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FOR THE SPACE SCIENCES

# A multi-messenger probe of the nature of neutrino mass

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*Washington University in St. Louis*



in collaboration with



Kiara Carloni, Ivan Martínez-Soler, Carlos Argüelles, and Kaladi Babu,

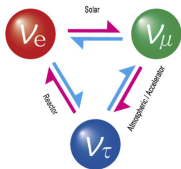
arXiv: 2212.00737 [astro-ph.HE]

The Mitchell Conference on Collider, Dark Matter, and Neutrino Physics

*Texas A&M University, College Station*

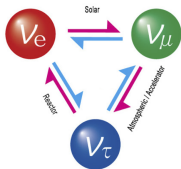
May 17, 2023

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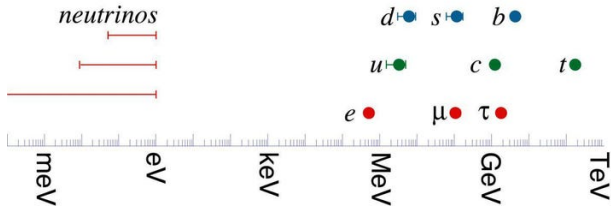


$\Rightarrow$  **Nonzero Neutrino Mass**  $\Rightarrow$  **BSM Physics**

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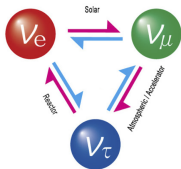


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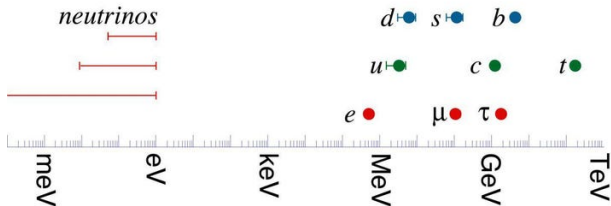


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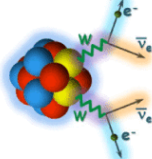
Majorana or Dirac (or something in between)?

Only experiments can tell.

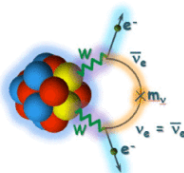


# $0\nu\beta\beta$ experiments ... maybe?

[Double beta decay]

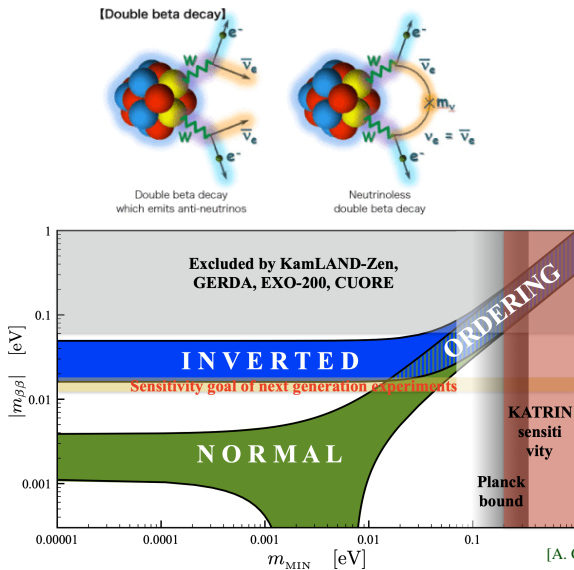


Double beta decay  
which emits anti-neutrinos

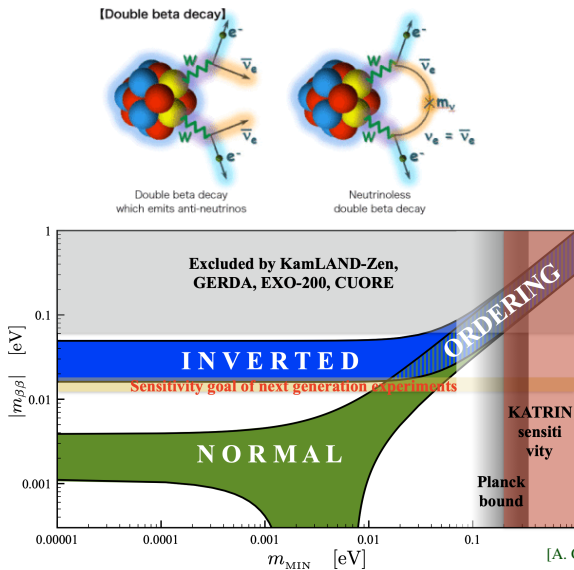


Neutrinoless  
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- If  $M_R = 0$ , lepton number is preserved and neutrinos are **Dirac**.
  - If  $M_R \neq 0$ , neutrinos are **Majorana**.
  - If  $||M_R|| \ll ||m_D||$ , neutrinos are **pseudo-Dirac** (small active-sterile mass splitting).
- But isn't it more natural to have  $||M_R|| \gg ||m_D||$  (**seesaw**)?

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- Maybe, but  $\|M_R\| \ll \|m_D\|$  is a logical possibility too.

