



McDONNELL CENTER  
FOR THE SPACE SCIENCES

# Model One Size Fits All: A Minimal R-parity Violating Supersymmetric Model for the Flavor Anomalies, Muon $g - 2$ and ANITA

**Bhupal Dev**

*Washington University in St. Louis*

W. Altmannshofer, BD, A. Soni, Y. Sui, arXiv: 2002.12910 [hep-ph]

**PHENO 2020**

*University of Pittsburgh*

May 5, 2020

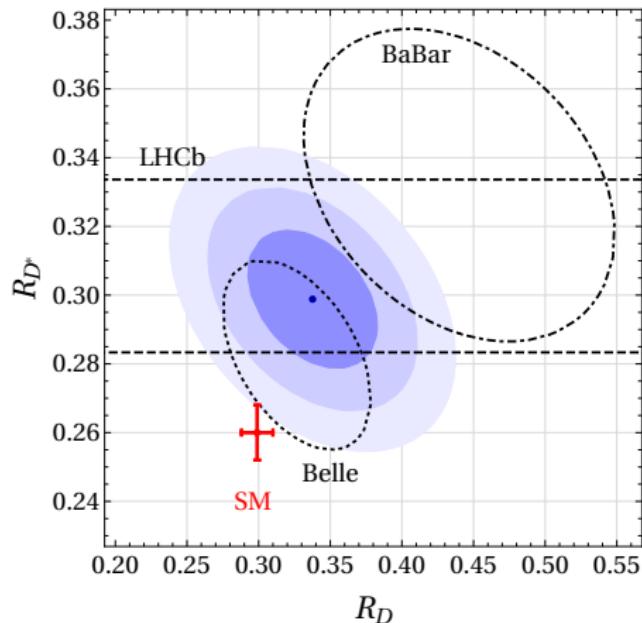
# Outline

- The Anomalies
- The RPV3 Framework
- Three Benchmark Cases
- Conclusion

# *B*-Anomalies

(see Flavor mini-review by J. Brod and LHCb plenary talk by K. Mueller)

$$R_{D^{(*)}} = \frac{\text{BR}(B \rightarrow D^{(*)}\tau\nu)}{\text{BR}(B \rightarrow D^{(*)}\ell\nu)} \quad (\text{with } \ell = e, \mu)$$

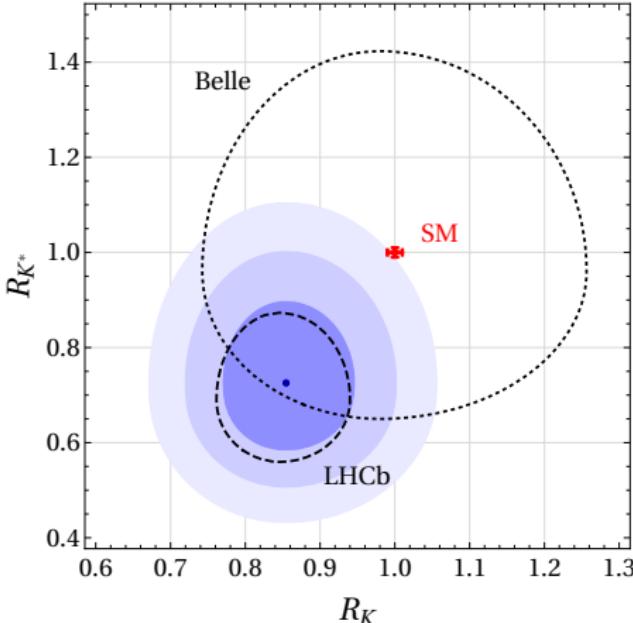
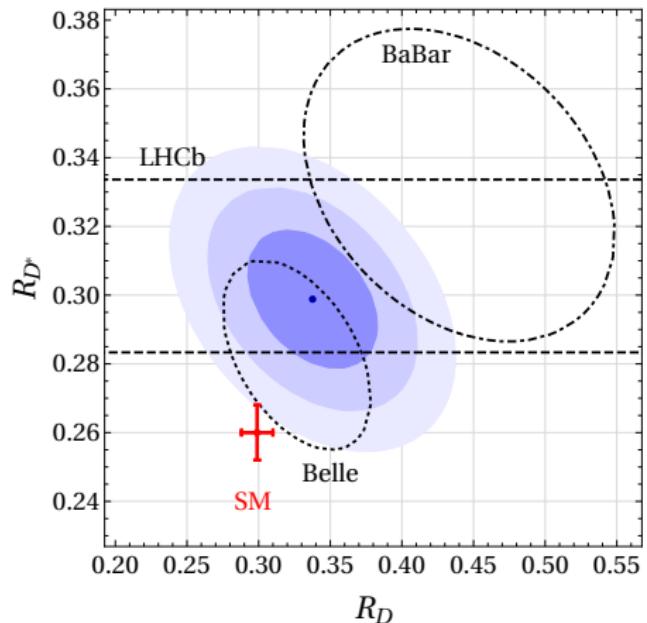


# B-Anomalies

(see Flavor mini-review by J. Brod and LHCb plenary talk by K. Mueller)

$$R_{D^{(*)}} = \frac{\text{BR}(B \rightarrow D^{(*)}\tau\nu)}{\text{BR}(B \rightarrow D^{(*)}\ell\nu)} \quad (\text{with } \ell = e, \mu)$$

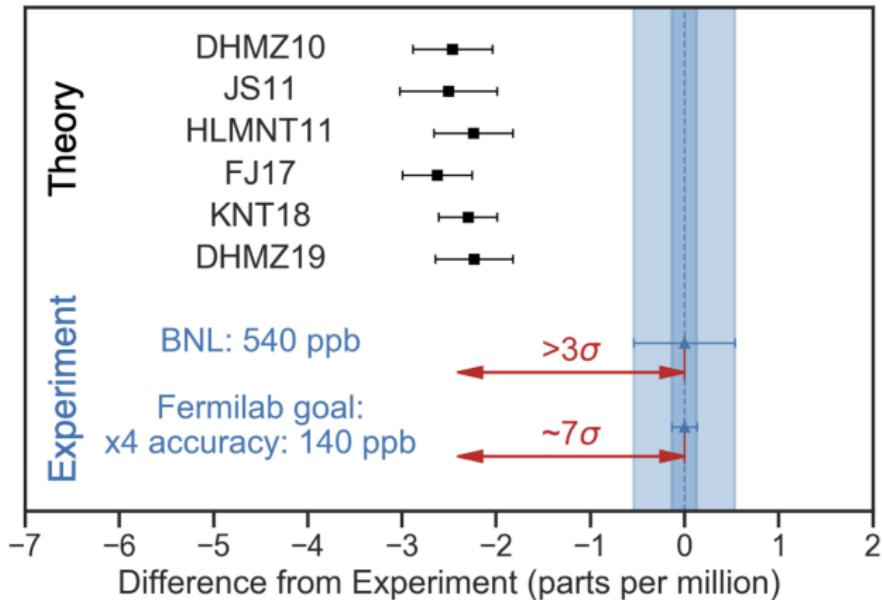
$$R_{K^{(*)}} = \frac{\text{BR}(B \rightarrow K^{(*)}\mu^+\mu^-)}{\text{BR}(B \rightarrow K^{(*)}e^+e^-)}$$



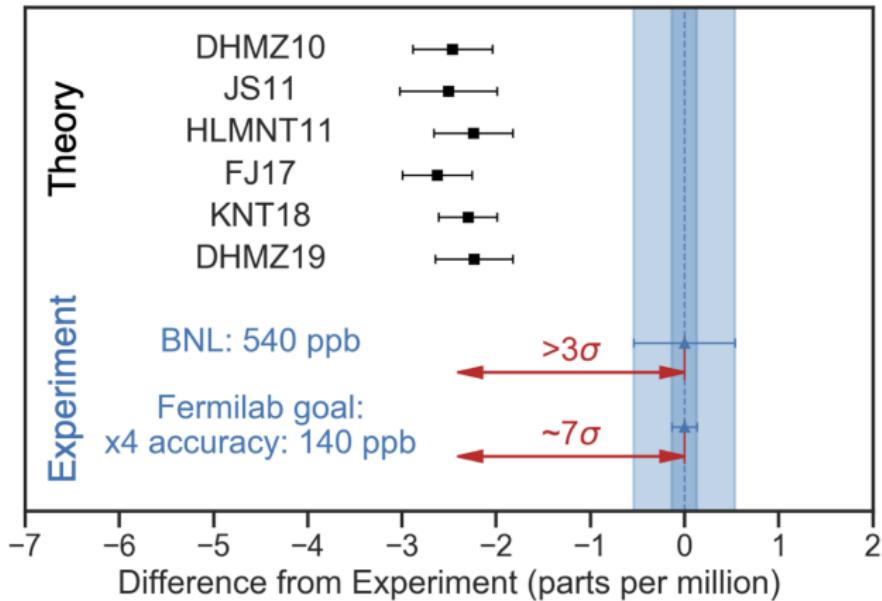
[Altmannshofer, BD, Soni, Sui '20]

# Muon $g - 2$

(see plenary talk by J. Kasper)



(see plenary talk by J. Kasper)



Observable	$R_{D^{(*)}}, R_{J/\psi}$	$R_{K^{(*)}}$	$(g - 2)_\mu$	All but $(g - 2)_\mu$	All
Pull	$3.3\sigma$ ( $2.2\sigma$ )	$3.4\sigma$	$3.3\sigma$	$4.5\sigma$ ( $3.7\sigma$ )	$5.3\sigma$ ( $4.6\sigma$ )

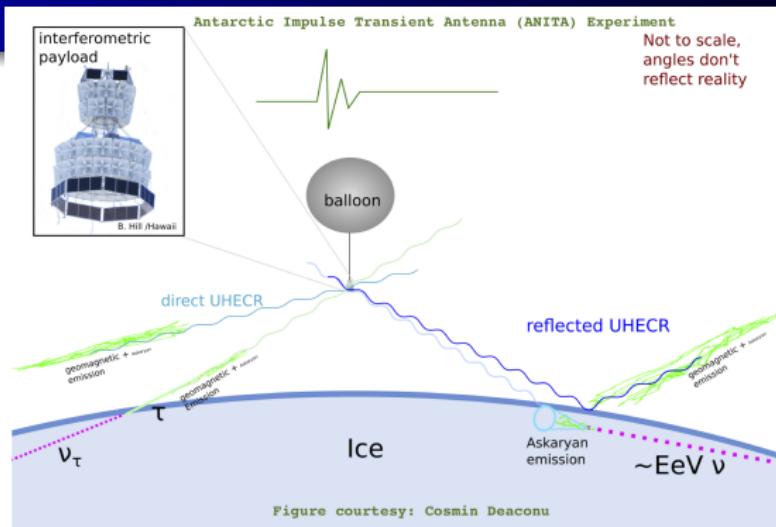


TABLE I: *ANITA-I,-III anomalous upward air showers.*  
**ANITA Collaboration, PRL'18**

event, flight	3985267, ANITA-I	15717147, ANITA-III
date, time	2006-12-28,00:33:20UTC	2014-12-20,08:33:22.5UTC
Lat., Lon. <sup>(1)</sup>	-82.6559, 17.2842	-81.39856, 129.01626
Altitude	2.56 km	2.75 km
Ice depth	3.53 km	3.22 km
El., Az.	$-27.4 \pm 0.3^\circ$ , $59.62 \pm 0.7^\circ$	$-35.0 \pm 0.3^\circ$ , $1.41 \pm 0.7^\circ$
RA, Dec <sup>(2)</sup>	$282.14064, +20.33043$	$50.78203, +38.65498$
$E_{shower}^{(3)}$	$0.6 \pm 0.4$ EeV	$0.56^{+0.3}_{-0.2}$ EeV

<sup>1</sup> Latitude, Longitude of the estimated ground position of the event.

