frac{1}{18} \begin{pmatrix} 10 & 4 & 4 \\ 4 & 7 & 7 \\ 4 & 7 & 7 \end{pmatrix} \begin{pmatrix} f_e \\ f_\mu \\ f_\tau \end{pmatrix}_s$$

Assuming TBM Mixing

	pp	py
Typical	(1 : 1 : 1)	(1 : 1 : 1)
μ damped	(4 : 7 : 7)	(4 : 7 : 7)

# Relation Between Ereal, Edep and Emedian



E real typically is linear to Edep and Erec. But for track, Erec could be very uncertain since the deposited energy for tracks are typically far less than real energy, so relation between E real and Erec is more of an estimation. Thus E real and Emedian's relation is also a rough estimation

# Constraints From H.E.S.S.?

At around TeV level, the constraints from H.E.S.S. is around  $10^{-5} E^2 \cdot \phi$ , while the constraints we have from Fermi LAT and HAWC is around  $10^{-6}$  to  $10^{-7}$ , a better lower constraint than H.E.S.S.

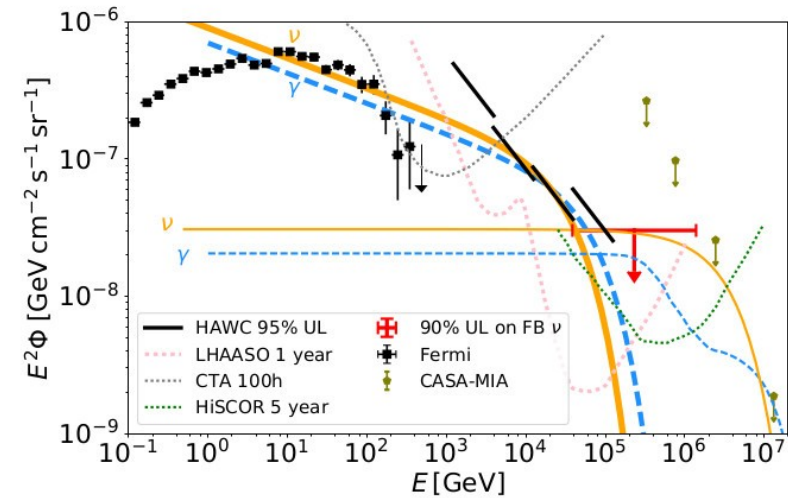
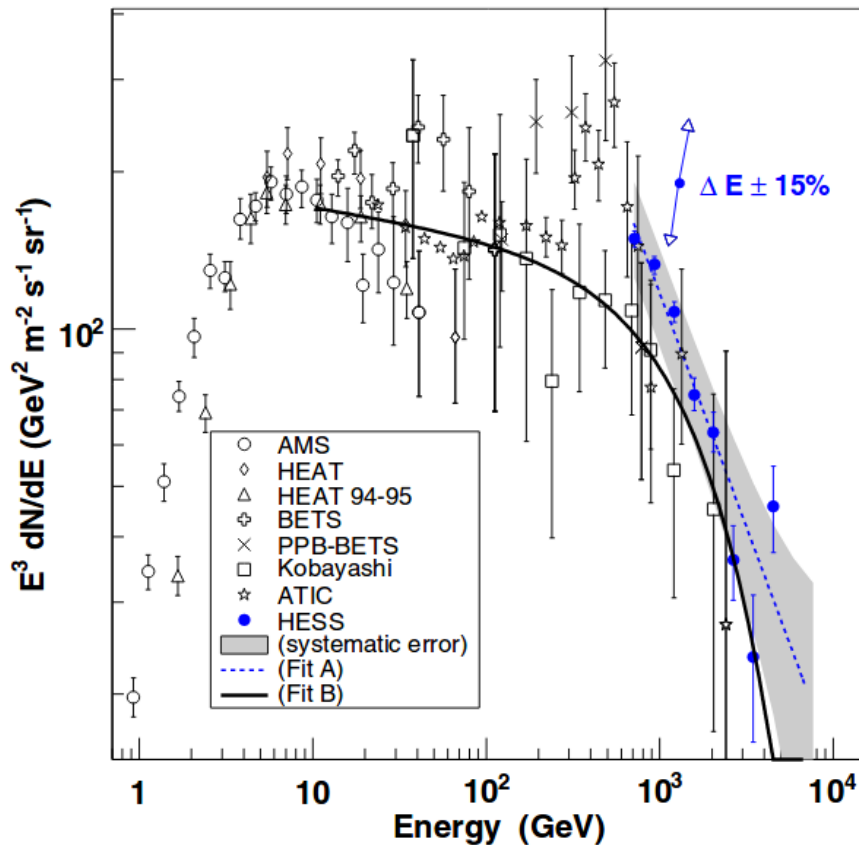
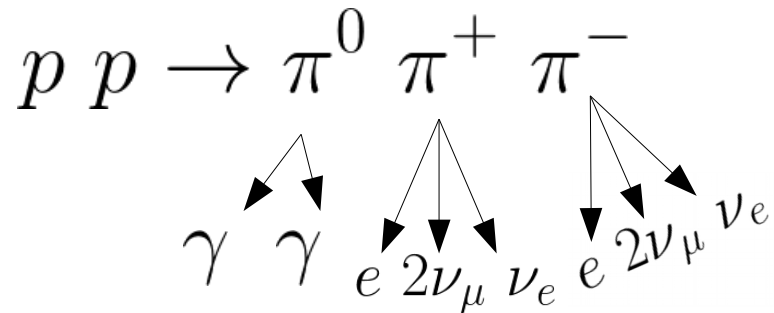