[Wolfenstein (NPB '81); Petcov (PLB '82); Valle (PRD '82); Valle, Singer (PRD '83); Kobayashi, Lim (PRD '01)]

# Models of pseudo-Dirac neutrinos

- A good starting point: Dirac neutrino models with  $m_D$  naturally small and  $M_R = 0$  at renormalizable level, e.g. in **Dirac seesaw**. [Roncadelli, Wyler (PLB '83); Roy, Shanker (PRL '84); Dick, Lindner, Ratz, Wright (PRL '00); Murayama, Pierce (PRL '02); Gu, He (JCAP '06); Joshipura, Mohanty, Pakvasa (PRD '14); Ma, Srivastava (PLB '15); Ma, Popov (PLB '17); Earl, Fong, Gregoire, Tonero (JCAP '20); ...]
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- Global lepton number symmetry.
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- Weinberg operators  $(\Psi\Psi HH)/M_{\text{Pl}}$  and  $(\Psi'\Psi'H'H')/M_{\text{Pl}}$  induce small diagonal  $M_\nu$  entries  $\implies$  **Pseudo-Dirac neutrinos**.
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- **But excluded by BBN and solar neutrino constraints (for maximal mixing).** ☹  
 $\delta m^2 \lesssim 10^{-8} \text{ eV}^2$  from BBN, [Barbieri, Dolgov (PLB '90)]  
 $10^{-11} \text{ eV}^2$  from solar. [de Gouvêa, Huang, Jenkins (PRD '09); Ansarifard, Farzan (PRD '23)]

## Models of pseudo-Dirac neutrinos

- An alternative is to gauge  $B - L$ .
- Introduce a singlet scalar  $S$  carrying two units of  $B - L$ .
- Lowest-order quantum gravity corrections are of the form  $(\Psi\Psi HHS)/M_{\text{Pl}}^2$ .
- For  $\langle S \rangle = v_{BL}$ , leads to diagonal elements of  $M_\nu$  of order  $v^2 v_{BL}/M_{\text{Pl}}^2$ .
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- Concrete prediction for  $\Delta N_{\text{eff}} \simeq 0.14$ . [Babu, He, Su, Thapa, 2205.09127 (JHEP '22)]
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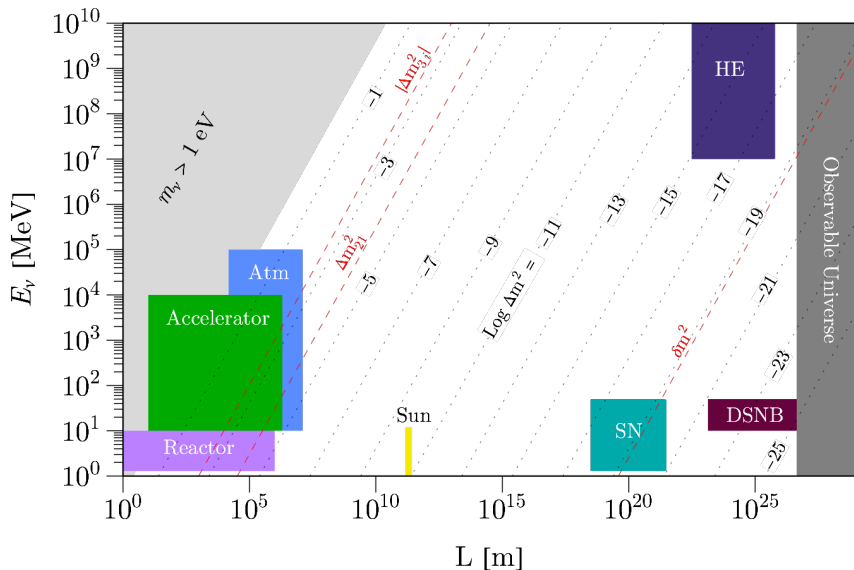
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## How to probe these tiny $\delta m^2$ values?

Oscillation effects are suppressed, unless  $L$  and  $E$  are such that  $\delta m^2 L/E \sim 1$ .



# Need astrophysical baselines



# Supernova neutrino constraints

$$P_{aa}(E_\nu) = \frac{1}{2} \left( 1 + e^{-\left(\frac{L}{L_{\text{coh}}}\right)^2} \cos\left(\frac{2\pi L}{L_{\text{osc}}}\right) \right).$$

$$L_{\text{osc}} = \frac{4\pi E_\nu}{\delta m^2} \approx 20 \text{ kpc} \left( \frac{E_\nu}{25 \text{ MeV}} \right) \left( \frac{10^{-19} \text{ eV}^2}{\delta m^2} \right),$$

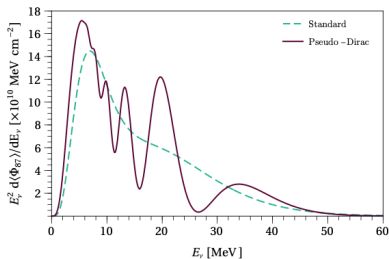
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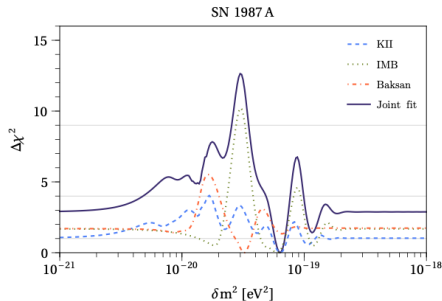
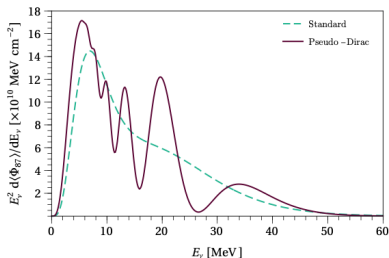