<sup>2</sup> Sky coordinates projected from event arrival angles at ANITA.

<sup>3</sup> For upward shower initiation at or near ice surface.

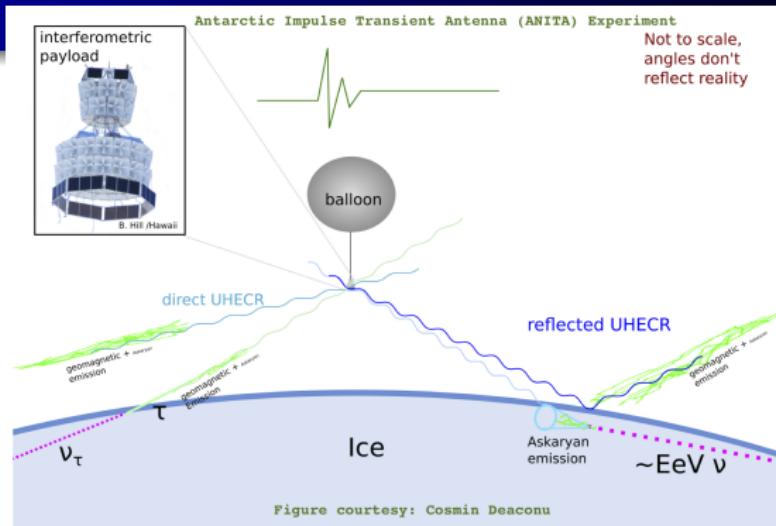


TABLE I: ANITA-I,-III anomalous upward air showers.  
ANITA Collaboration, PRL'18

event, flight	3985267, ANITA-I	15717147, ANITA-III
date, time	2006-12-28,00:33:20UTC	2014-12-20,08:33:22.5UTC
Lat., Lon. <sup>(1)</sup>	-82.6559, 17.2842	-81.39856, 129.01626
Altitude	2.56 km	2.75 km
Ice depth	3.53 km	3.22 km
El., Az.	$-27.4 \pm 0.3^\circ$ , $59.62 \pm 0.7^\circ$	$-35.0 \pm 0.3^\circ$ , $1.41 \pm 0.7^\circ$
RA, Dec <sup>(2)</sup>	$282.14064, +20.33043$	$50.78203, +38.65498$
$E_{\text{shower}}^{(3)}$	$0.6 \pm 0.4 \text{ EeV}$	$0.56^{+0.3}_{-0.2} \text{ EeV}$

<sup>1</sup> Latitude, Longitude of the estimated ground position of the event.

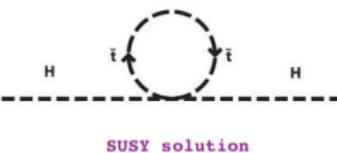
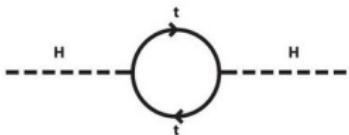
<sup>2</sup> Sky coordinates projected from event arrival angles at ANITA.

<sup>3</sup> For upward shower initiation at or near ice surface.

This talk: A SUSY solution to ANITA, muon  $g - 2$  and the  $B$ -anomalies!

# Natural SUSY

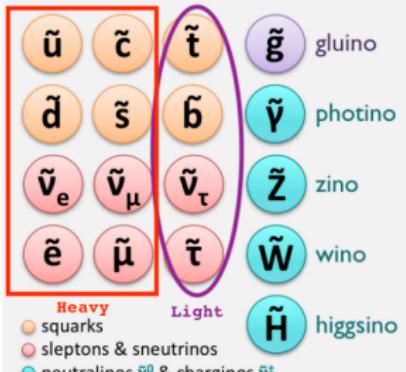
Gauge hierarchy problem



Standard Model particles



Supersymmetric partners



## Natural SUSY

[Papucci, Ruderman, Weiler (JHEP '12); Brust, Katz, Lawrence, Sundrum (JHEP '12)]

- More natural to include RPV couplings. [Brust, Katz, Lawrence, Sundrum (JHEP '12)]
- Preserves gauge coupling unification. [Altmannshofer, BD, Soni (PRD '17)]
- RPV3: RPV SUSY with light 3rd-generation sfermions.**
- Can naturally accommodate  $R_{D^{(*)}}$  ( $b \rightarrow c\tau\nu$ ) via  $LQD$  interactions. [Deshpande, He (EPJC '17); Altmannshofer, BD, Soni (PRD '17); Trifinopoulos (EPJC '18); Hu, Li, Muramatsu, Yang (PRD '19)]

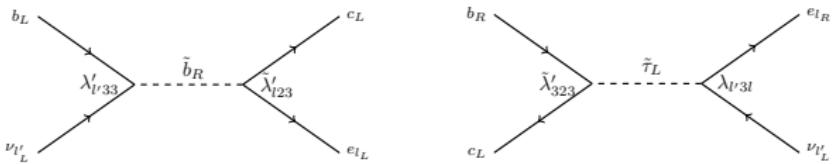
$$\mathcal{L}_{LQD} = \lambda'_{ijk} [\tilde{\nu}_{iL} \bar{d}_{kR} d_{jL} + \tilde{d}_{jL} \bar{d}_{kR} \nu_{iL} + \tilde{d}_{kR}^* \bar{\nu}_{iL}^c d_{jL} - \tilde{e}_{iL} \bar{d}_{kR} e_{jL} - \tilde{u}_{jL} \bar{d}_{kR} e_{iL} - \tilde{d}_{kR}^* \bar{e}_{iL}^c u_{jL}] + \text{H.c.}$$

- Can simultaneously explain  $R_{K^{(*)}}$  ( $b \rightarrow s\ell\ell$ ) by invoking  $LLE$  interactions, together with  $LQD$ . [Das, Hati, Kumar, Mahajan (PRD '17); Earl, Grégoire (JHEP '18); Trifinopoulos (EPJC '18); Hu, Huang (PRD '20); Altmannshofer, BD, Soni, Sui '20]

$$\mathcal{L}_{LLE} = \frac{1}{2} \lambda_{ijk} [\tilde{\nu}_{iL} \bar{e}_{kR} e_{jL} + \tilde{e}_{jL} \bar{e}_{kR} \nu_{iL} + \tilde{e}_{kR}^* \bar{\nu}_{iL}^c e_{jL} - (i \leftrightarrow j)] + \text{H.c.}$$

- Restricting to RPV3 and using some ansatz, we'll limit the number of independent  $\lambda'$  and  $\lambda$  couplings.

# $B$ -anomalies in RPV3



**Figure:** RPV3 contributions to  $R_{D^{(*)}}$ . [Deshpande, He (EPJC '17); Altmannshofer, BD, Soni (PRD '17); · · ·]

# $B$ -anomalies in RPV3

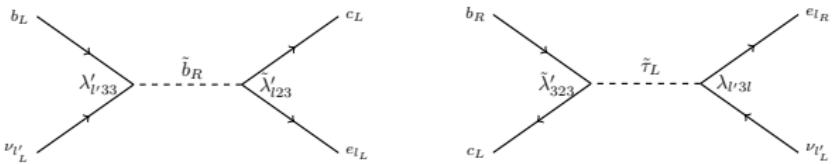


Figure: RPV3 contributions to  $R_{D^{(*)}}$ . [Deshpande, He (EPJC '17); Altmannshofer, BD, Soni (PRD '17); ···]

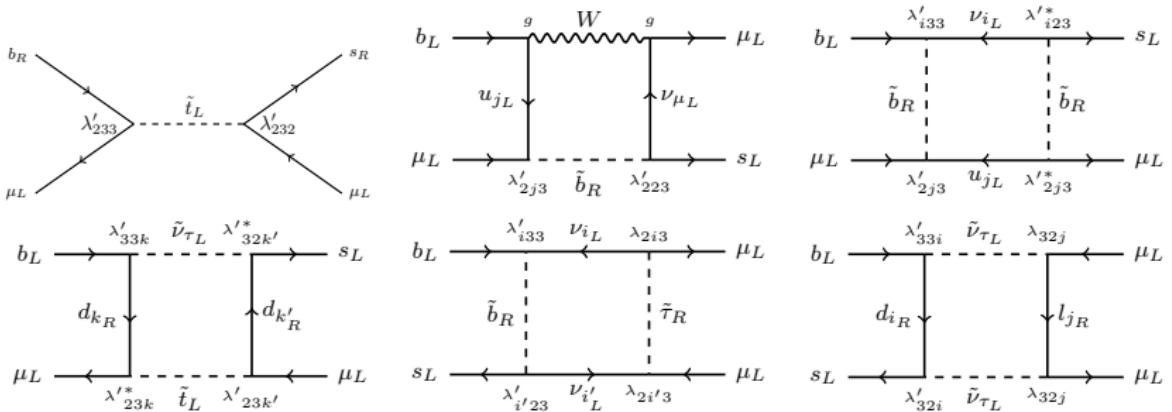


Figure: RPV3 contributions to  $R_{K^{(*)}}$ . [Das, Hati, Kumar, Mahajan (PRD '17); Trifinopoulos (EPJC '18)]