FIG. 3: The modeled intensity and spectrum of the neutrino and  $\gamma$ -ray emission produced by hadronic interactions in the *Fermi* bubbles. We show the predicted  $\gamma$ -ray (blue dashed) and all-flavor neutrino (orange solid) spectrum for our models of hadronic *Fermi* bubbles production (thick lines), as well as the hadronic fraction of our hybrid leptonic-hadronic model (thin lines). Details of the models are given in Section III. We note that the  $\gamma$ -ray spectrum in our leptonic-hadronic model receives additional contributions from the interactions of primary electrons, which are not shown here. We compare our results to  $\gamma$ -ray observations of the *Fermi* bubbles by the Fermi-LAT at GeV energies (black squares), the 95% confidence upper limits on the TeV  $\gamma$ -ray flux recorded by HAWC (black solid bars), the 90% confidence upper limits on ultrahigh-energy gamma rays by CASA-MIA scaled to the bubbles region (olive upper limits; [23, 32]), and the 90% confidence upper limit on the neutrino flux at TeV–PeV energies as calculated in this work (red upper limit). We additionally show the projected sensitivity from 100 hr of CTA observations (grey dotted; [33]), 5 yr of HiSCOR observations (green dotted; [34]), and 1 yr of LHAASO observations (pink dotted; [35]) in the region of the *Fermi* bubbles. In the hadronic scenario (thick lines), the maximum neutrino flux allowed by the Fermi-LAT and HAWC measurements does not produce a significant IceCube flux at high neutrino energies. However, in the hybrid leptonic-hadronic scenario (thin lines), the spectral index of the sub-dominant  $\gamma$ -ray component can be extremely hard, producing a bright neutrino flux detectable by IceCube. We note that the IceCube upper limit is calculated over a wide energy bin, and a significant number of neutrinos are observed at energies exceeding  $\sim 100$  TeV where the flux in the pure hadronic model is negligible.

$$E_\gamma^2 \Phi_\gamma \approx \frac{4}{K} (E_\nu^2 \Phi_{\nu_i}) \big|_{E_\nu=0.5E_\gamma}$$