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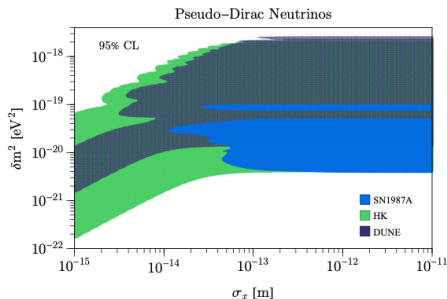
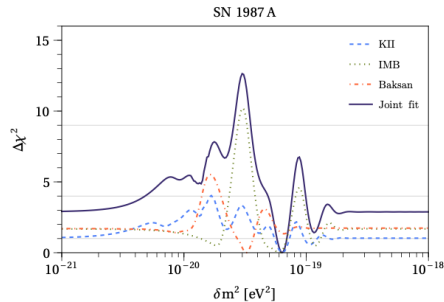
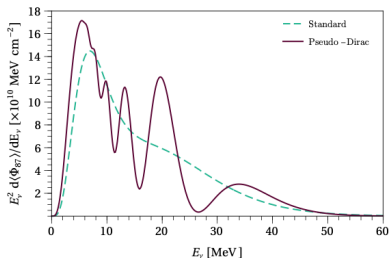


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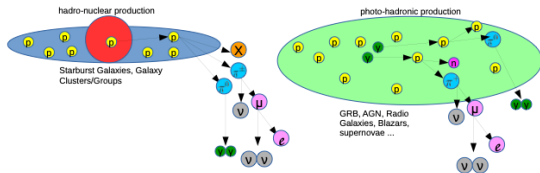
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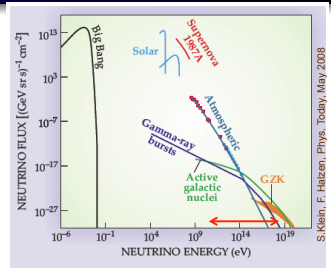
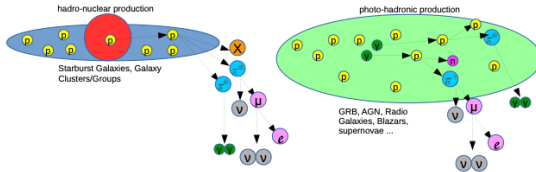
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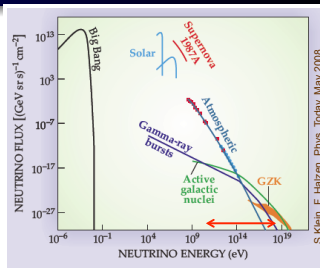
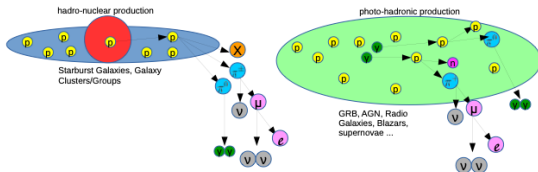
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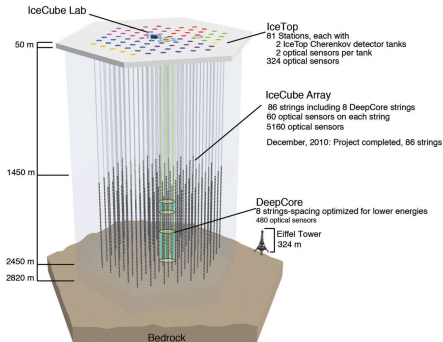


# Astrophysical neutrinos



S.Klein, F. Halzen, Phys. Today, May 2008

**Need gigantic detectors to compensate for the tiny flux.**



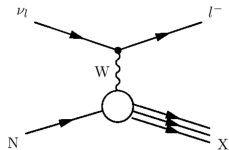


# High-energy neutrino signals at IceCube

$$\nu_\ell + N \rightarrow \begin{cases} \ell + X & (\text{CC}) \\ \nu_\ell + X & (\text{NC}) \end{cases}$$

Flavor composition:

$$(\nu_e : \nu_\mu : \nu_\tau) = (1 : 2 : 0)_\star \longrightarrow (1 : 1 : 1)_\oplus.$$

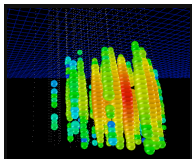
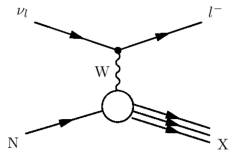


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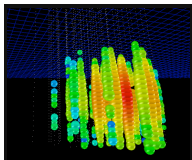
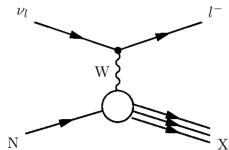
CC EM/NC all  
(shower)

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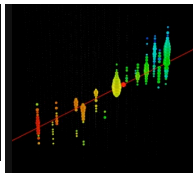
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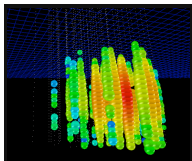
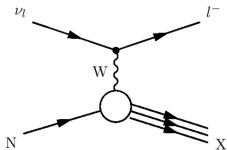
CC Muon (track)