# Muon $g - 2$ and ANITA

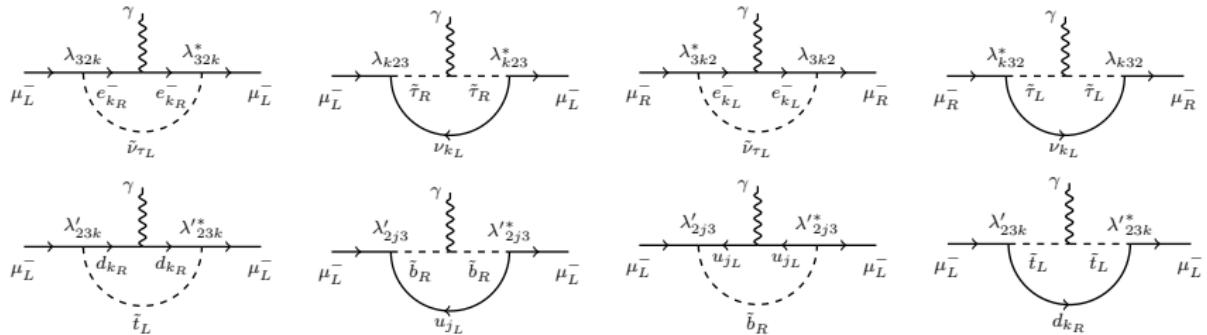


Figure: RPV3 contributions to  $(g - 2)_\mu$ . [Kim, Kyae, Lee (PLB '01)]

# Muon $g - 2$ and ANITA

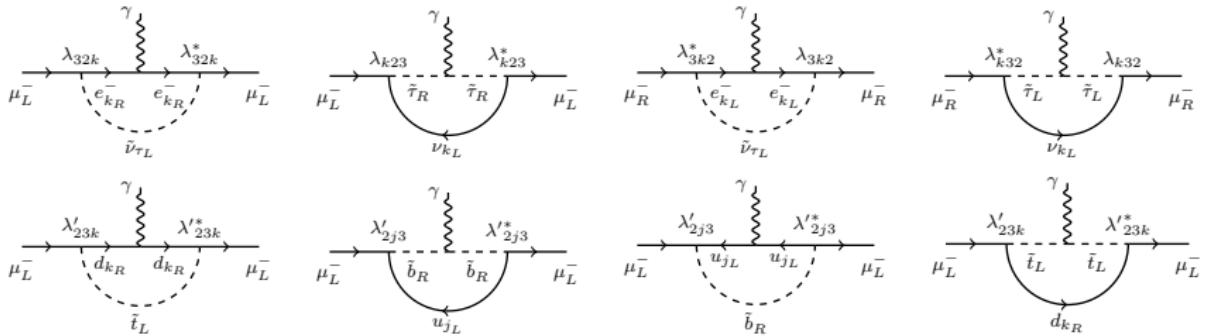


Figure: RPV3 contributions to  $(g - 2)_\mu$ . [Kim, Kyae, Lee (PLB '01)]

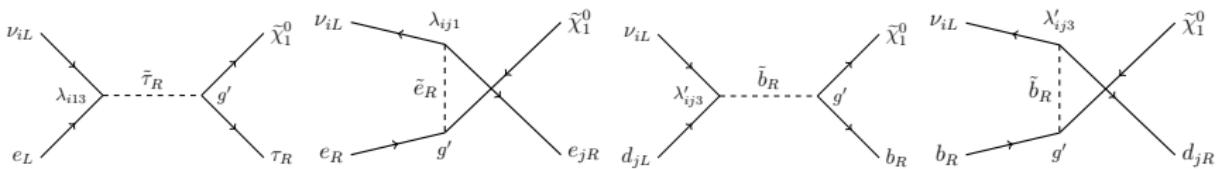


Figure: RPV3 contributions to ANITA anomalous events. [Collins, BD, Sui (PRD '19)]

## Three Benchmark Cases

- **Case 1: CKM-like Structure**

$$\lambda'_{ijk} = \lambda'_{333} \epsilon^{(3-i)+(3-j)+(3-k)}, \quad \lambda_{ijk} = \lambda_{233} \epsilon^{(2-i)+(3-j)+(3-k)}.$$

Only 3 independent coupling parameters:  $\{\lambda'_{333}, \lambda_{233}, \epsilon\}$ .

## Three Benchmark Cases

- **Case 1: CKM-like Structure**

$$\lambda'_{ijk} = \lambda'_{333} \epsilon^{(3-i)+(3-j)+(3-k)}, \quad \lambda_{ijk} = \lambda_{233} \epsilon^{(2-i)+(3-j)+(3-k)}.$$

Only 3 independent coupling parameters:  $\{\lambda'_{333}, \lambda_{233}, \epsilon\}$ .

- **Case 2:  $U(2)_q \times U(2)_\ell$  Flavor Symmetry**

$$\lambda'_{1jk} = \lambda'_{211} = \lambda'_{231} = \lambda'_{213} = \lambda'_{311} = \lambda'_{331} = \lambda'_{313} \simeq 0, \quad \lambda'_{233} \simeq \lambda' \epsilon_\ell,$$

$$\lambda'_{221} = \lambda'_{212} \simeq \lambda' \epsilon_\ell \epsilon'_q, \quad \lambda'_{321} = \lambda'_{312} \simeq \lambda' \epsilon'_q,$$

$$\lambda'_{222} = \lambda'_{223} = \lambda'_{232} \simeq \lambda' \epsilon_\ell \epsilon_q, \quad \lambda'_{322} = \lambda'_{323} = \lambda'_{332} \simeq \lambda' \epsilon_q,$$

$$\lambda_{121} = \lambda_{131} = \lambda_{133} \simeq 0, \quad \lambda_{123} = \lambda_{132} = \lambda_{231} \simeq \lambda \epsilon'_\ell,$$

$$\lambda_{232} \simeq \lambda \epsilon_{\ell S}, \quad \lambda_{122} \simeq \lambda \epsilon_\ell \epsilon'_\ell, \quad \lambda_{233} \simeq \lambda \epsilon_\ell,$$

where  $\epsilon_q \approx m_s/m_b \simeq 0.025$ ,  $\epsilon'_q \approx \epsilon_q \sqrt{m_d/m_s} \simeq 0.005$ ,  $\epsilon_\ell \simeq 1$ ,  $\epsilon'_\ell \simeq 0.004$  and  $\epsilon_{\ell S} \simeq 0.06$  [Trifinopoulos (EPJC '18)]. Again, 3 independent couplings:  $\{\lambda'_{333}, \lambda', \lambda\}$ .

## Three Benchmark Cases

- **Case 1: CKM-like Structure**

$$\lambda'_{ijk} = \lambda'_{333} \epsilon^{(3-i)+(3-j)+(3-k)}, \quad \lambda_{ijk} = \lambda_{233} \epsilon^{(2-i)+(3-j)+(3-k)}.$$

Only 3 independent coupling parameters:  $\{\lambda'_{333}, \lambda_{233}, \epsilon\}$ .

- **Case 2:  $U(2)_q \times U(2)_\ell$  Flavor Symmetry**

$$\lambda'_{1jk} = \lambda'_{211} = \lambda'_{231} = \lambda'_{213} = \lambda'_{311} = \lambda'_{331} = \lambda'_{313} \simeq 0, \quad \lambda'_{233} \simeq \lambda' \epsilon_\ell,$$

$$\lambda'_{221} = \lambda'_{212} \simeq \lambda' \epsilon_\ell \epsilon'_q, \quad \lambda'_{321} = \lambda'_{312} \simeq \lambda' \epsilon'_q,$$

$$\lambda'_{222} = \lambda'_{223} = \lambda'_{232} \simeq \lambda' \epsilon_\ell \epsilon_q, \quad \lambda'_{322} = \lambda'_{323} = \lambda'_{332} \simeq \lambda' \epsilon_q,$$

$$\lambda_{121} = \lambda_{131} = \lambda_{133} \simeq 0, \quad \lambda_{123} = \lambda_{132} = \lambda_{231} \simeq \lambda \epsilon'_\ell,$$

$$\lambda_{232} \simeq \lambda \epsilon_{\ell S}, \quad \lambda_{122} \simeq \lambda \epsilon_\ell \epsilon'_\ell, \quad \lambda_{233} \simeq \lambda \epsilon_\ell,$$

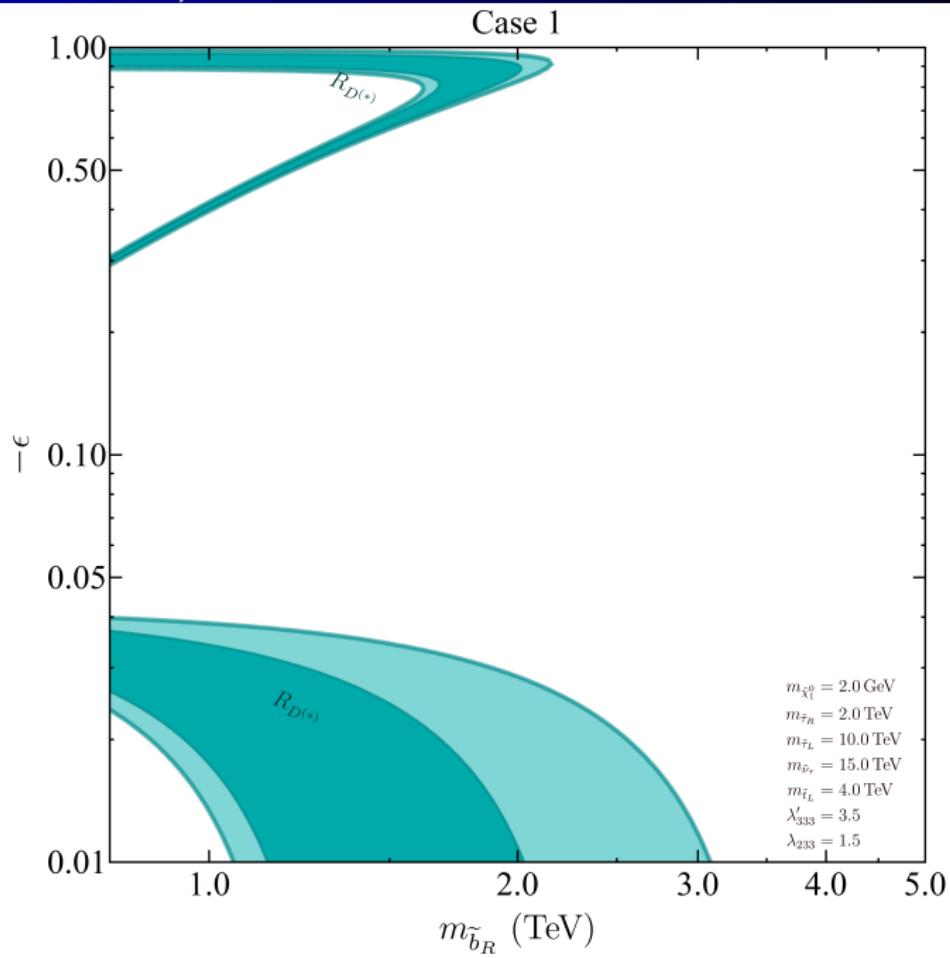
where  $\epsilon_q \approx m_s/m_b \simeq 0.025$ ,  $\epsilon'_q \approx \epsilon_q \sqrt{m_d/m_s} \simeq 0.005$ ,  $\epsilon_\ell \simeq 1$ ,  $\epsilon'_\ell \simeq 0.004$  and  $\epsilon_{\ell S} \simeq 0.06$  [Trifinopoulos (EPJC '18)]. Again, 3 independent couplings:  $\{\lambda'_{333}, \lambda', \lambda\}$ .

