



# BSM Interpretations of the Flavor Anomalies

**Bhupal Dev**

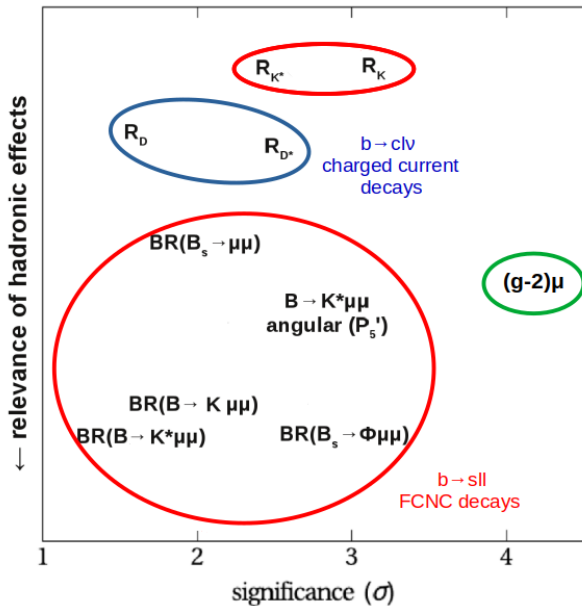
*Washington University in St. Louis*

SchwingerFest 2022: Muon  $g - 2$

University of California, Los Angeles

June 16, 2022

# Flavor Anomalies

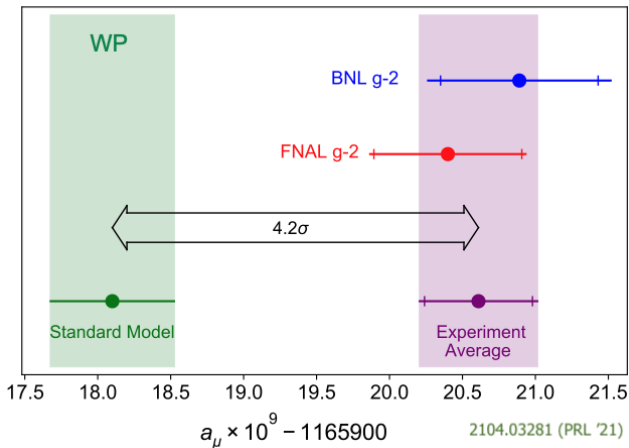
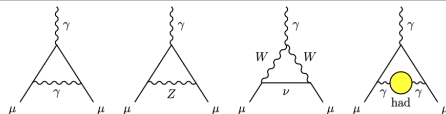


[from W. Altmannshofer's talk at *Anomalies 2021*]



Can a single BSM framework explain all the flavor anomalies?

# Muon Anomalous Magnetic Moment



$$a_\mu^{(\text{expt})} - a_\mu^{(\text{SM})} = (251 \pm 59) \times 10^{-11}$$

[see talk from G. Venanzoni]

# BSM Solutions to $(g - 2)_\mu$ Anomaly

Final Report of the Muon E821 Anomalous Magnetic Moment Measurement at BNL

#1

Muon  $g-2$  Collaboration · G.W. Bennett (Brookhaven) et al. (Feb, 2006)

Published in: *Phys.Rev.D* 73 (2006) 072003 · e-Print: [hep-ex/0602035](#) [hep-ex]

 pdf  DOI  cite

 2,882 citations

Measurement of the Positive Muon Anomalous Magnetic Moment to 0.46 ppm

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[see talks from S. Heinemeyer, P. Paradisi, E. Sessolo, P. Athron]

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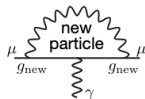
[pdf](#) [links](#) [DOI](#) [cite](#)

812 citations

[see talks from S. Heinemeyer, P. Paradisi, E. Sessolo, P. Athron]

- Need  $\Delta a_\mu = 251(59) \times 10^{-11}$  which is coincidentally at the same level as  $a_\mu^{\text{EW}} = 153.6(1.0) \times 10^{-11}$ .

$$\Delta a_\mu \sim \frac{g_{\text{new}}^2}{16\pi^2} \frac{(\text{muon mass} \sim 0.1 \text{ GeV})^2}{(\text{new particle mass})^2}$$
$$\sim a_\mu^{\text{EW}} \quad \text{when} \quad \begin{cases} g_{\text{new}} \sim W \text{ boson coupling} \\ m_{\text{new}} \sim W \text{ boson mass} \end{cases}$$



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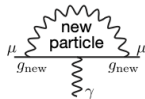
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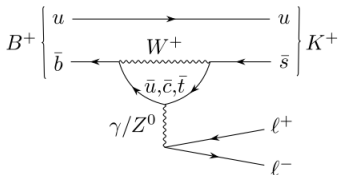
- Essentially two types of solutions:
  - Small interaction, small mass (e.g., ALP, dark photon, light  $Z'$ ) [see talks from J. Heeck, J. Fan]
  - $\mathcal{O}(1)$  interaction,  $\mathcal{O}(\text{EW})$  mass (e.g. 2HDM, SUSY, leptoquark) [see talk from S. Heinemeyer]
- New particle(s) in the loop can be anything: neutral/charged spin 0, 1/2, 1.

[Lindner, Platscher, Queiroz, 1610.06587 (Phys. Rep. '18)]

- Need to be careful about the sign of the BSM contribution.
- Also need flavor non-universal couplings to avoid other experimental constraints (mostly involving electron/quark sector).

# $R_{K^{(*)}}$ Anomaly ( $b \rightarrow s\ell^+\ell^-$ )

$$R_{K^{(*)}} = \frac{\text{BR}(B \rightarrow K^{(*)}\mu^+\mu^-)}{\text{BR}(B \rightarrow K^{(*)}e^+e^-)}$$



- Flavor Changing Neutral Current  $\rightarrow$  **loop-suppressed** in the SM.
- New physics can be heavy (multi-TeV).

$$R_{K^+}^{[1,6]} = 0.846^{+0.042+0.013}_{-0.039-0.012}$$

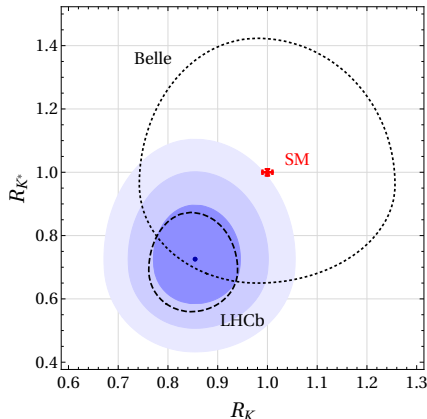
$$R_{K^*0}^{[0.045,1.1]} = 0.66^{+0.11}_{-0.07} \pm 0.03$$

$$R_{K^*0}^{[1,1,6]} = 0.69^{+0.11}_{-0.07} \pm 0.05$$

$$R_{K_S}^{[1,1,6]} = 0.66^{+0.20+0.02}_{-0.14-0.04}$$

$$R_{K^{*+}}^{[0.045,6]} = 0.70^{+0.18+0.03}_{-0.13-0.04}$$

$$R_{pK}^{[0,1,6]} = 0.86^{+0.14}_{-0.11} \pm 0.05$$



[Altmannshofer, BD, Soni, Sui, 2002.12910 (PRD '20)]

- $3.4\sigma$  net discrepancy.
- All measurements are consistently below the SM.
- **LHCb update** [2103.11769 (Nature Phys. '22)] **didn't change the central value.**