Same amount of 3 pions, and they have approximately same energy:



$$E_\gamma = 1/2 E_\pi \quad \Delta N_\pi \doteq \Delta N_{\pi^+} = \Delta N_{\pi^-} = \Delta N_{\pi^0}$$

$$E_{\pi^+} = E_{\pi^-} = E_{\pi^0} = E_\pi$$

$$E_\nu = 1/4 E_\pi \quad \text{1 pion goes to 4 leptons, share share the E}$$

$$\Delta N_\pi = \int_{E_{\pi 1}}^{E_{\pi 2}} \frac{dN_\pi}{dE_\pi} \cdot dE_\pi$$

$$\frac{dN_\gamma}{dE_\gamma} \big|_{E_\gamma=E_\pi/2} = 4 \frac{dN_\pi}{dE_\pi} \big|_{E_\pi} \quad \text{Derivative for Epi2} \quad (1)$$

$$= 1/2 \Delta N_\gamma = 1/2 \int_{E_{\gamma 1}=1/2 E_{\pi 1}}^{E_{\gamma 2}=1/2 E_{\pi 2}} \frac{dN_\gamma}{dE_\gamma} \cdot dE_\gamma \quad (2)$$

$$N_{\nu_e} : N_{\nu_\mu} : N_{\nu_\tau} = 1 : 2 : 0$$

oscillation

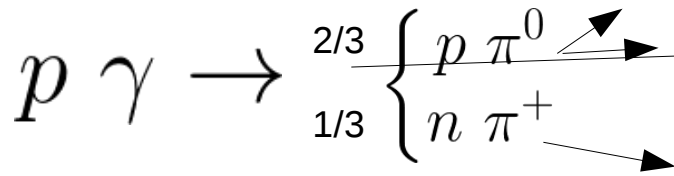
$$N_{\nu_e} \big|_{\text{earth}} : N_{\nu_\mu} \big|_{\text{earth}} : N_{\nu_\tau} \big|_{\text{earth}} = 1 : 1 : 1$$

$$N_{\nu_e} \big|_{\text{earth}} = N_{\nu_\mu} \big|_{\text{earth}} = N_{\nu_\tau} \big|_{\text{earth}} \doteq N_\nu = N_{\nu_e}$$

$$\frac{dN_\nu}{dE_\nu} \big|_{E_\nu=1/4 E_\pi} = 8 \frac{dN_\pi}{dE_\pi} \big|_{E_\pi} \quad \text{Derivative for Epi2} \quad 2\Delta N_\pi = \Delta N_\nu$$

$$\frac{dN_\nu}{dE_\nu} \big|_{E_\nu=1/4 E_\pi} = 2 \frac{dN_\gamma}{dE_\gamma} \big|_{E_\gamma=1/2 E_\pi} \longrightarrow 2E_\nu^2 \frac{dN_\nu}{dE_\nu} \big|_{E_\nu=1/4 E_\pi} = E_\gamma^2 \frac{dN_\gamma}{dE_\gamma} \big|_{E_\gamma=1/2 E_\pi}$$

$$E_\gamma^2 \Phi_\gamma \approx \frac{4}{K} (E_\nu^2 \Phi_{\nu_i}) \mid_{E_\nu=0.5E_\gamma}$$



Same amount of 3 pions, and they have approximately same energy:

$$\begin{aligned} E_\gamma &= 1/2 E_\pi \\ E_{\pi^+} &= E_{\pi^-} = E_{\pi^0} = E_\pi \\ E_\nu &= 1/4 E_\pi \quad \text{1 pion goes to 4 leptons, share share the E} \end{aligned}$$

$$\Delta N_{\pi^0} = \int_{E_{\pi 1}}^{E_{\pi 2}} \frac{dN_{\pi^0}}{dE_\pi} \cdot dE_\pi$$

pi0

$$\frac{dN_\gamma}{dE_\gamma} \mid_{E_\gamma=E_{\pi^0}/2} = 4 \frac{dN_{\pi^0}}{dE_{\pi^0}} \mid_{E_\pi}$$