- **Case 3: No Symmetry** Also choose 3 independent couplings:

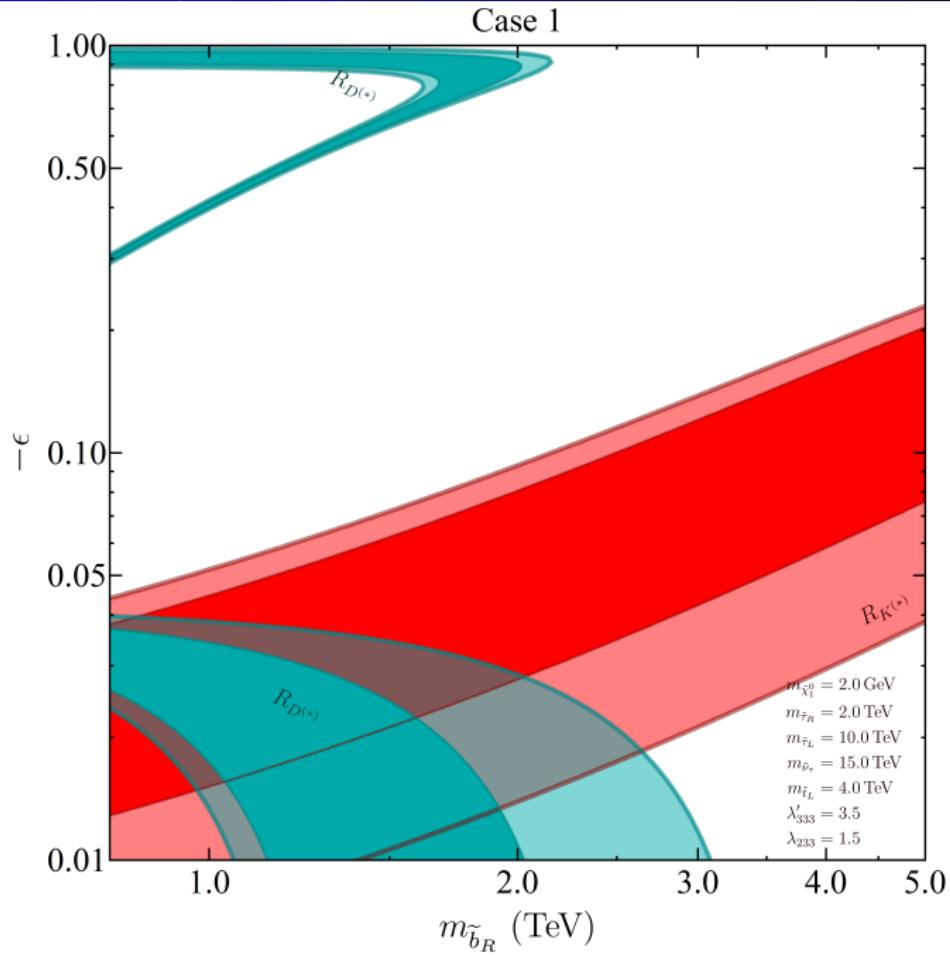
$$\{\lambda'_{223}, \quad \lambda' \equiv \lambda'_{123} = \lambda'_{233} = \lambda'_{323}, \quad \lambda \equiv \lambda_{132} = \lambda_{231} = \lambda_{232}\}.$$

- In each case, six free mass parameters:  $\{m_{\tilde{b}_R}, m_{\tilde{t}_L}, m_{\tilde{\tau}_L}, m_{\tilde{\tau}_R}, m_{\tilde{\nu}_\tau}, m_{\tilde{\chi}_1^0}\}$ .

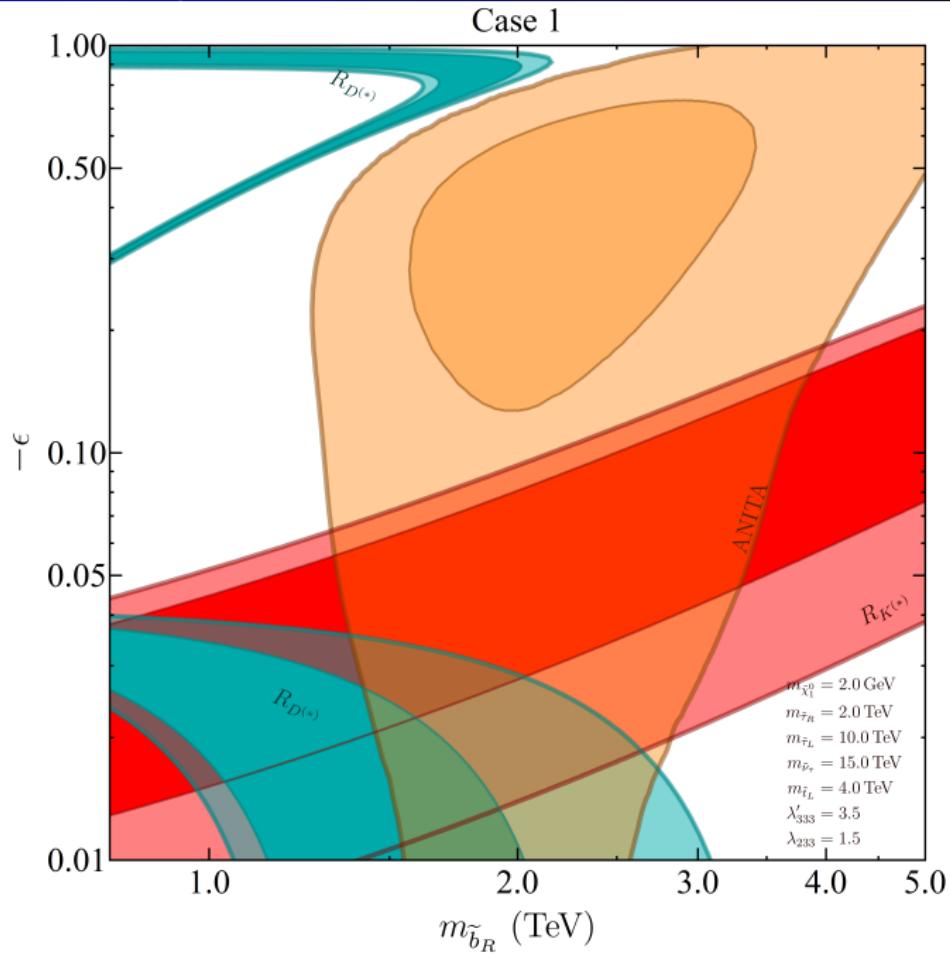
## Case 1 (CKM-Like)