# BSM Solutions to $R_{K^{(*)}}$ Anomaly

$$\mathcal{H}_{\text{eff}} = \mathcal{H}_{\text{eff}}^{\text{SM}} - \frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{e^2}{16\pi^2} \sum_i C_i \mathcal{O}_i$$

$$O_9^{bs\ell\ell} = (\bar{s}\gamma_\mu P_L b)(\bar{\ell}\gamma^\mu \ell),$$

$$O_9^{bs\ell\ell} = (\bar{s}\gamma_\mu P_R b)(\bar{\ell}\gamma^\mu \ell),$$

$$O_{10}^{bs\ell\ell} = (\bar{s}\gamma_\mu P_L b)(\bar{\ell}\gamma^\mu \gamma_5 \ell),$$

$$O_{10}^{bs\ell\ell} = (\bar{s}\gamma_\mu P_R b)(\bar{\ell}\gamma^\mu \gamma_5 \ell),$$

Altmannshofer, Stangl, 2103.13370 (EPJC '21)		$b \rightarrow s\mu\mu$		LFU, $B_s \rightarrow \mu\mu$		all rare $B$ decays	
Wilson coefficient		best fit	pull	best fit	pull	best fit	pull
$C_9^{bs\mu\mu}$		$-0.75^{+0.22}_{-0.23}$	$3.4\sigma$	$-0.74^{+0.20}_{-0.21}$	$4.1\sigma$	$-0.73^{+0.15}_{-0.15}$	$5.2\sigma$
$C_{10}^{bs\mu\mu}$		$+0.42^{+0.23}_{-0.24}$	$1.7\sigma$	$+0.60^{+0.14}_{-0.14}$	$4.7\sigma$	$+0.54^{+0.12}_{-0.12}$	$4.7\sigma$
$C_9^{rbs\mu\mu}$		$+0.24^{+0.27}_{-0.26}$	$0.9\sigma$	$-0.32^{+0.16}_{-0.17}$	$2.0\sigma$	$-0.18^{+0.13}_{-0.14}$	$1.4\sigma$
$C_{10}^{rbs\mu\mu}$		$-0.16^{+0.16}_{-0.16}$	$1.0\sigma$	$+0.06^{+0.12}_{-0.12}$	$0.5\sigma$	$+0.02^{+0.10}_{-0.10}$	$0.2\sigma$
$C_9^{bs\mu\mu} = C_{10}^{bs\mu\mu}$		$-0.20^{+0.15}_{-0.15}$	$1.3\sigma$	$+0.43^{+0.18}_{-0.18}$	$2.4\sigma$	$+0.05^{+0.12}_{-0.12}$	$0.4\sigma$
$C_9^{bs\mu\mu} = -C_{10}^{bs\mu\mu}$		$-0.53^{+0.13}_{-0.13}$	$3.7\sigma$	$-0.35^{+0.08}_{-0.08}$	$4.6\sigma$	$-0.39^{+0.07}_{-0.07}$	$5.6\sigma$

# BSM Solutions to $R_{K^{(*)}}$ Anomaly

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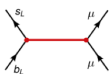
$$O_{10}^{bs\ell\ell} = (\bar{s}\gamma_\mu P_L b)(\bar{\ell}\gamma^\mu \gamma_5 \ell),$$

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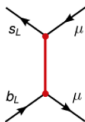
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## ➤ Possible BSM models

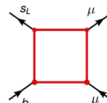


- Heavy  $Z'$  model
- $SU(2)_L$  singlet or triplet
- arXiv:1403.1269, 1501.00993, 1503.03477, 1611.02703, ...



- Leptoquark model
- Spin 0 or 1
- arXiv:01511.01900, 1503.01084, 1704.05835, 1512.01560, 1511.06024, 1408.1627, ...

arXiv:1706.07808

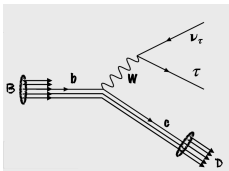


- Other new heavy scalars/vectors also leptoquark possible
- arXiv:01509.05020, 1608.07832, 1704.05438, 1607.01659, 1704.07845, hep-ph/0610037, ...

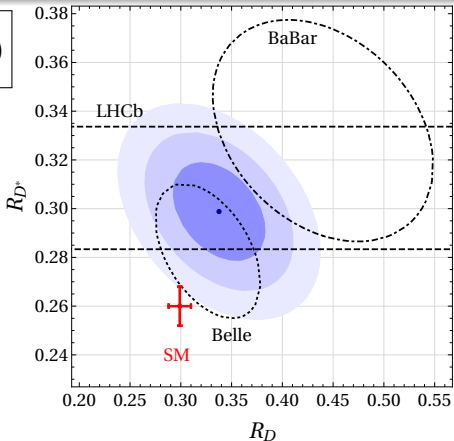


# $R_{D^{(*)}}$ Anomaly ( $b \rightarrow c\tau\nu$ )

$$R_{D^{(*)}} = \frac{\text{BR}(B \rightarrow D^{(*)}\tau\nu)}{\text{BR}(B \rightarrow D^{(*)}\ell\nu)} \quad (\text{with } \ell = e, \mu)$$



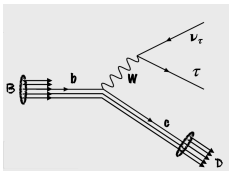
Experiment	Tag method	$\tau$ decay mode	$R_D$	$R_{D^*}$	$R_{J/\psi}$
Babar (2012) [1]	hadronic	$\ell\nu\nu$	$0.440 \pm 0.058 \pm 0.042$	$0.332 \pm 0.024 \pm 0.018$	
Belle (2015) [2]	hadronic	$\ell\nu\nu$	$0.375 \pm 0.064 \pm 0.026$	$0.293 \pm 0.038 \pm 0.015$	
LHCb (2015) [5]	hadronic	$\ell\nu\nu$	-	$0.336 \pm 0.027 \pm 0.030$	
Belle (2016) [2]	semileptonic	$\ell\nu\nu$	-	$0.302 \pm 0.030 \pm 0.011$	
Belle (2017) [3]	hadronic	$\pi(\rho)\nu$	-	$0.270 \pm 0.035 \pm 0.027$	
LHCb (2017) [6]	hadronic	$3\pi\nu$	-	$0.291 \pm 0.019 \pm 0.029$	
Belle (2019) [4]	semileptonic	$\ell\nu\nu$	$0.307 \pm 0.037 \pm 0.016$	$0.283 \pm 0.018 \pm 0.014$	
LHCb (2016) [67]	hadronic	$\ell\nu\nu$	-	-	$0.71 \pm 0.17 \pm 0.18$
SM	-	-	$0.299 \pm 0.011$ [63]	$0.260 \pm 0.008$ [64]	$0.26 \pm 0.02$ [68]



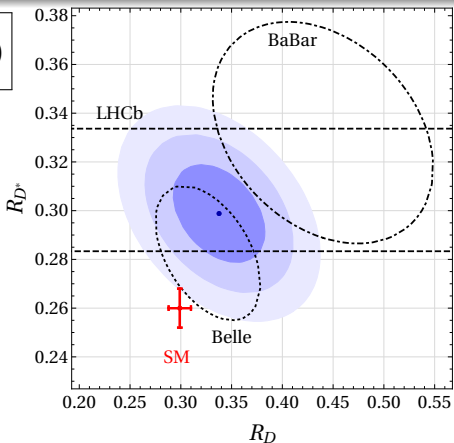
[Altmannshofer, BD, Soni, Sui, 2002.12910 (PRD '20)]

