

1. a) b)

$$h = 6.63 \times 10^{-34};$$

$$c = 3 \times 10^8;$$

$$k = 1.38 \times 10^{-23};$$

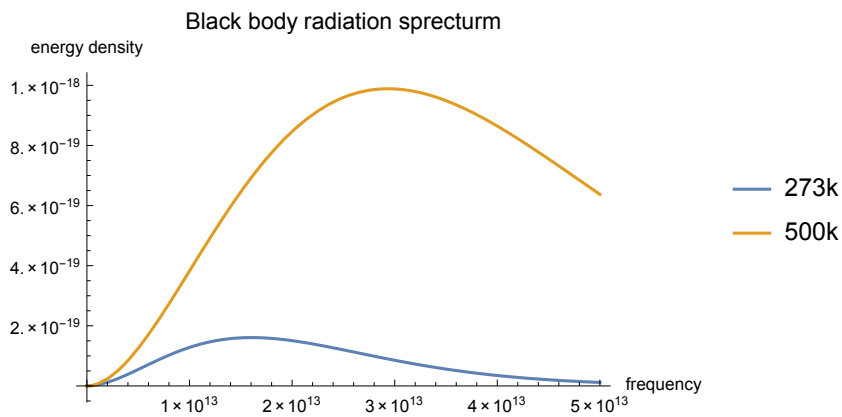
$$t1 = 273;$$

$$t2 = 500;$$

$$c = 3 \times 10^8;$$

$$\text{planck}[f_, t_] := 8 \pi h f^3 / ((c^3) * (E^{h f / (k t)} - 1));$$

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Plot[{planck[f, t1], planck[f, t2]}, {f, 0, 5 \times 10^{13}}, PlotRange \to Full,  
PlotLegends \to {"273k", "500k"}, AxesLabel \to {"frequency", "energy density"},  
PlotLabel \to "Black body radiation spectrum"]
```



c)

$$i = \text{Integrate}[\text{planck}[f, t] * c / 4, \{f, 0, \text{Infinity}\}, \text{Assumptions} \to t > 0]$$

$$5.64185 \times 10^{-8} t^4$$

2. left hand side

$$v = \{x, x, x\};$$

$$\text{Integrate}[\{0, 0, 1\}.\text{Curl}[v, \{x, y, z\}], \{y, -1, 0\}, \{x, -y-1, y+1\}] +$$

$$\text{Integrate}[\{0, 0, 1\}.\text{Curl}[v, \{x, y, z\}], \{y, 0, 1\}, \{x, y-1, -y+1\}]$$

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right hand side

$$\text{Integrate}[v.\{1, -1, 0\}, \{x, 1, 0\}] + \text{Integrate}[v.\{1, 1, 0\}, \{x, 0, -1\}] +$$

$$\text{Integrate}[v.\{1, -1, 0\}, \{x, -1, 0\}] + \text{Integrate}[v.\{1, 1, 0\}, \{x, 0, 1\}]$$

2