# Case 1 (CKM-Like)

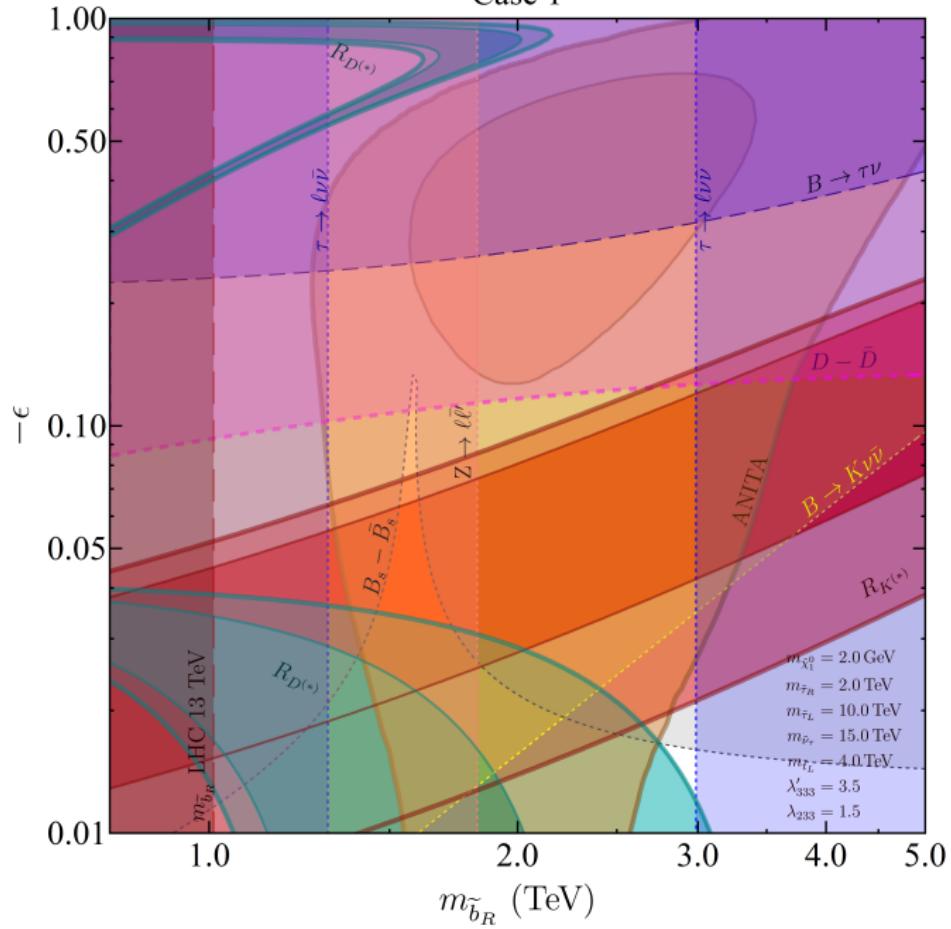


# Case 1 (CKM-Like)

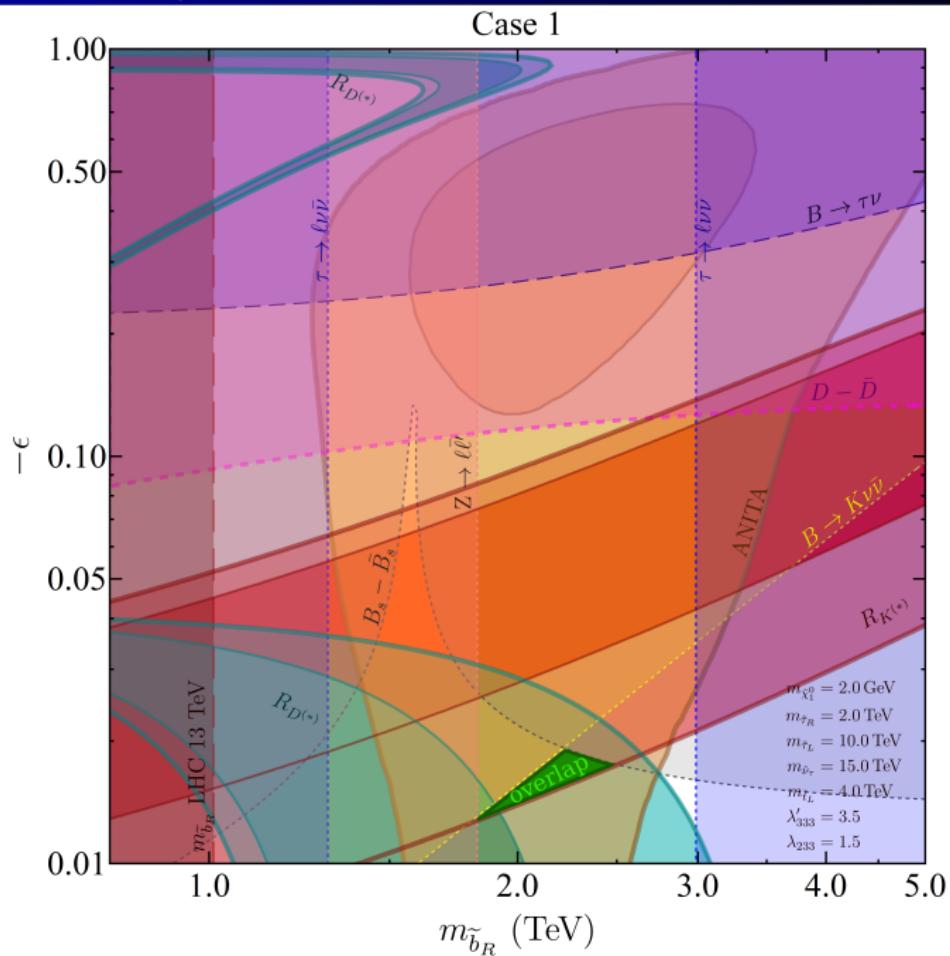


# Case 1 (CKM-Like)

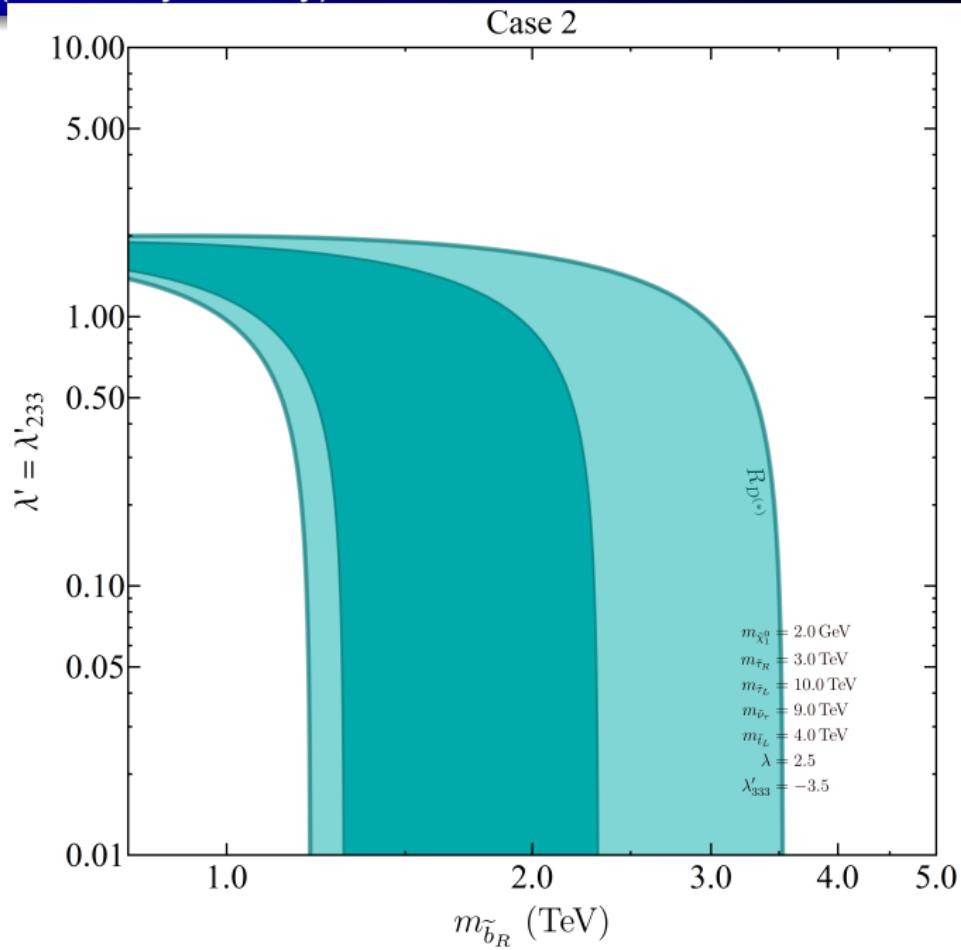
Case 1



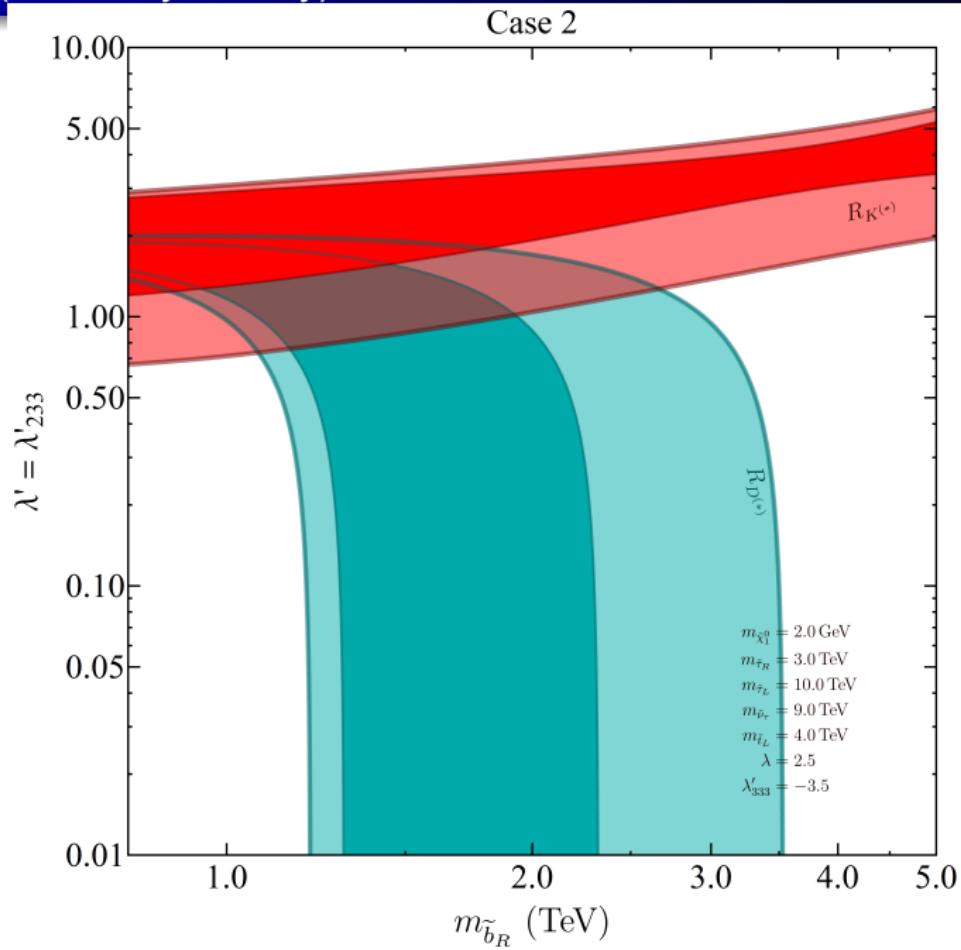
# Case 1 (CKM-Like)



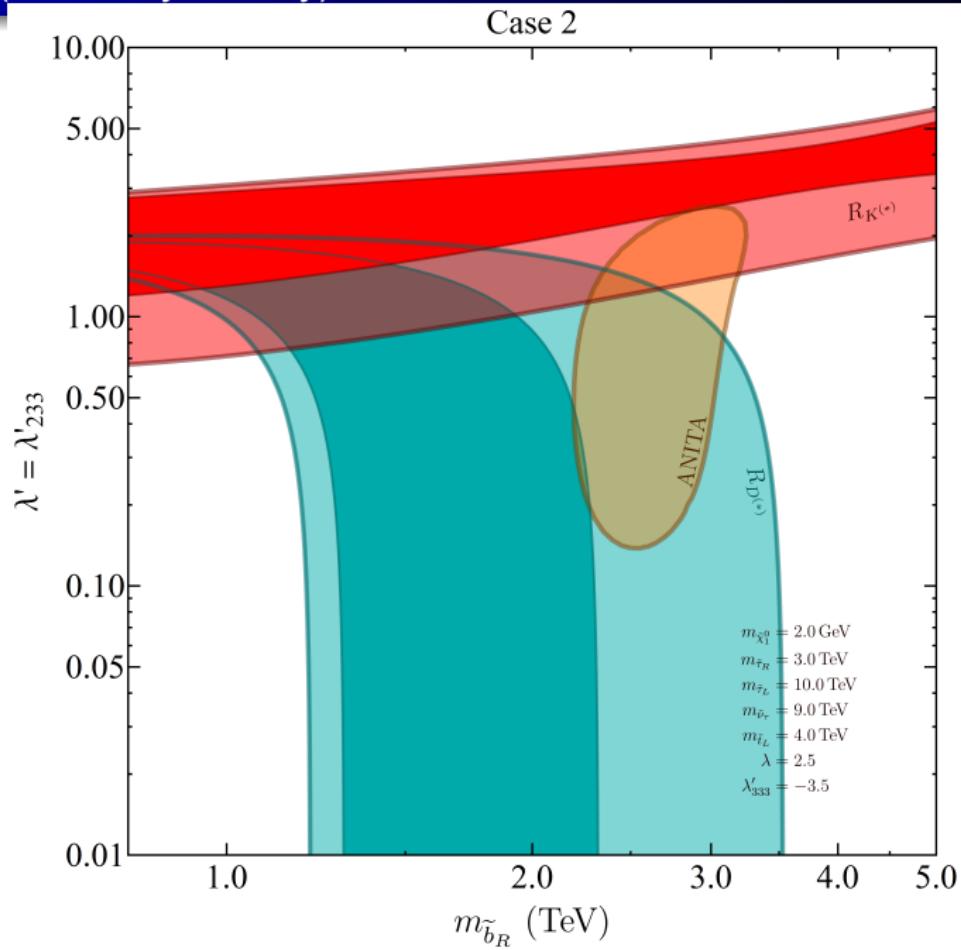
## Case 2 (Flavor Symmetry)