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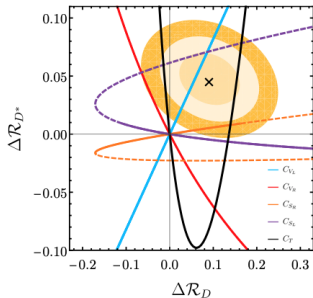


[Altmannshofer, BD, Soni, Sui, 2002.12910 (PRD '20)]

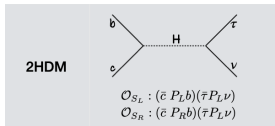
- Flavor Changing Charged Current – **tree-level** in the SM (only CKM-suppressed).
- BSM effect has to be large  $\implies \lesssim \mathcal{O}(\text{TeV})$ -scale new particle.
- **All experimental measurements to date are consistently above the SM prediction.**
- $3.3\sigma$  discrepancy (HFLAV gives  $3.1\sigma$ )  $\longrightarrow$  **Lattice can improve SM prediction.**

# BSM Solutions to $R_{D^{(*)}}$ Anomaly

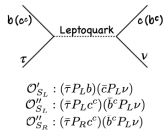
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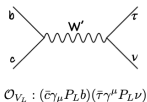
[Murgui, Peñuelas, Jung, Pich, 1904.09311 (JHEP '19)]



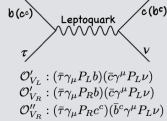
**Scalar  
Leptoquark**



**W'**

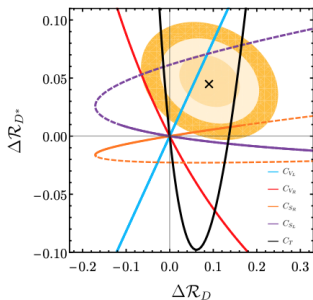


**Vector  
Leptoquark**

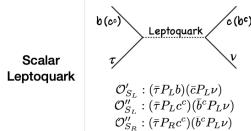
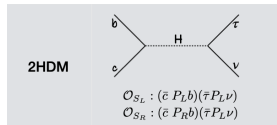


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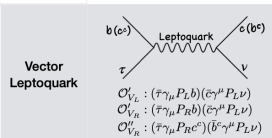
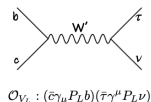
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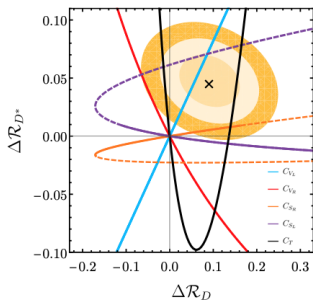
**$W'$**



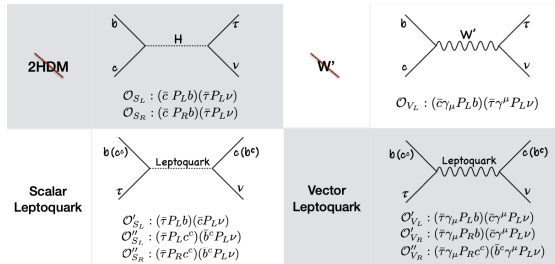
- Charged Higgs solution in type-II 2HDM (MSSM-type) goes in the wrong direction [BaBar, 1303.0571 (PRD '13); Belle, 1906.06871].
- In general, tension with LHC mono- $\tau$  data [Greljo, Camalich, Ruiz-Alvarez, 1811.07920 (PRL '19)] and induces a large  $\text{BR}(B_c \rightarrow \tau \nu) > 50\%$  which is problematic [Alonso, Grinstein, Camalich, 1611.06676 (PRL '17); Akeroyd, Chen, 1708.04072 (PRD '17); Aebischer, Grinstein, 2105.02988]
- $W'$  solution is challenged by LHC di-tau data [Faroughy, Greljo, Kamenik, 1609.07138 (PLB '17)] and by precision Z-pole observables [Feruglio, Paradisi, Pattori, 1606.00524 (PRL '17)].

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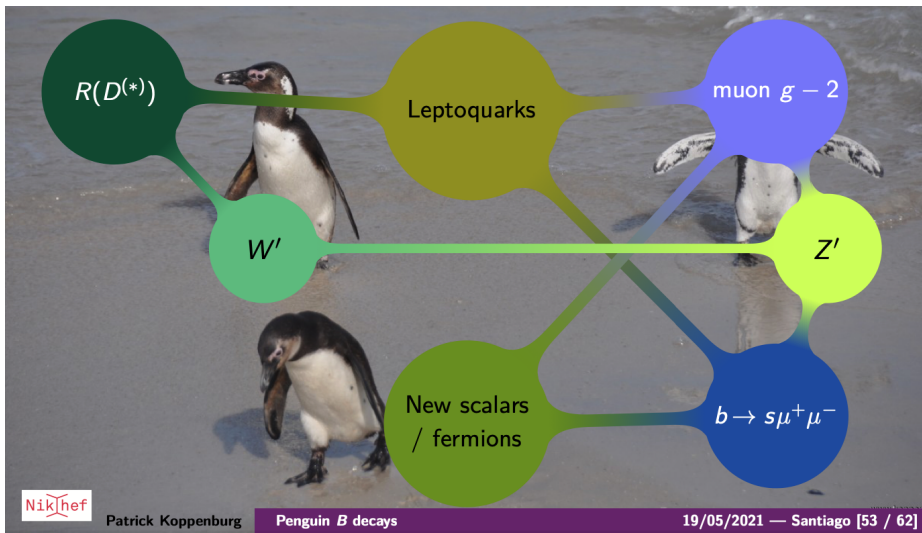


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# BSM Solutions to All Flavor Anomalies

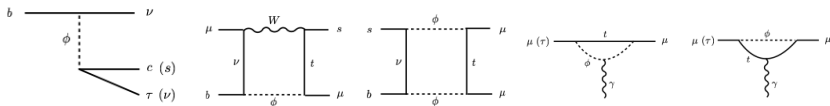


**Leptoquarks emerge as the winner! (or not too soon?)**



# Leptoquarks

- Single scalar leptoquark solution [Bauer, Neubert, 1511.01900 (PRL '16)]

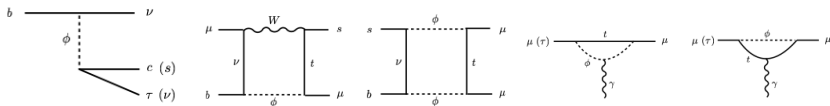


- Now disfavored by global fits (including  $b \rightarrow s\mu^+\mu^-$  observables, as well as LHC constraints). [Angelescu, Becirevic, Faroughy, Jaffredo, Sumensari, 2103.12504]

Model	$R_{K^{(*)}}$	$R_{D^{(*)}}$	$R_{K^{(*)}}$ & $R_{D^{(*)}}$
$S_3$ ( $\bar{\mathbf{3}}, \mathbf{3}, 1/3$ )	✓	✗	✗
$S_1$ ( $\bar{\mathbf{3}}, \mathbf{1}, 1/3$ )	✗	✓	✗
$R_2$ ( $\mathbf{3}, \mathbf{2}, 7/6$ )	✗	✓	✗
$U_1$ ( $\mathbf{3}, \mathbf{1}, 2/3$ )	✓	✓	✓
$U_3$ ( $\mathbf{3}, \mathbf{3}, 2/3$ )	✓	✗	✗

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$S_1$ ( $\bar{\mathbf{3}}, \mathbf{1}, 1/3$ )	✗	✓	✗
$R_2$ ( $\mathbf{3}, \mathbf{2}, 7/6$ )	✗	✓	✗
$U_1$ ( $\mathbf{3}, \mathbf{1}, 2/3$ )	✓	✓	✓
$U_3$ ( $\mathbf{3}, \mathbf{3}, 2/3$ )	✓	✗	✗

- Vector LQ must be embedded into some UV-completion [e.g. Heeck, Teresi, 1808.07492]
- Solutions with more than one scalar LQ also possible. [Chen, Nomura, Okada, 1703.03251; Bigaran, Gargalionis, Volkas, 1906.01870]; Saad, 2005.04352; Babu, BD, Jana, Thapa, 2009.01771; Heeck, Thapa, 2202.08854; Crivellin, Fuks, Schnell, 2203.10111; ...]