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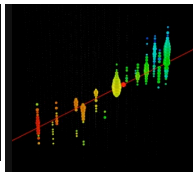
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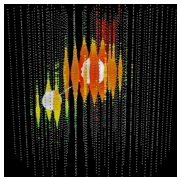
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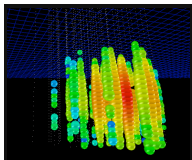
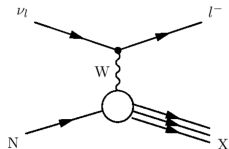
CC tau 'double bang'  
(only at  $E_\nu \gtrsim 100$  TeV)

# High-energy neutrino signals at IceCube

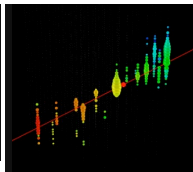
$$\nu_\ell + N \rightarrow \begin{cases} \ell + X & (\text{CC}) \\ \nu_\ell + X & (\text{NC}) \end{cases}$$

Flavor composition:

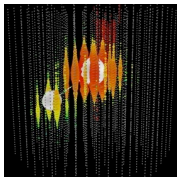
$$(\nu_e : \nu_\mu : \nu_\tau) = (1 : 2 : 0)_\star \longrightarrow (1 : 1 : 1)_\oplus.$$



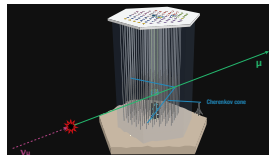
CC EM/NC all  
(shower)



CC Muon (track)



CC tau 'double bang'  
(only at  $E_\nu \gtrsim 100$  TeV)



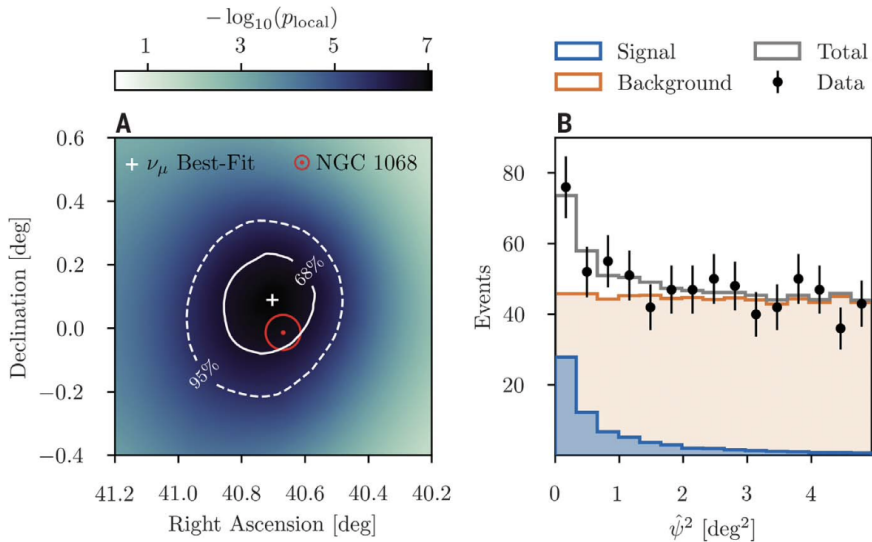
Throughgoing muon  
(track only, huge statistics)

[Picture courtesy: C. Kopper]

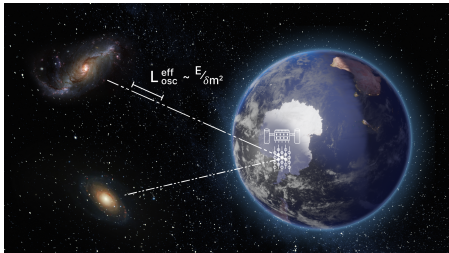
**Showers:** Good energy resolution, but poor angular resolution

**Tracks:** Excellent angular resolution ( $< 1^\circ$ ), but modest energy resolution ( $\sim 30\%$ )

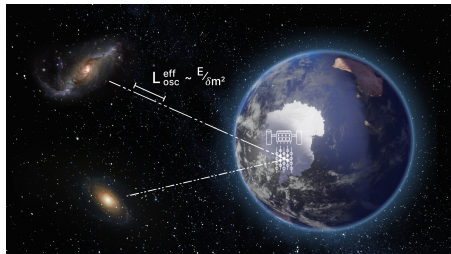
**Track events are ideal for astrophysical source identification.**



# A new probe of pseudo-Dirac neutrinos



# A new probe of pseudo-Dirac neutrinos

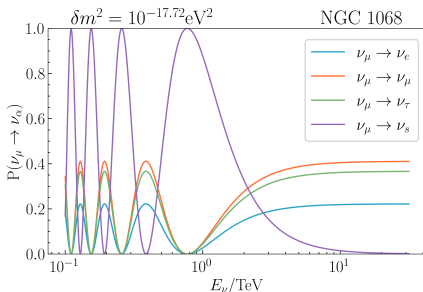


Carlóni, Martínez-Soler, Argüelles, Babu, BD, 2212.00737

- Oscillation probability:

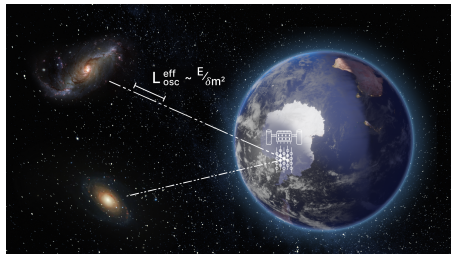
$$P_{\alpha\beta} = \frac{1}{2} \sum_{j=1}^3 |U_{\beta j}|^2 |U_{\alpha j}|^2 \left[ 1 + \cos \left( \frac{\delta m_j^2 L_{\text{eff}}}{2E_\nu} \right) \right],$$

with  $L_{\text{eff}} = \int \frac{dz}{H(z)(1+z)^2}$  and  $H(z) = H_0 \sqrt{\Omega_m(1+z)^3 + \Omega_\Lambda + (1 - \Omega_m - \Omega_\Lambda)(1+z)^2}$ .