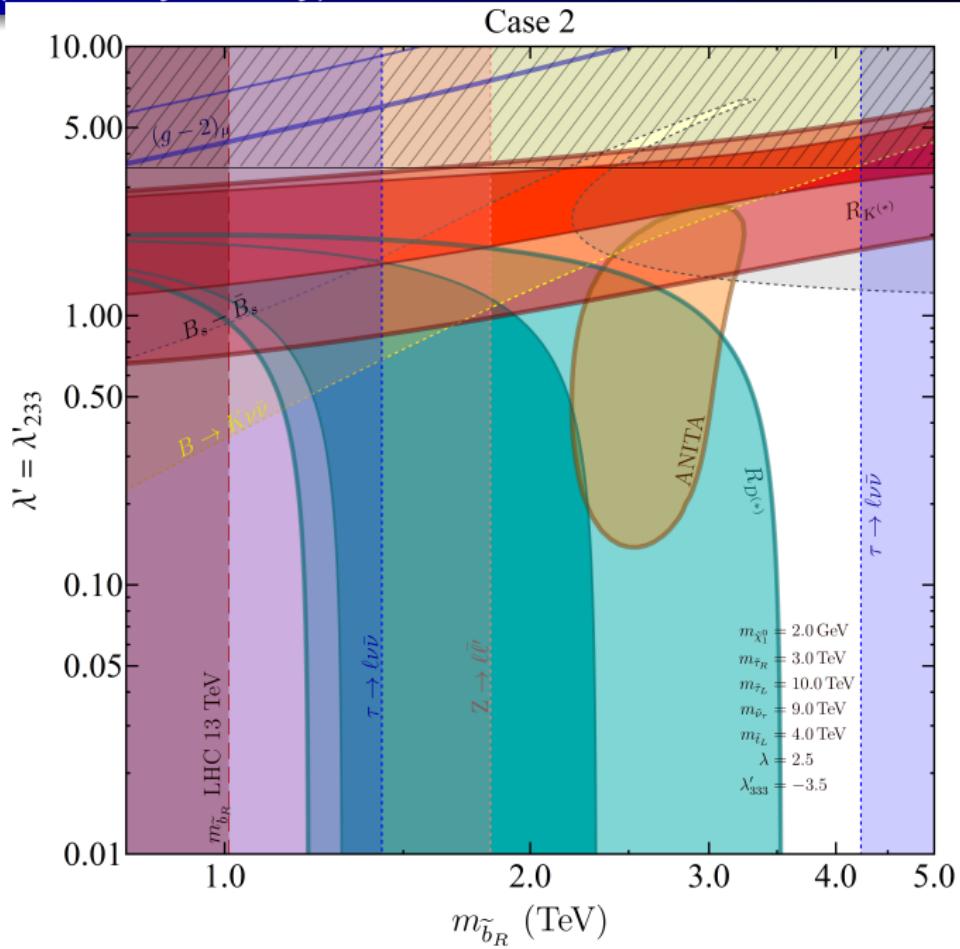
## Case 2 (Flavor Symmetry)