## An alternative route: $R$ -parity violating Supersymmetry!

(not just another LQ model)

# An alternative route: $R$ -parity violating Supersymmetry!

(not just another LQ model)



The image is a screenshot of the Scientific American website. At the top, the logo "SCIENTIFIC AMERICAN" is displayed in a large, serif font. To its right is a small graphic of a horse and the text "20th NATIONAL MAGAZINE AWARD WINNER". Below the logo is a search bar with the text "Search ScientificAmerican.com" and a magnifying glass icon. A red navigation bar contains links for "Subscribe", "News & Features", "Blogs", "Multimedia", "Education", "Citizen Science", and "Topics". Below this bar, the breadcrumb "Home > Scientific American Magazine > May 2012" is visible. A section labeled "Advertise | More Science" includes social media buttons for Twitter (20) and Facebook (343). The main article is titled "Is Supersymmetry Dead?" in a large, bold font. The sub-headline reads: "The grand scheme, a stepping-stone to string theory, is still high on physicists' wish lists. But if no solid evidence surfaces soon, it could begin to have a serious PR problem." The byline is "By Davide Caselvecchi | April 25, 2012" with a "29" indicating the number of comments. A small thumbnail image of a particle detector is shown to the left of the article title.

# An alternative route: $R$ -parity violating Supersymmetry!

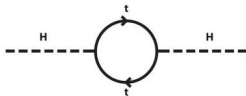
(not just another LQ model)



**SUSY is alive and doing just fine.**

# Why SUSY?

Gauge hierarchy problem



SUSY solution

# Why SUSY?



## Standard Model particles



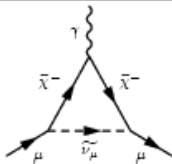
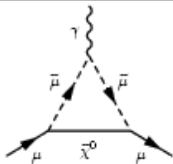
## Supersymmetric partners



## Natural SUSY

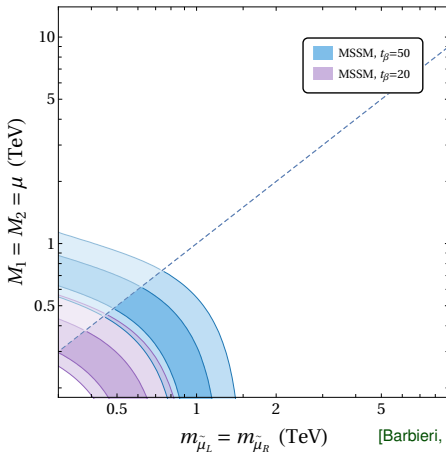
[Brust, Katz, Lawrence, Sundrum, 1110.6670 (JHEP '12); Papucci, Ruderman, Weiler, 1110.6926 (JHEP '12)]

# Muon $g - 2$ in MSSM



$$a_{\mu}^{\tilde{\chi}^\pm - \tilde{\nu}_\mu} \simeq \frac{\alpha m_\mu^2 M_2 \tan \beta}{4\pi \sin^2 \theta_W m_{\tilde{\nu}_\mu}^2} \left[ \frac{f_{\chi^\pm} (M_2^2/m_{\tilde{\nu}_\mu}^2) - f_{\chi^\pm} (\mu^2/m_{\tilde{\nu}_\mu}^2)}{M_2^2 - \mu^2} \right],$$

$$a_{\mu}^{\tilde{\chi}^0 - \tilde{\mu}} \simeq \frac{\alpha m_\mu^2 M_1 (\mu \tan \beta - A_\mu)}{4\pi \cos^2 \theta_W (m_{\tilde{\mu}_R}^2 - m_{\tilde{\mu}_L}^2)} \left[ \frac{f_{\chi^0} (M_1^2/m_{\tilde{\mu}_R}^2)}{m_{\tilde{\mu}_R}^2} - \frac{f_{\chi^0} (M_1^2/m_{\tilde{\mu}_L}^2)}{m_{\tilde{\mu}_L}^2} \right]$$



[Barbieri, Maiani (PLB '82); Moroi (PRD '96);

Chakraborti, Heinemeyer, Saha (2104.03287); Altmannshofer, Gadam, Gori, Hamer (2104.08293)]



- There are tree level contributions to  $B \rightarrow D^{(*)} \tau \nu$  from **charged Higgs exchange**

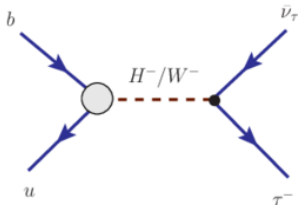
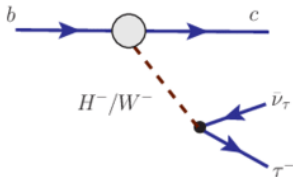
$$\frac{R_D}{R_D^{\text{SM}}} \sim 1 - 1.5 \frac{m_\tau m_b}{m_{H^\pm}^2} \tan^2 \beta$$

$$\frac{R_{D^*}}{R_{D^*}^{\text{SM}}} \sim 1 - 0.12 \frac{m_\tau m_b}{m_{H^\pm}^2} \tan^2 \beta$$

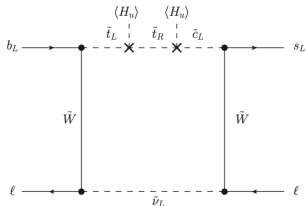
- Effect goes in the **wrong direction** and is much smaller for  $R_{D^*}$
- Correlated with effect in  $B \rightarrow \tau \nu$

$$\frac{\text{BR}(B \rightarrow \tau \nu)}{\text{BR}(B \rightarrow \tau \nu)_{\text{SM}}} \simeq \left( 1 - \frac{m_B^2}{m_{H^\pm}^2} \tan^2 \beta \right)^2$$

⇒ **Can't explain  $R_{D^{(*)}}$  with charged Higgs exchange** in the MSSM



# $R_{K(*)}$ in MSSM



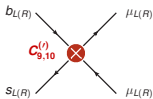
- only way to get lepton flavor non universal contribution to rare  $b \rightarrow s \ell \ell$  decays is through box diagrams with light winos (or Binos) and large **non-universality in slepton masses**.