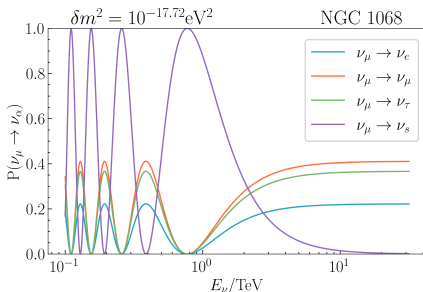




# A new probe of pseudo-Dirac neutrinos



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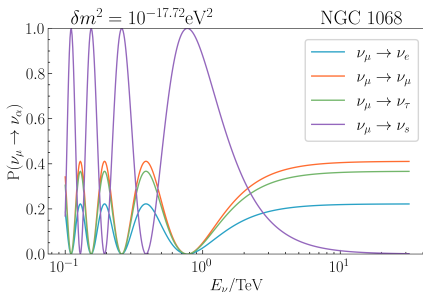
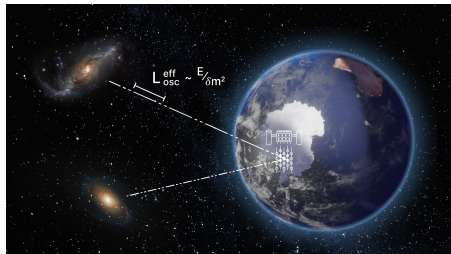
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- Typical oscillation length:  $L_{\text{osc}} = \frac{2E_\nu}{\delta m^2} \approx 6.4 \text{ Mpc} \left( \frac{E_\nu}{1 \text{ TeV}} \right) \left( \frac{2 \times 10^{-18} \text{ eV}^2}{\delta m^2} \right)$ .

# A new probe of pseudo-Dirac neutrinos



Carlóni, Martínez-Soler, Argüelles, Babu, BD, 2212.00737

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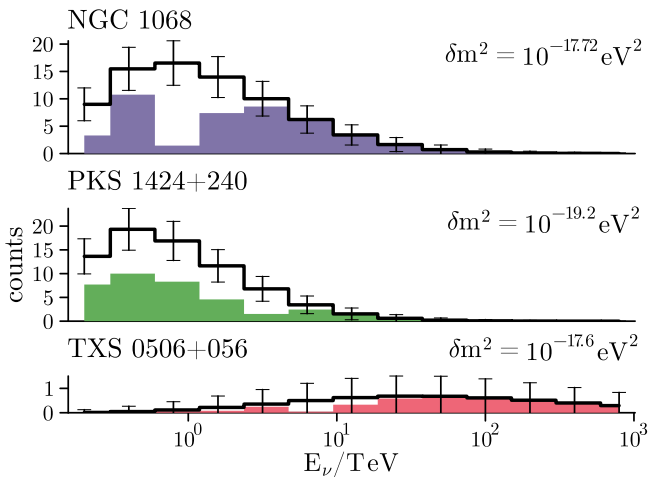
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- Typical coherence length: [Kersten, Smirnov, 1512.09068 (EPJC '16); Rink, Sen, 2211.16520]

$$L_{\text{coh}} = \frac{4\sqrt{2}E_\nu^2}{|\delta m^2|} \approx 10^{10} \text{ Mpc} \left( \frac{E_\nu}{1 \text{ TeV}} \right)^2 \left( \frac{2 \times 10^{-18} \text{ eV}^2}{|\delta m^2|} \right) \left( \frac{\sigma_x}{10^{-10} \text{ m}} \right) \gg L_{\text{osc}}.$$