## Case 2 (Flavor Symmetry)

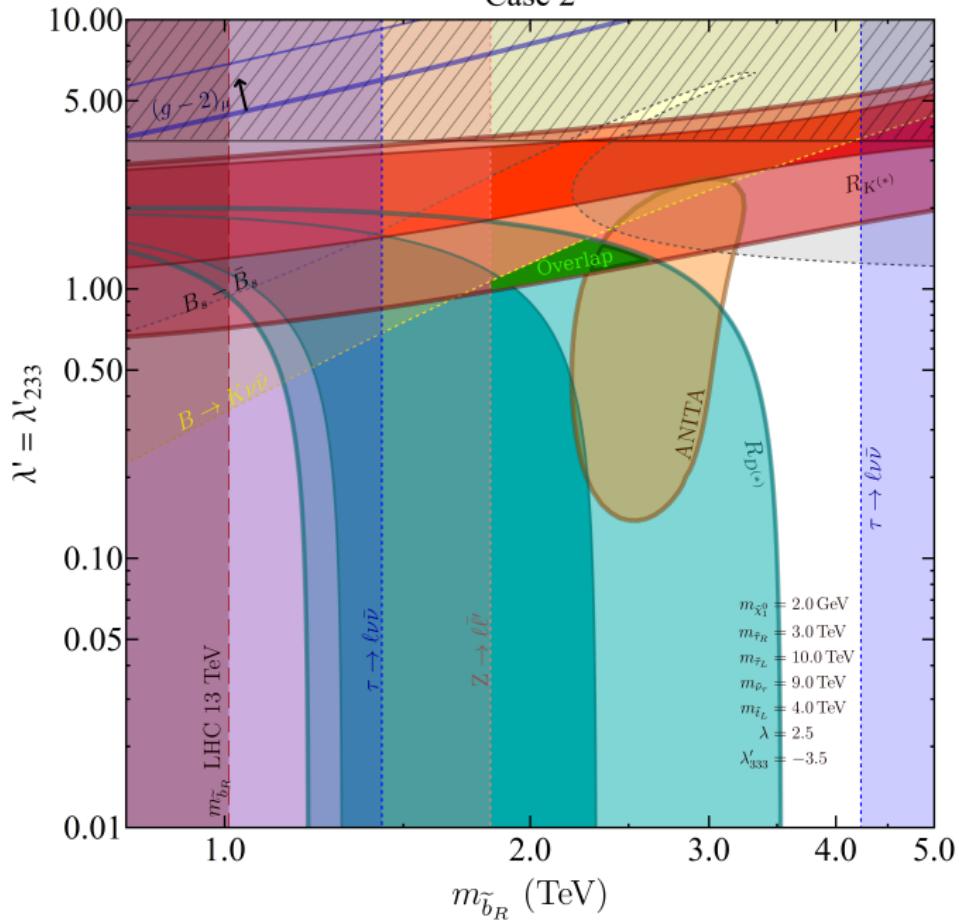


## Case 2 (Flavor Symmetry)

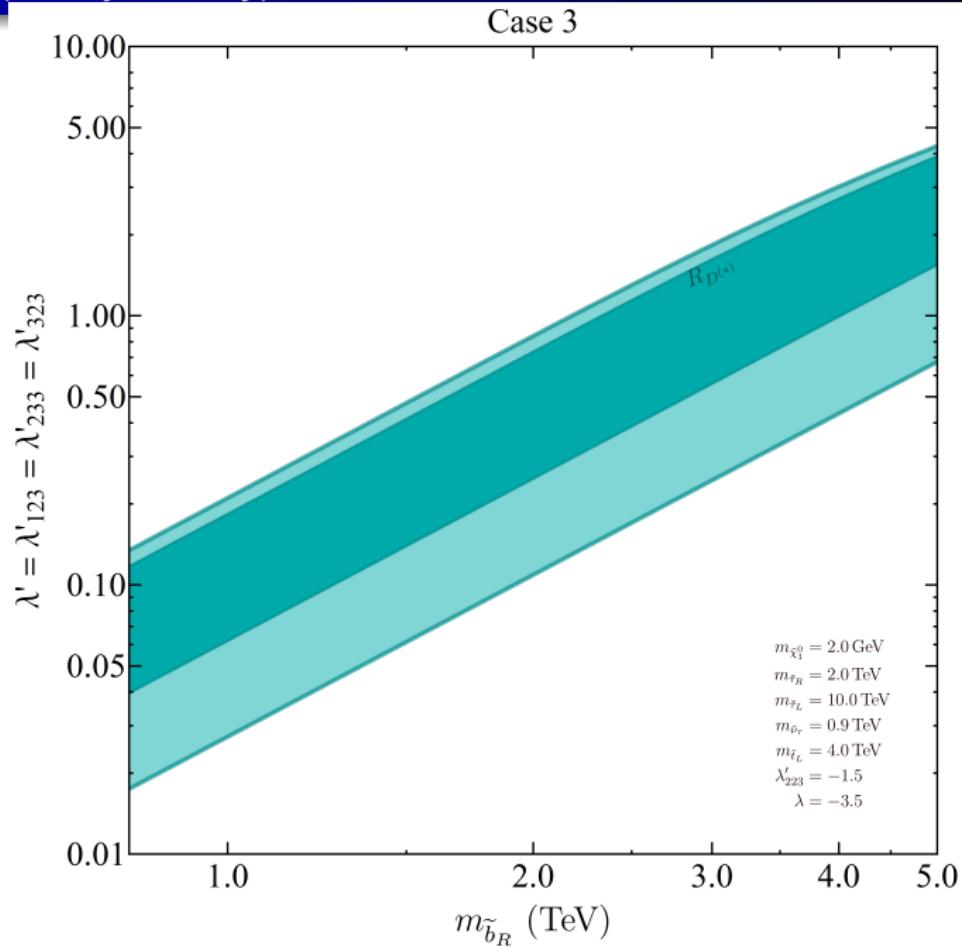


## Case 2 (Flavor Symmetry)

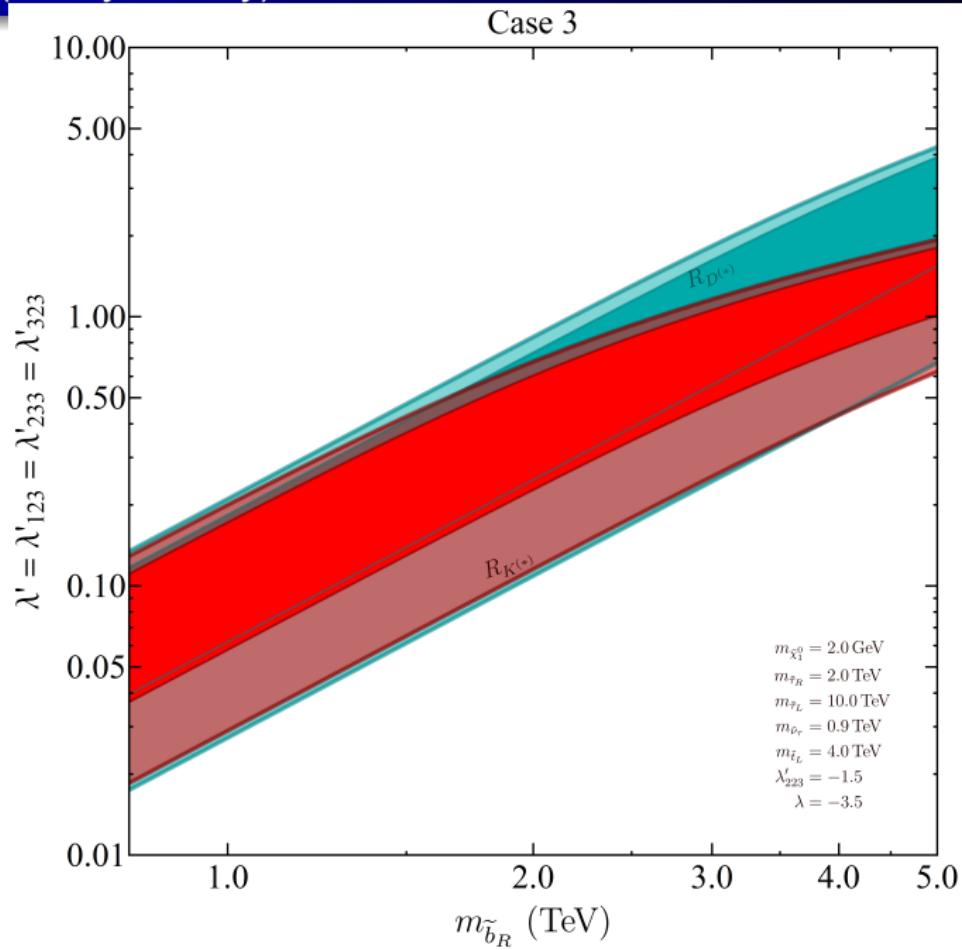
Case 2



## Case 3 (No Symmetry)

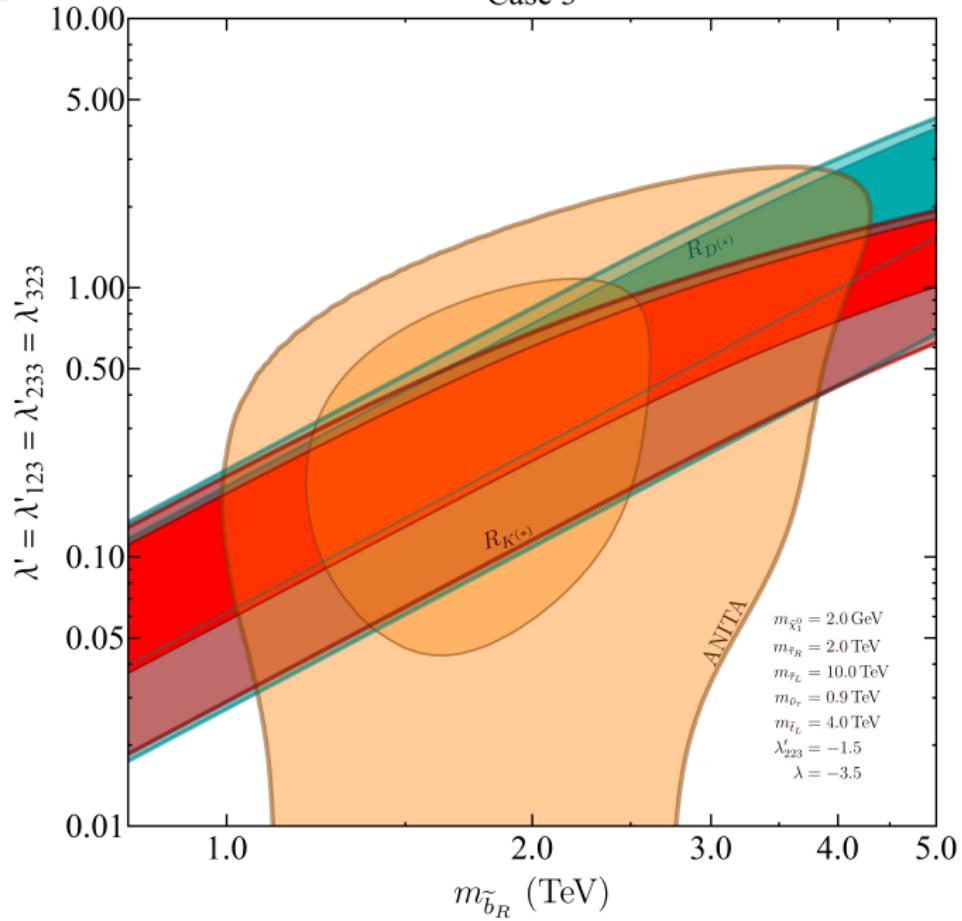


# Case 3 (No Symmetry)



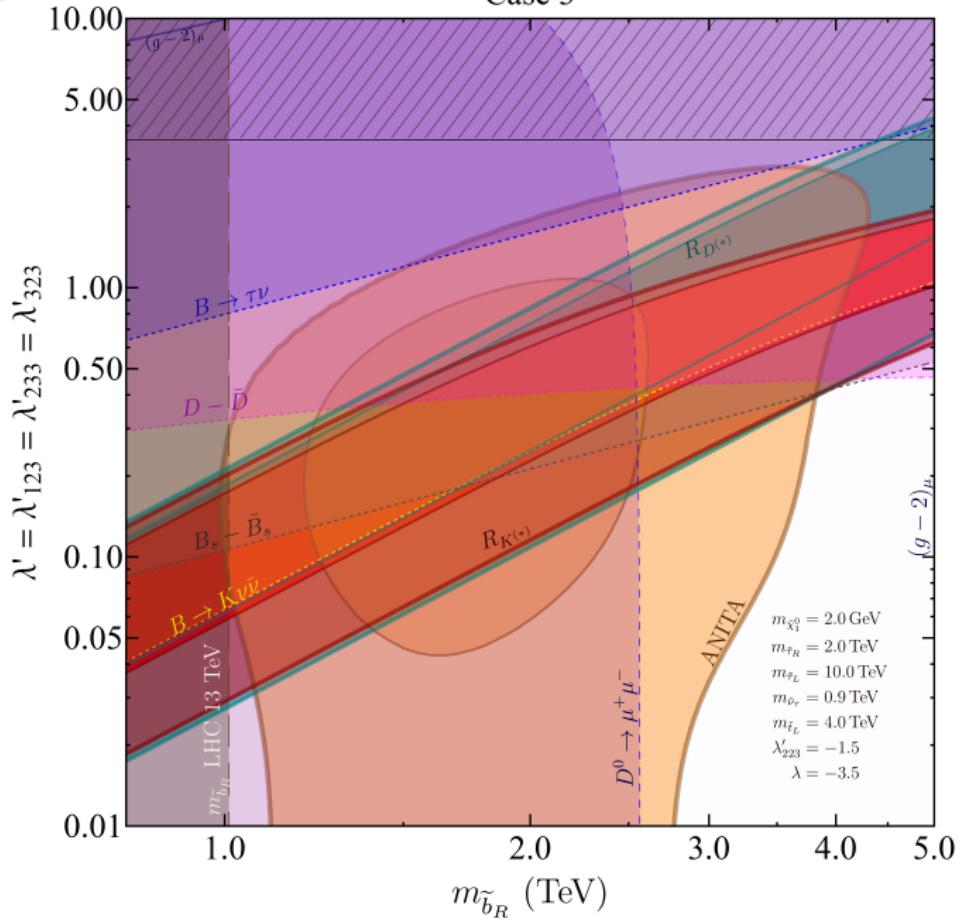
# Case 3 (No Symmetry)