- requires an **extremely light spectrum** to get  $C_9^{bs\mu\mu} \sim -0.5$ :

winos and smuons around 100 GeV;  
sbottoms around 500 GeV;

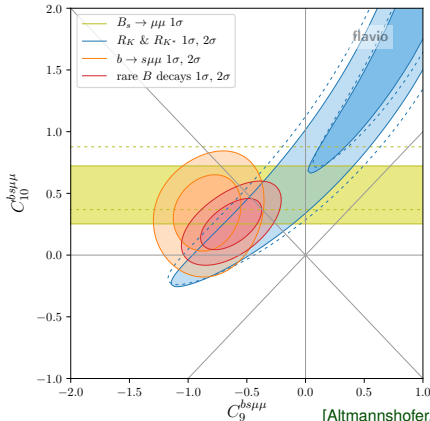
**very challenging** to hide this at the LHC...

semileptonic operators



$$C_9^{(r)}(\bar{s}\gamma_\mu P_{L(R)}b)(\bar{\mu}\gamma^\mu\mu)$$

$$C_{10}^{(r)}(\bar{s}\gamma_\mu P_{L(R)}b)(\bar{\mu}\gamma^\mu\gamma_5\mu)$$



[Altmannshofer, Stangl (2103.13370)]

# MSSM with R-Parity Violation

- More natural to include RPV couplings, rather than imposing  $R$ -parity by hand.  
[Brust, Katz, Lawrence, Sundrum, 1110.6670 (JHEP '12)]
- LFUV arises naturally – á la Yang-Mills. [BD, Soni, Xu, 2106.15647]
- Third generation may be special. (LFUV in  $B$ -sector, but not in  $D$  nor in  $\Lambda$ )
- **RPV3**: RPV SUSY with light 3rd-generation sfermions.  
[Altmannshofer, BD, Soni, 1704.06659 (PRD '17)]

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- **RPV3**: RPV SUSY with light 3rd-generation sfermions.

[Altmannshofer, BD, Soni, 1704.06659 (PRD '17)]

- Can naturally accommodate  $R_{D^{(*)}}$  ( $b \rightarrow c \tau \nu$ ) via  $LQD$  interactions. [Deshpande, He

(EPJC '17); Altmannshofer, BD, Soni (PRD '17); Trifinopoulos (EPJC '18); Hu, Li, Muramatsu, Yang (PRD '19)]

$$\mathcal{L}_{LQD} = \lambda'_{ijk} [\tilde{\nu}_{iL} \bar{d}_{kR} d_{jL} + \tilde{d}_{jL} \bar{d}_{kR} \nu_{iL} + \tilde{d}_{kR}^* \bar{\nu}_{iL}^c d_{jL} - \tilde{e}_{iL} \bar{d}_{kR} u_{jL} - \tilde{u}_{jL} \bar{d}_{kR} e_{iL} - \tilde{d}_{kR}^* \bar{e}_{iL}^c u_{jL}] + \text{H.c.}$$

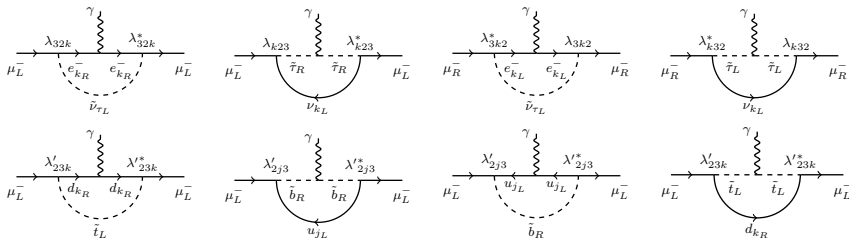
- Can *simultaneously* explain  $R_{K^{(*)}}$  ( $b \rightarrow s \ell \ell$ ) via  $LLE$  interactions, together with  $LQD$ . [Das, Hati, Kumar, Mahajan (PRD '17); Earl, Grégoire (JHEP '18); Trifinopoulos (EPJC '18); Hu, Huang (PRD '20);

Altmannshofer, BD, Soni, Sui (PRD '20)]

$$\mathcal{L}_{LLE} = \frac{1}{2} \lambda_{ijk} [\tilde{\nu}_{iL} \bar{e}_{kR} e_{jL} + \tilde{e}_{jL} \bar{e}_{kR} \nu_{iL} + \tilde{e}_{kR}^* \bar{\nu}_{iL}^c e_{jL} - (i \leftrightarrow j)] + \text{H.c.}$$

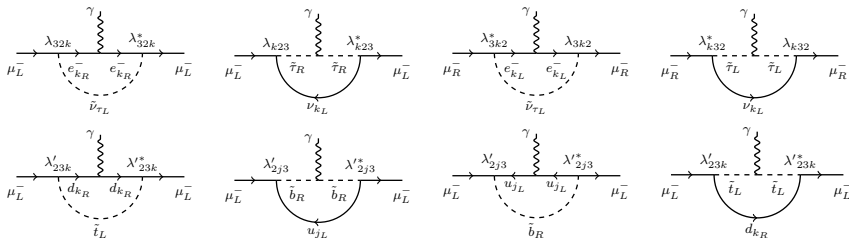
- Muon  $g - 2$  from both  $LQD$  and  $LLE$  terms, but  $LLE$  more relevant.

# Muon $g - 2$ in RPV3



[Kim, Kyae, Lee (PLB '01)]

# Muon $g - 2$ in RPV3

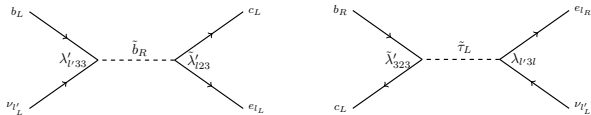


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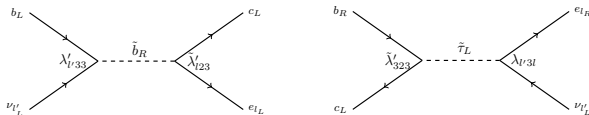
- 1-loop contributions from  $\lambda'$  and  $\lambda$  couplings (in addition to the standard MSSM contributions)

$$\Delta a_\mu = \frac{m_\mu^2}{96\pi^2} \sum_{k=1}^3 \left( \frac{2(|\lambda_{32k}|^2 + |\lambda_{3k2}|^2)}{m_{\tilde{\nu}_\tau}^2} - \frac{|\lambda_{3k2}|^2}{m_{\tilde{\tau}_L}^2} - \frac{|\lambda_{k23}|^2}{m_{\tilde{\tau}_R}^2} + \frac{3|\lambda'_{2k3}|^2}{m_{\tilde{b}_R}^2} \right)$$

- Need **light sbottoms and/or sneutrinos** with **large couplings** to get a relevant contribution in the right direction



[Deshpande, He (EPJC '17); Altmannshofer, BD, Soni (PRD '17); ...]



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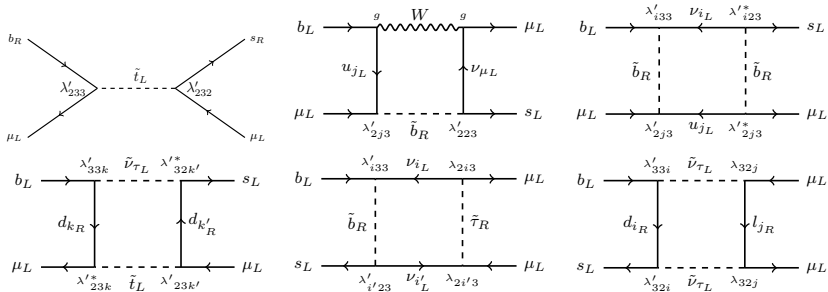
- Tree level contributions from **sbottom or stau exchange**
- Stau behaves like a charged Higgs (but its couplings are less constrained). **Stau contribution disfavored** by  $B_c \rightarrow \tau \nu$  branching ratio and kinematic distributions in  $B \rightarrow D^{(*)} \tau \nu$ .
- **Sbottom behaves like a leptoquark**. Chirality structure as preferred by model independent fits (Shi et al. 1905.08498; Murgui et al. 1904.09311; Asadi, Shih 1905.03311; Cheung et al. 2002.07272; ...)
- **Can address the  $R_{D^{(*)}}$  anomalies** for sbottom masses  $O(1 \text{ TeV})$  and couplings  $\lambda' \sim O(1)$
- need to be careful to **keep  $\mu - e$  universality** in  $b \rightarrow c \ell \nu$