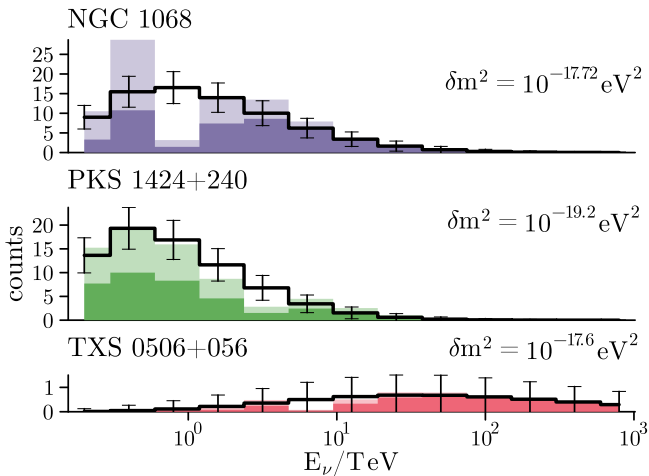
# Event Distributions

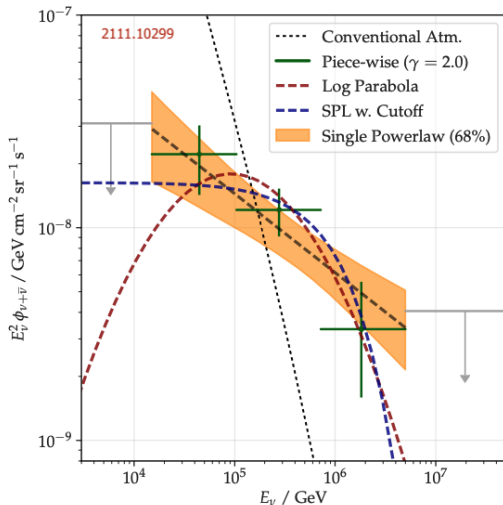
Source	Source Type	$-\log_{10} p_{\text{local}}$	$\hat{n}_s$	$\hat{\gamma}$	$z$
NGC 1068	SBG/AGN	7.0 ( $5.2\sigma$ )	79	3.2	0.0038 (16 Mpc)
PKS 1424+240	BLL	4.0 ( $3.7\sigma$ )	77	3.5	0.6047 (2.6 Gpc)
TXS 0506+056	BLL/FSRQ	3.6 ( $3.5\sigma$ )	5	2.0	0.3365 (1.4 Gpc)



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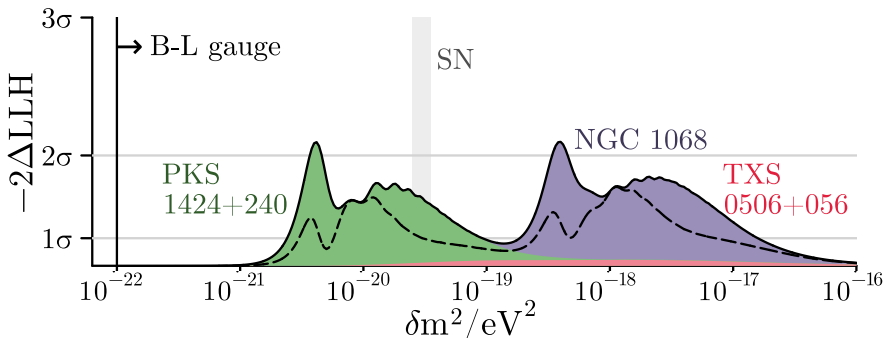


[IceCube Collaboration, 2111.10299 (ApJ '22)]

$$\Phi(E_\nu) = \begin{cases} \Phi_0 (E_\nu/E_0)^{-\gamma} & \text{(single power law)} \\ \Phi'_0 (E_\nu/E_0)^{-\gamma'} e^{-E_\nu/E_{\text{cutoff}}} & \text{(SPL with cutoff)} \\ \Phi''_0 \cdot (E/E_0)^{-(\alpha+\beta \log(E/E_0))} & \text{(log parabola)} \end{cases}$$

# First IceCube constraints on $\delta m^2$

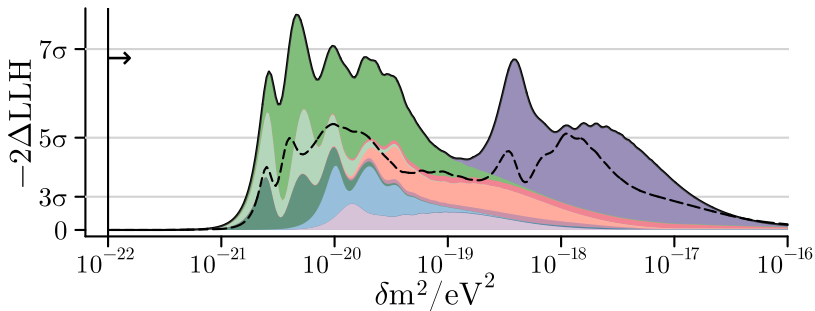
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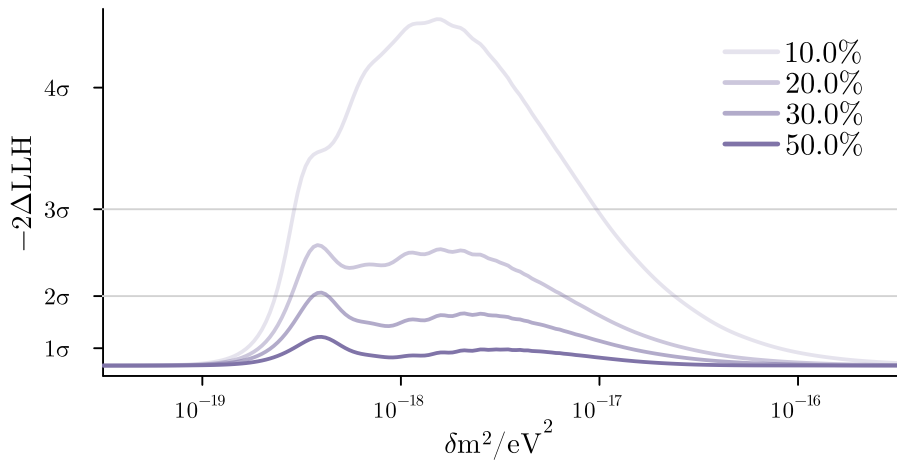
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# Future IceCube-Gen2 sensitivity