Case 3

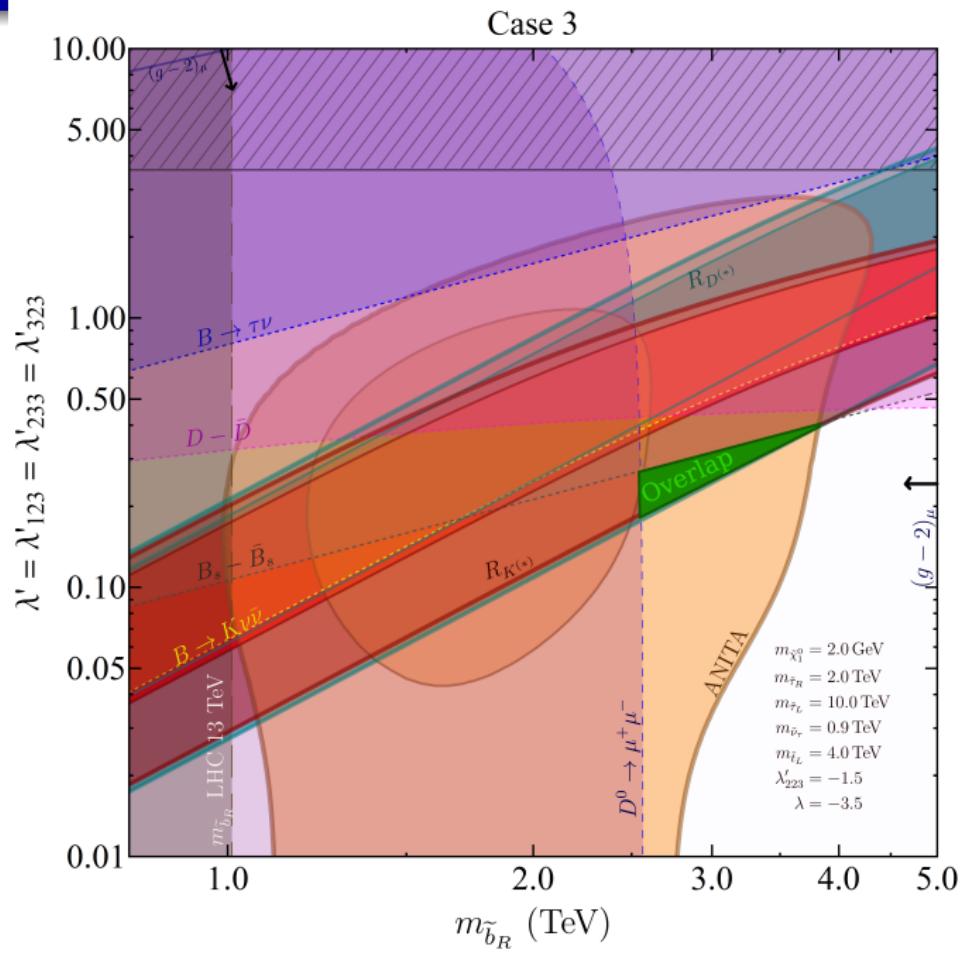


# Case 3 (No Symmetry)

Case 3



# Case 3 (No Symmetry)

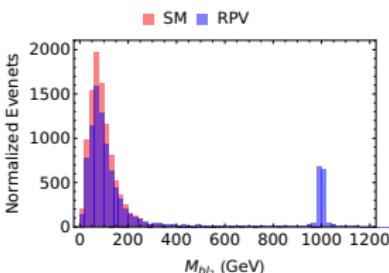
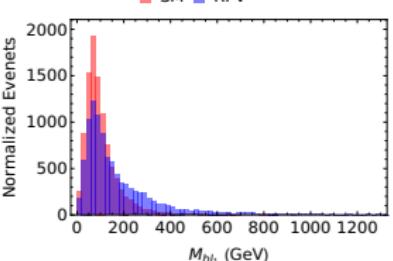
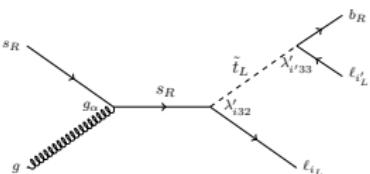


# Other Predictions

Flavor-violating decay mode	$\lambda, \lambda'$ dependence	RPV3 Prediction			Current experimental bound/measurement
		Case 1	Case 2	Case 3	
$\tau \rightarrow \mu\phi$	$\lambda'_{332}\lambda'_{232}, \lambda_{323}\lambda'_{322}$	$1.9 \times 10^{-15}$	$3.8 \times 10^{-10}$	$2.6 \times 10^{-12}$	$< 8.4 \times 10^{-8}$
$\tau \rightarrow \mu KK$	$\lambda'_{332}\lambda'_{232}, \lambda_{323}\lambda'_{322}$	$1.2 \times 10^{-17}$	$2.4 \times 10^{-12}$	$2.9 \times 10^{-13}$	$< 4.4 \times 10^{-8}$
$\tau \rightarrow \mu K_s^0$	$\lambda'_{332}\lambda'_{231}, \lambda'_{312}\lambda_{323}$	$4.5 \times 10^{-19}$	$8.7 \times 10^{-12}$	$3.1 \times 10^{-13}$	$< 2.3 \times 10^{-8}$
$\tau \rightarrow \mu\gamma$	$\lambda'_{333}\lambda'_{233}, \lambda_{133}\lambda_{123}$	$1.3 \times 10^{-10}$	$1.3 \times 10^{-8}$	$2.4 \times 10^{-10}$	$< 4.4 \times 10^{-8}$
$\tau \rightarrow \mu\mu\mu$	$\lambda_{323}\lambda_{322}$	$1.7 \times 10^{-11}$	$1.2 \times 10^{-9}$	$1.2 \times 10^{-11}$	$< 2.1 \times 10^{-8}$
$B_{(s)} \rightarrow K^{(*)}(\phi)\mu\tau$	$\lambda'_{333}\lambda'_{232}, \lambda'_{233}\lambda'_{332}, \lambda'_{332}\lambda_{323}$	$4.1 \times 10^{-9}$	$1.2 \times 10^{-7}$	$2.2 \times 10^{-10}$	$< 2.8 \times 10^{-5}$
$B_s \rightarrow \tau\mu$	$\lambda'_{333}\lambda'_{232}, \lambda'_{233}\lambda'_{332}, \lambda'_{332}\lambda_{323}$	$4.4 \times 10^{-10}$	$1.3 \times 10^{-8}$	$2.3 \times 10^{-11}$	$< 3.4 \times 10^{-5}$
$b \rightarrow s\tau\tau$	$\lambda'_{333}\lambda'_{332}$	$3.4 \times 10^{-7}$	$2.8 \times 10^{-8}$	$1.3 \times 10^{-13}$	N/A
$B \rightarrow K^{(*)}\tau\tau$	$\lambda'_{333}\lambda'_{332}$	$3.7 \times 10^{-6}$	$4.2 \times 10^{-8}$	$9.6 \times 10^{-12}$	$< 2.2 \times 10^{-3}$
$B_s \rightarrow \tau\tau$	$\lambda'_{333}\lambda'_{332}$	$3.7 \times 10^{-8}$	$3.0 \times 10^{-9}$	$1.4 \times 10^{-14}$	$< 6.8 \times 10^{-3}$
$b \rightarrow s\mu\mu$	$\lambda'_{233}\lambda'_{232}, \lambda'_{332}\lambda_{232}$	$5.9 \times 10^{-9}$	$3.2 \times 10^{-8}$	$8.8 \times 10^{-9}$	$4.4 \times 10^{-6}$
$B_s \rightarrow \mu\mu$	$\lambda'_{233}\lambda'_{232}, \lambda'_{332}\lambda_{232}$	$4.1 \times 10^{-11}$	$6.5 \times 10^{-11}$	$1.8 \times 10^{-11}$	$3.0 \times 10^{-9}$

# Other Predictions

Flavor-violating decay mode	$\lambda, \lambda'$ dependence	RPV3 Prediction			Current experimental bound/measurement
		Case 1	Case 2	Case 3	
$\tau \rightarrow \mu\phi$	$\lambda'_{332}\lambda'_{232}, \lambda_{323}\lambda'_{322}$	$1.9 \times 10^{-15}$	$3.8 \times 10^{-10}$	$2.6 \times 10^{-12}$	$< 8.4 \times 10^{-8}$
$\tau \rightarrow \mu KK$	$\lambda'_{332}\lambda'_{232}, \lambda_{323}\lambda'_{322}$	$1.2 \times 10^{-17}$	$2.4 \times 10^{-12}$	$2.9 \times 10^{-13}$	$< 4.4 \times 10^{-8}$
$\tau \rightarrow \mu K_s^0$	$\lambda'_{332}\lambda'_{231}, \lambda'_{312}\lambda_{323}$	$4.5 \times 10^{-19}$	$8.7 \times 10^{-12}$	$3.1 \times 10^{-13}$	$< 2.3 \times 10^{-8}$
$\tau \rightarrow \mu\gamma$	$\lambda'_{333}\lambda'_{233}, \lambda_{133}\lambda_{123}$	$1.3 \times 10^{-10}$	$1.3 \times 10^{-8}$	$2.4 \times 10^{-10}$	$< 4.4 \times 10^{-8}$
$\tau \rightarrow \mu\mu\mu$	$\lambda_{323}\lambda'_{322}$	$1.7 \times 10^{-11}$	$1.2 \times 10^{-9}$	$1.2 \times 10^{-11}$	$< 2.1 \times 10^{-8}$
$B_{(s)} \rightarrow K^{(*)}(\phi)\mu\tau$	$\lambda'_{333}\lambda'_{232}, \lambda'_{233}\lambda'_{332}, \lambda'_{332}\lambda_{323}$	$4.1 \times 10^{-9}$	$1.2 \times 10^{-7}$	$2.2 \times 10^{-10}$	$< 2.8 \times 10^{-5}$
$B_s \rightarrow \tau\mu$	$\lambda'_{333}\lambda'_{232}, \lambda'_{233}\lambda'_{332}, \lambda'_{332}\lambda_{323}$	$4.4 \times 10^{-10}$	$1.3 \times 10^{-8}$	$2.3 \times 10^{-11}$	$< 3.4 \times 10^{-5}$
$b \rightarrow s\tau\tau$	$\lambda'_{333}\lambda'_{332}$	$3.4 \times 10^{-7}$	$2.8 \times 10^{-8}$	$1.3 \times 10^{-13}$	N/A
$B \rightarrow K^{(*)}\tau\tau$	$\lambda'_{333}\lambda'_{332}$	$3.7 \times 10^{-6}$	$4.2 \times 10^{-8}$	$9.6 \times 10^{-12}$	$< 2.2 \times 10^{-3}$
$B_s \rightarrow \tau\tau$	$\lambda'_{333}\lambda'_{332}$	$3.7 \times 10^{-8}$	$3.0 \times 10^{-9}$	$1.4 \times 10^{-14}$	$< 6.8 \times 10^{-3}$
$b \rightarrow s\mu\mu$	$\lambda'_{233}\lambda'_{232}, \lambda'_{332}\lambda_{232}$	$5.9 \times 10^{-9}$	$3.2 \times 10^{-8}$	$8.8 \times 10^{-9}$	$4.4 \times 10^{-6}$
$B_s \rightarrow \mu\mu$	$\lambda'_{233}\lambda'_{232}, \lambda'_{332}\lambda_{232}$	$4.1 \times 10^{-11}$	$6.5 \times 10^{-11}$	$1.8 \times 10^{-11}$	$3.0 \times 10^{-9}$



A more dedicated LHC analysis underway.

## Conclusion

- Analyzed the possibility of a common origin of the  $B$ -anomalies, muon  $g - 2$ , and ANITA anomaly in a single testable framework.
- Third-generation-centric RPV SUSY framework ([RPV3](#)), motivated by Higgs naturalness.
- Three benchmark cases, each with 9 parameters only.
- Remarkably, allowed overlap regions for all the anomalies still exist.
- Predictions for flavor-violating  $B$ -meson and tau decays could be tested at Belle II and LHCb.
- Complementary tests in the high- $p_T$  LHC experiments.

## Conclusion

- Analyzed the possibility of a common origin of the  $B$ -anomalies, muon  $g - 2$ , and ANITA anomaly in a single testable framework.
- Third-generation-centric RPV SUSY framework ([RPV3](#)), motivated by Higgs naturalness.
- Three benchmark cases, each with 9 parameters only.
- Remarkably, allowed overlap regions for all the anomalies still exist.
- Predictions for flavor-violating  $B$ -meson and tau decays could be tested at Belle II and LHCb.
- Complementary tests in the high- $p_T$  LHC experiments.

**Thank You.**