$$\frac{R_D}{R_D^{\text{SM}}} = \frac{R_{D^*}}{R_{D^*}^{\text{SM}}} = \frac{|\Delta_{31}^c|^2 + |\Delta_{32}^c|^2 + |1 + \Delta_{33}^c|^2}{|\Delta_{21}^c|^2 + |1 + \Delta_{22}^c|^2 + |\Delta_{23}^c|^2},$$

$$\text{with } \Delta_{ll'}^c = \frac{v^2}{4m_{b_R}^2} \lambda'_{l'33} \left( \lambda'_{l33} + \lambda'_{l23} \frac{V_{cs}}{V_{cb}} + \lambda'_{l13} \frac{V_{cd}}{V_{cb}} \right).$$

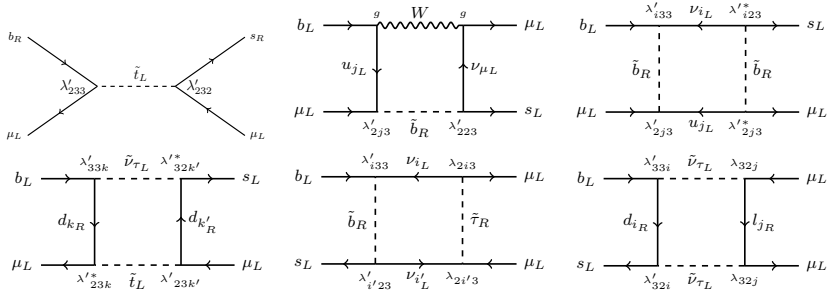


# $R_{K(*)}$ in RPV3



[Das, Hati, Kumar, Mahajan (PRD '17); Trifinopoulos (EPJC '18); ...]

# $R_{K(*)}$ in RPV3



[Das, Hati, Kumar, Mahajan (PRD '17); Trifinopoulos (EPJC '18); ...]

- Tree level contribution from stop exchange have the wrong chirality
- Several loop contributions with the right chirality and  $C_9 = -C_{10}$
- Both  $\lambda$  and  $\lambda'$  couplings can be involved

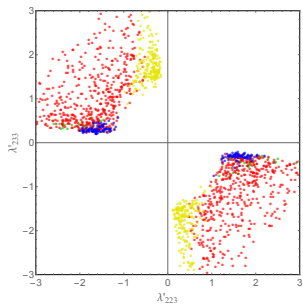
$$C_9^\mu = -C_{10}^\mu = \frac{m_t^2}{m_{b_R}^2} \frac{|\lambda'_{233}|^2}{16\pi\alpha_{\text{em}}} - \frac{v^2}{m_{b_R}^2} \frac{X_{bs}X_{\mu\mu}}{64\pi\alpha_{\text{em}}V_{tb}V_{ts}^*},$$

where  $X_{bs} = \sum_{i=1}^3 \lambda'_{i33}\lambda'_{i23}$  and  $X_{\mu\mu} = \sum_{j=1}^3 |\lambda'_{2j3}|^2$ .

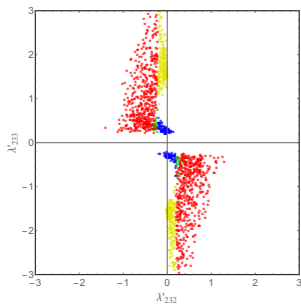
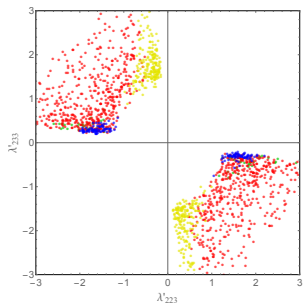
# Low-energy Constraints

Constraint	Parameter dependence	Relevant terms
$B \rightarrow \tau \nu$	$\lambda'_{\ell'33}, \lambda'_{3j3}, m_{\tilde{b}_R}$	$\frac{\lambda'_{\ell'33} \cdot \lambda'_{3j3}}{m_{\tilde{b}_R}^2}$
$B \rightarrow K^{(*)} \nu \bar{\nu}$	$\lambda'_{\ell'33}, \lambda'_{\ell 23}, m_{\tilde{b}_R}$	$\frac{\lambda'_{\ell'33} \cdot \lambda'_{\ell 23}}{m_{\tilde{b}_R}^2}, \frac{\lambda'_{\ell'33} \cdot \lambda'_{\ell 32}}{m_{\tilde{b}_L}^2}$
$B \rightarrow \pi/\rho \nu \bar{\nu}$	$\lambda'_{\ell'33}, \lambda'_{\ell 13}, m_{\tilde{b}_R}$	$\frac{\lambda'_{\ell'33} \cdot \lambda'_{\ell 13}}{m_{\tilde{b}_R}^2}$
$B_s - \bar{B}_s$ mixing	$\lambda'_{i33}, \lambda'_{i23}, \lambda'_{i32},$ $m_{\tilde{b}_R}, m_{\tilde{\nu}}$	$\frac{\lambda'_{i23} \lambda'_{i33} \lambda'_{j23} \lambda'_{j33}}{m_{\tilde{b}_R}^2},$ $\frac{\lambda'_{i23} \lambda'_{i32} \lambda'_{j33} \lambda'_{j33}}{m_{\tilde{b}_R}^2},$ $\frac{\lambda'_{332} \lambda'_{323}}{m_{\tilde{\nu}}^2}$
$D - \bar{D}$ mixing	$\lambda'_{323}, m_{\tilde{b}_R}, m_{\tilde{\tau}_R}$	$\frac{\lambda_{323}^4}{m_{\tilde{b}_R}^2}, \frac{\lambda_{323}^{\prime 4}}{m_{\tilde{\tau}_R}^2}$
$D^0 \rightarrow \mu^+ \mu^-$	$\lambda'_{2j3}, m_{\tilde{b}_R}$	$\frac{\lambda'_{2j3} \lambda'_{2j'3}}{m_{\tilde{b}_R}^2}$
$\tau \rightarrow \ell \nu \bar{\nu}$	$\lambda_{323}, \lambda'_{333}, m_{\tilde{\tau}_R}, m_{\tilde{b}_R}$	$\frac{\lambda_{323}^2}{m_{\tilde{\tau}_R}^2}, \frac{\lambda_{333}^{\prime 2}}{m_{\tilde{b}_R}^2}$
$Z \rightarrow \ell \bar{\ell}'$	$\lambda'_{333}, m_{\tilde{b}_R}$	$\frac{\lambda_{333}^{\prime 2}}{m_{\tilde{b}_R}^2}$

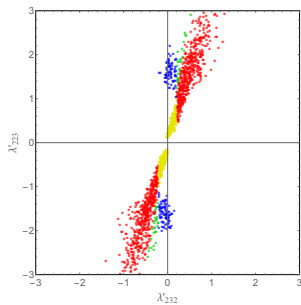
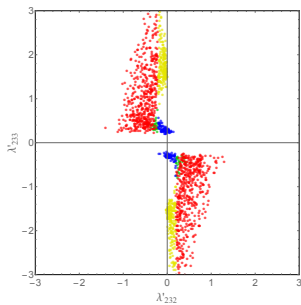
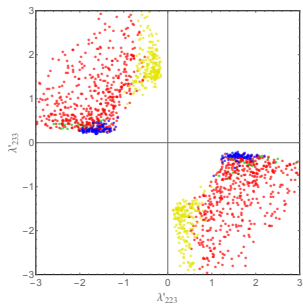
# Numerical Scan