Source	Source Type	$-\log_{10} p_{\text{local}}$	$\hat{n}_s$	$\hat{\gamma}$	$z$
NGC 1068	SBG/AGN	7.0	79	3.2	0.0038
PKS 1424+240	BLL	4.0	77	3.5	0.6047
TXS 0506+056	BLL/FSRQ	3.6	5	2.0	0.3365
S5 1044+71	FSRQ	1.3	45	4.3	1.1500
IC 678	GAL	0.9	22	3.1	0.04799
NGC 5380	GAL	0.9	4	2.4	0.010584
B2 1520+31	FSRQ	1.0	35	4.3	1.48875
PKS 1717+177	BLL	1.0	34	4.3	0.137
3C 454.3	FSRQ	1.2	1	1.5	0.859
GB6 J1542+6129	BLL	1.9	16	4.3	0.117

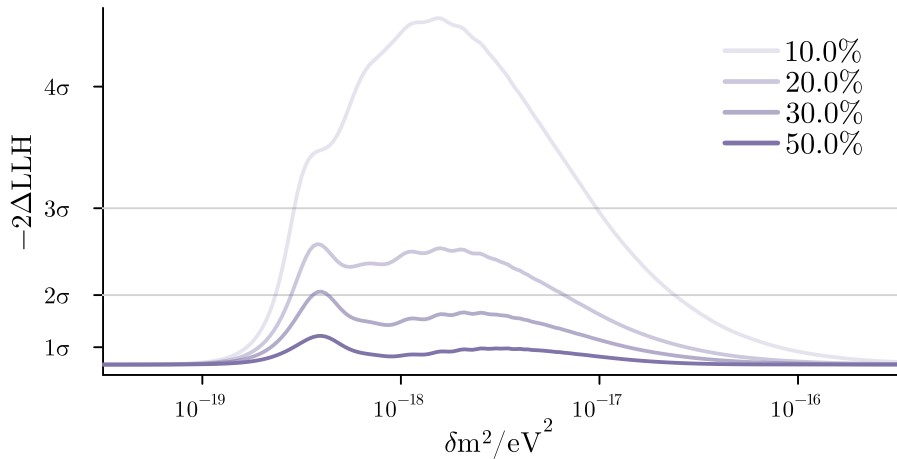


## Effect of energy resolution





## Effect of energy resolution



- Lot of room for improvement with better technology.
- Showers can do much better, if the angular resolution can be improved somehow.
- Possible with KM3NeT or P-ONE (or something even bigger and better).



# Conclusion

- The nature of neutrino mass (Majorana, Dirac, or pseudo-Dirac) has to be *experimentally* determined.
- We proposed a new experimental probe of pseudo-Diracness of neutrinos using high-energy astrophysical neutrinos.
- Made possible by recent breakthroughs in multi-messenger neutrino astrophysics.
- **Current IceCube data on the three most significant astrophysical neutrino sources already constrain  $\delta m^2$  in the range of  $10^{-21} - 10^{-16} \text{ eV}^2$  with up to  $2\sigma$  significance.**
- With additional sources and more statistics at IceCube-Gen2 (+KM3NeT), a larger range of  $\delta m^2$  can be probed with higher significance.
- Robust against astrophysical flux and flavor ratio uncertainties.

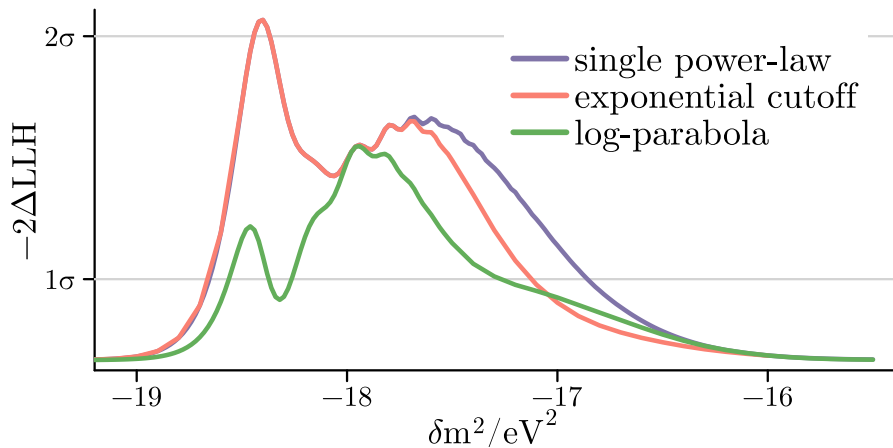
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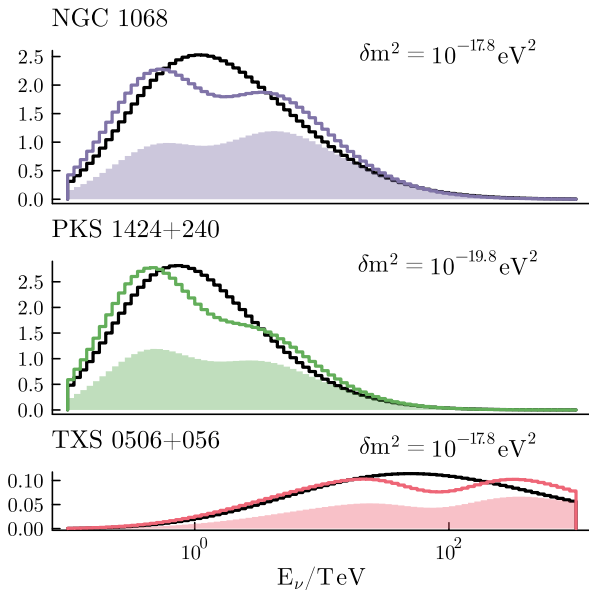
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**Thank You.**