Derivative for Epi2 (1)

$$= 1/2 \Delta N_\gamma = 1/2 \int_{E_{\gamma 1}=1/2 E_{\pi 1}}^{E_{\gamma 2}=1/2 E_{\pi 2}} \frac{dN_\gamma}{dE_\gamma} \cdot dE_\gamma$$

$$2\Delta N_{\pi^+} = \Delta N_{\pi^0} \quad (2)$$

$$N_{\nu_e} : N_{\nu_\mu} : N_{\nu_\tau} = 1 : 2 : 0$$

oscillation

$$\begin{aligned} N_{\nu_e} \mid_{\text{earth}} : N_{\nu_\mu} \mid_{\text{earth}} : N_{\nu_\tau} \mid_{\text{earth}} &= 1 : 1 : 1 \\ N_{\nu_e} \mid_{\text{earth}} &= N_{\nu_\mu} \mid_{\text{earth}} = N_{\nu_\tau} \mid_{\text{earth}} = N_\nu = N_{\nu_e} \end{aligned}$$

Due to only pi+, no pi-

pi+

$$\frac{dN_\nu}{dE_\nu} \mid_{E_\nu=1/4 E_{\pi^+}} = 4 \frac{dN_{\pi^+}}{dE_{\pi^+}} \mid_{E_\pi}$$

Derivative for Epi2

$$\Delta N_{\pi^+} = \Delta N_\nu$$

$$\boxed{2} \frac{dN_\nu}{dE_\nu} \mid_{E_\nu=1/4 E_\pi} = \boxed{\phantom{2}} \frac{dN_\gamma}{dE_\gamma} \mid_{E_\gamma=1/2 E_\pi} \longrightarrow \boxed{8}$$

Twice more than Murase's Formula, I think he took pi0 and pi+ to have same amount

# Details of goodness of fit

- goodness of fit test:

We use this statistical method to provide favored region of the parameters

For binned data, we could take it as Poisson distribution:

$$L(\theta) = f_P(n; \theta) = \prod_{i=1}^n \frac{\mu_i^{n_i}}{n_i!} e^{-\mu_i} \quad \theta = (M_{dm}, \tau_{dm})$$

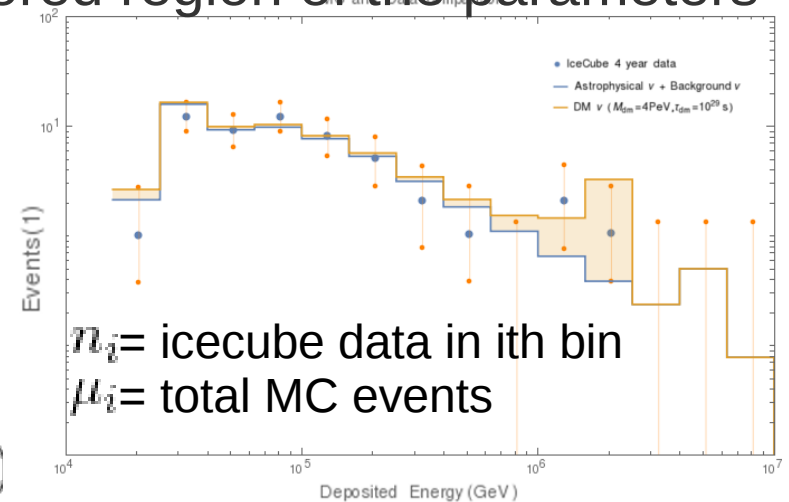
The likelihood ratio is:

$$\lambda(\theta) = \frac{f_P(n; \theta)}{f_P(n; \hat{\mu})} \quad \text{where} \quad \hat{\mu} = (n_1, n_2, \dots, n_N)$$

We choose the test statistic as:

$$TS = -2 \ln(\lambda(\theta)) = 2 \sum_{i=1}^N [\mu_i(\theta) - n_i + n_i \ln \frac{n_i}{\mu_i(\theta)}]$$

TS will be a function of theta and thus we could find out the region that is statistically favored



To acquire the TS distribution of Mdm and tdm, we perform a grid calculation:

Mdm=(0.1, 0.2,...,10)PeV

Tdm= $10^{(1,1.03,1.06,\dots,3)} \times 10^{27}$  s