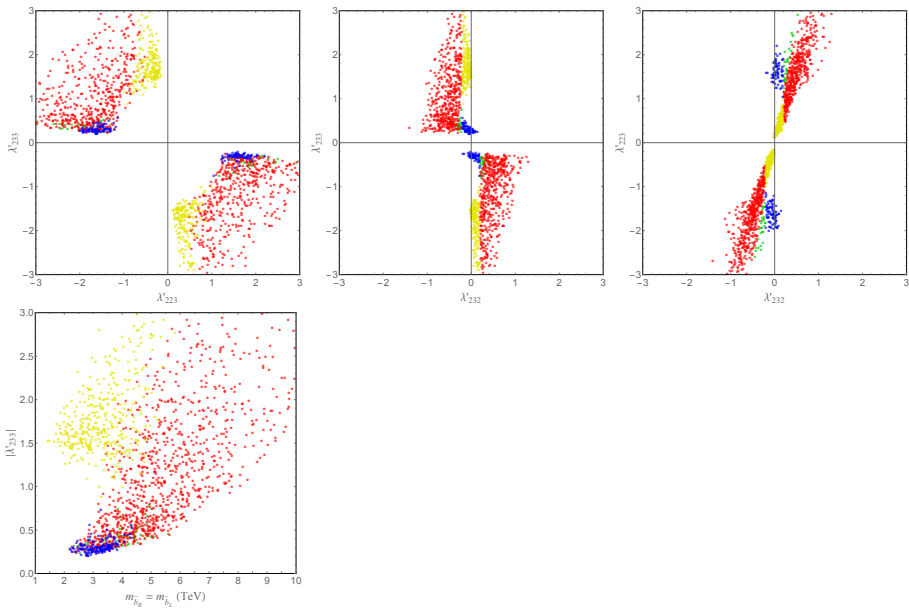
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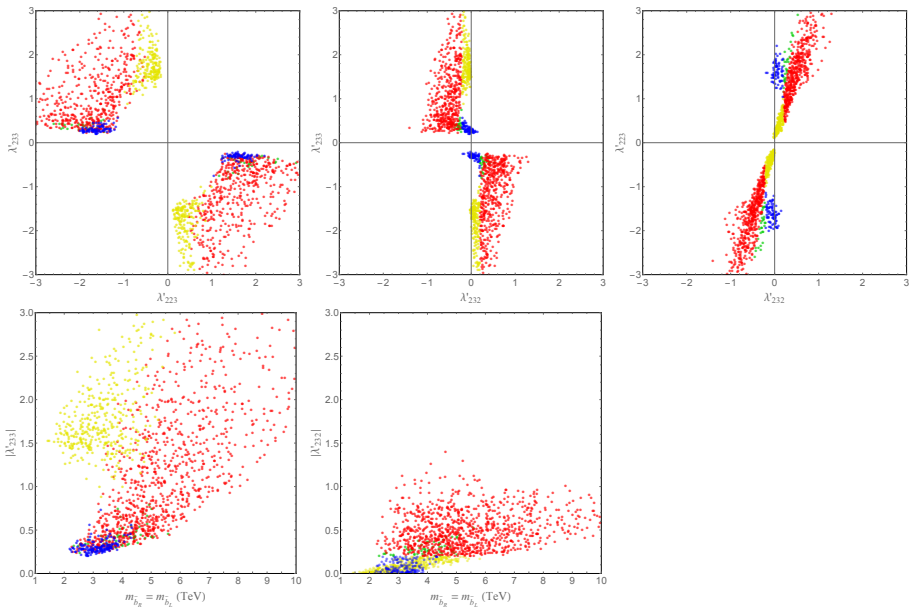
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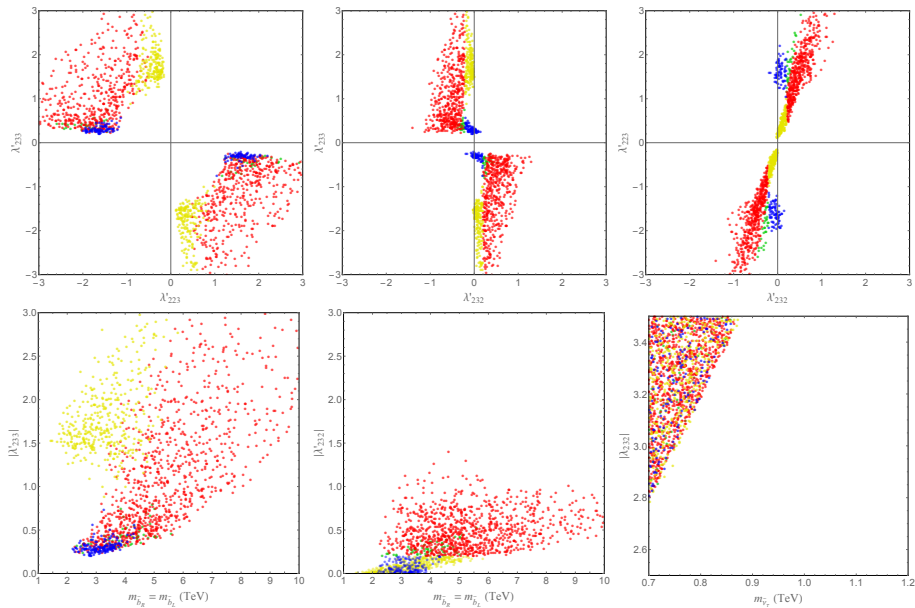