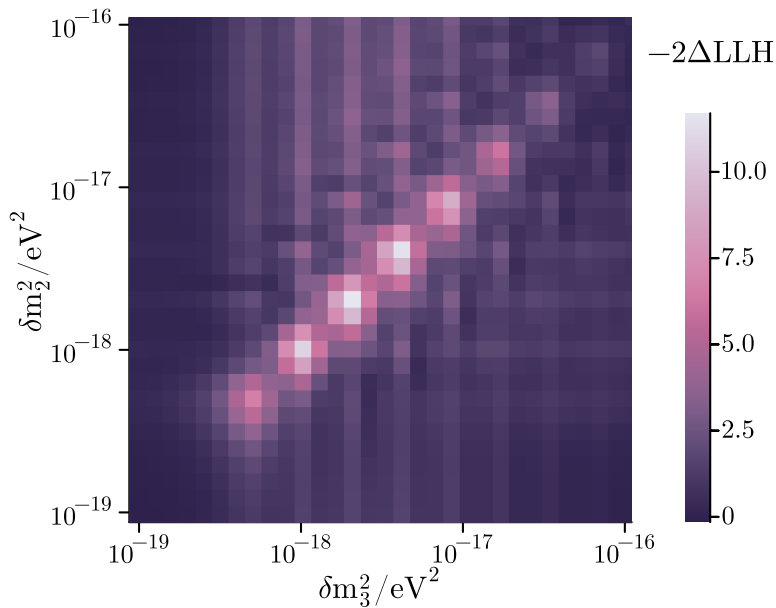
## **Backup Slides**

## Different flux models

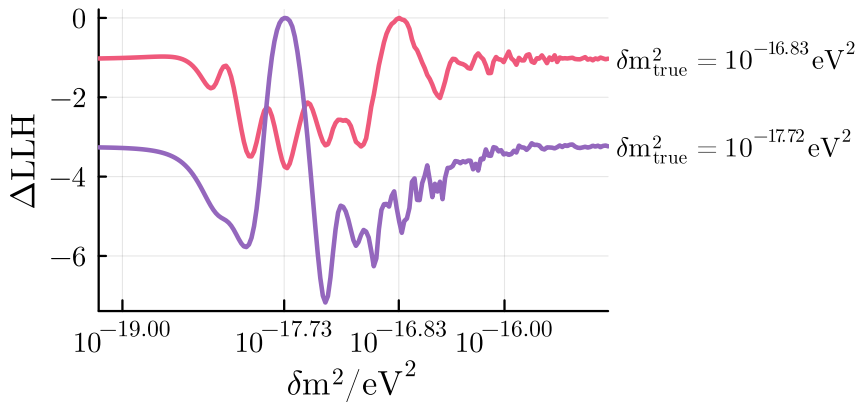




## Different mass splittings

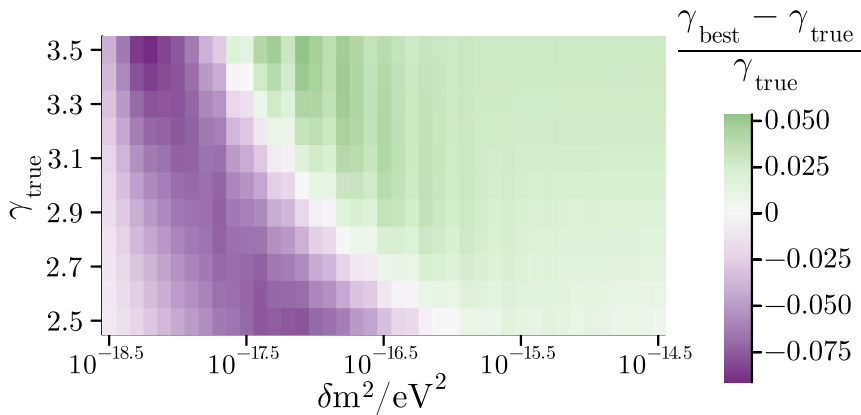


## Recovery of true pseudo-Dirac parameters

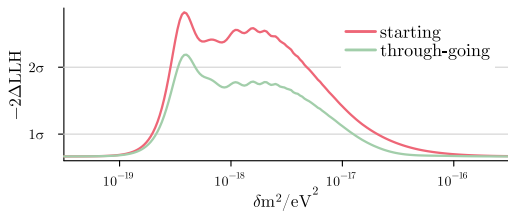
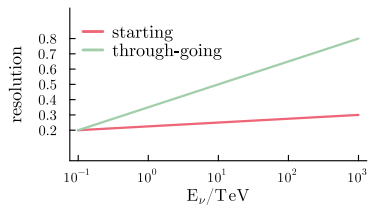




## Standard Model fits to pseudo-Dirac reality



# Linear models for energy resolution



# Solar neutrino constraint