# Numerical Scan

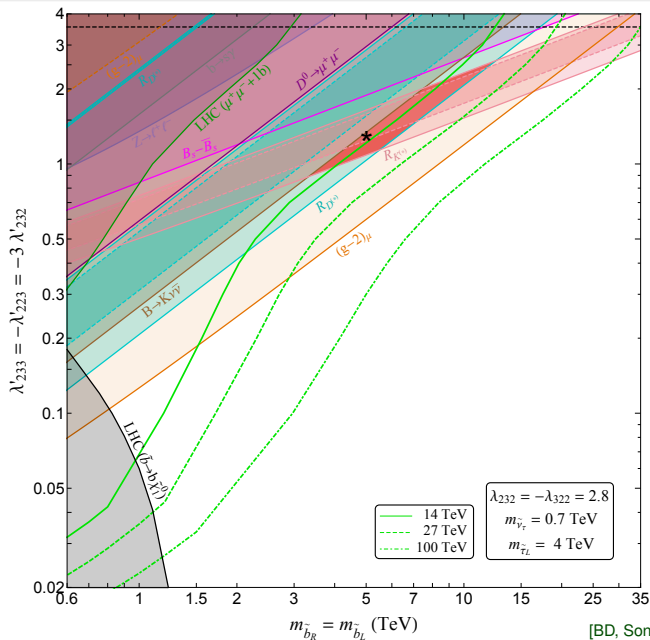




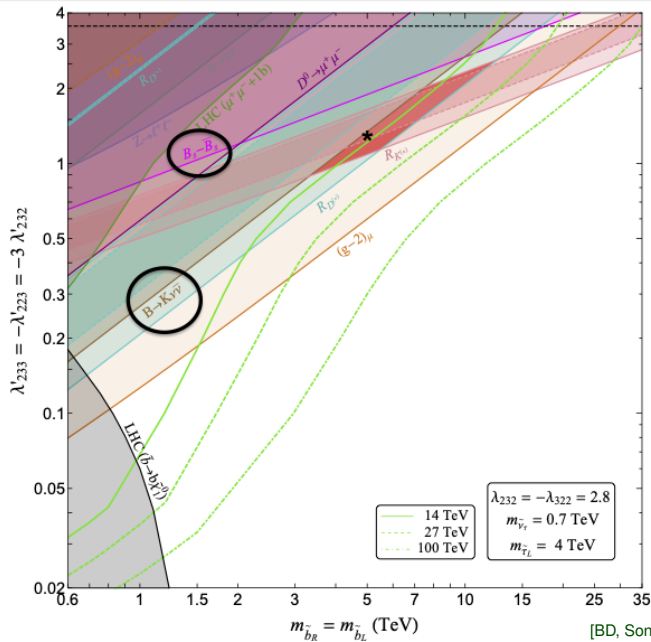
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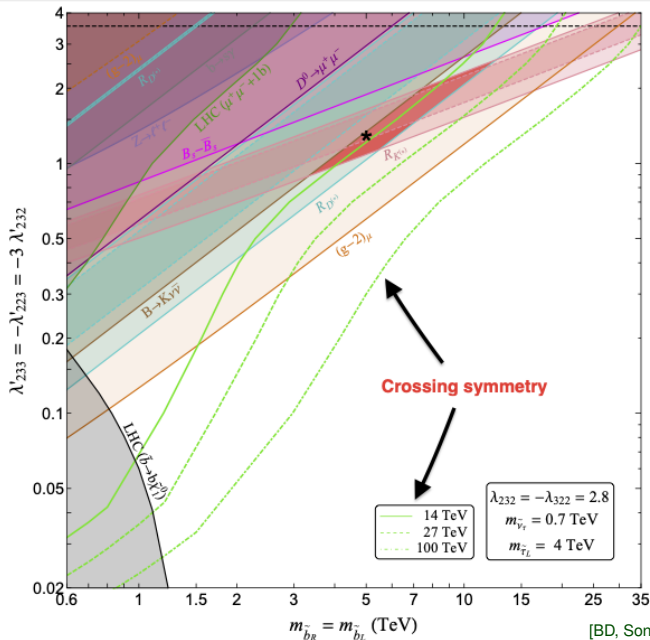
# A Combined RPV3 Fit to All Flavor Anomalies



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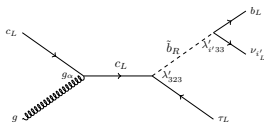
# Distinct LHC Signals in RPV3

- Effective operators:

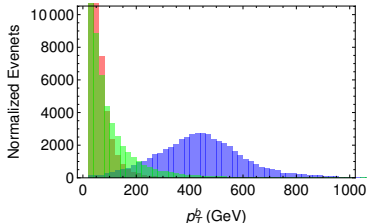
$$R_{D^{(*)}} : \mathcal{O}_{V_L} = (\bar{c}\gamma^\mu P_L b)(\bar{\tau}\gamma_\mu P_L \nu)$$

$$R_{K^{(*)}} : Q_{9(10)}^\ell = (\bar{s}\gamma^\mu P_L b)(\bar{\ell}\gamma_\mu(\gamma_5)\ell)$$

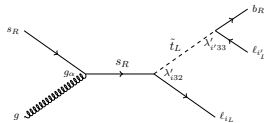
- Crossing symmetry:  $b \rightarrow c\tau\nu$  leads to  $gc \rightarrow b\tau\nu$ , and  $b \rightarrow s\ell\ell$  leads to  $gs \rightarrow b\ell\ell$ .



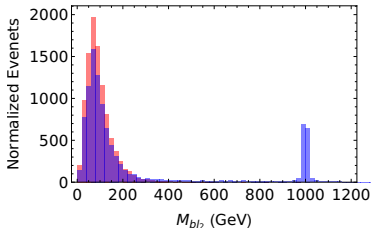
■ SM ■ Vector ■ Scalar



[Altmannshofer, BD, Soni (PRD '17)]

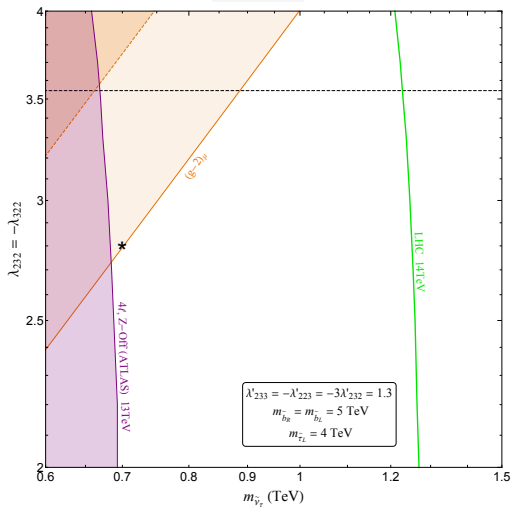
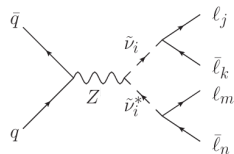
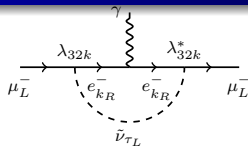


■ SM ■ RPV



[Altmannshofer, BD, Soni, Sui (PRD '20)]

# An LHC Test of Muon $g - 2$



[BD, Soni, Xu (2106.15647)]

- Mounting evidence for the violation of lepton flavor universality.  
[Crivellin, Hoferichter, 2111.1273 (Science '21)]
- Can be explained by invoking BSM physics (true for any anomaly).
- Leptoquarks and RPV-SUSY remain as the most attractive scenarios for a simultaneous explanation of  $B$ -anomalies and muon  $g - 2$ .
- Personal choice: **RPV3** – motivated by Higgs naturalness and other beautiful features of SUSY, while being consistent with null searches at the LHC.
  - Removes the accidental flavor symmetry of the SM.
  - Same chiral structure as the SM  $\implies$  correct  $D^*$  and  $\tau$  polarizations, as well as  $R_K - R_{K^{(*)}}$  correlation come automatically.
  - Highly predictive and testable at Belle II, LHCb and high- $p_T$  LHC experiments.
  - Improved lattice input for  $B \rightarrow K \nu \bar{\nu}$  and  $B_s - \bar{B}_s$  will be crucial.
  - **Flavor anomalies might be providing the first experimental hint of SUSY!**

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- Can be explained by invoking BSM physics (true for any anomaly).
- Leptoquarks and RPV-SUSY remain as the most attractive scenarios for a simultaneous explanation of  $B$ -anomalies and muon  $g - 2$ .
- Personal choice: **RPV3** – motivated by Higgs naturalness and other beautiful features of SUSY, while being consistent with null searches at the LHC.
  - Removes the accidental flavor symmetry of the SM.
  - Same chiral structure as the SM  $\implies$  correct  $D^*$  and  $\tau$  polarizations, as well as  $R_K - R_{K^{(*)}}$  correlation come automatically.
  - Highly predictive and testable at Belle II, LHCb and high- $p_T$  LHC experiments.
  - Improved lattice input for  $B \rightarrow K \nu \bar{\nu}$  and  $B_s - \bar{B}_s$  will be crucial.
  - **Flavor anomalies might be providing the first experimental hint of SUSY!**

**Thank You.**